

# Improvement on Exoplanet Detection Methods and Analysis via Gaussian Process Fitting Techniques



Bryce B. A. Van Ross<sup>1, 2</sup>, Johanna K. Teske<sup>2</sup>

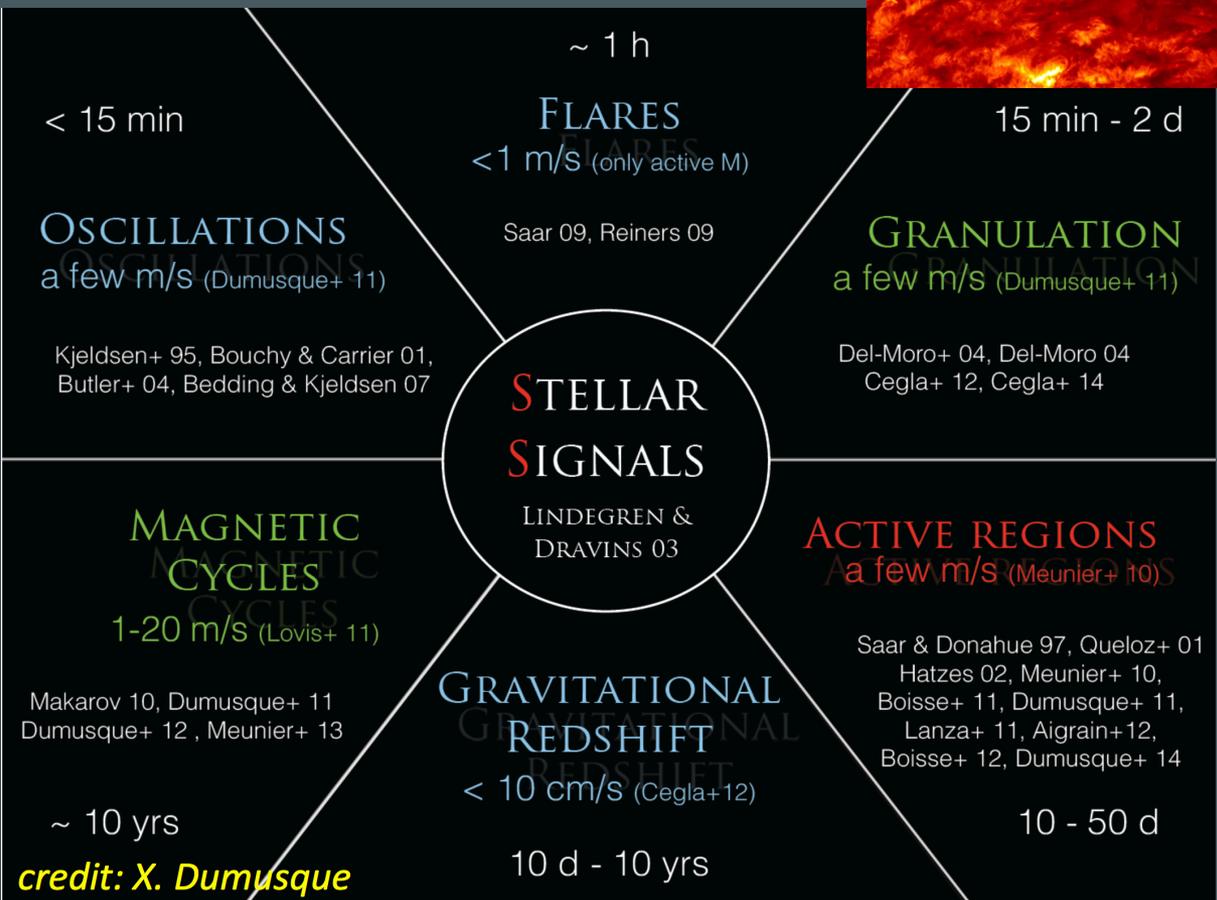
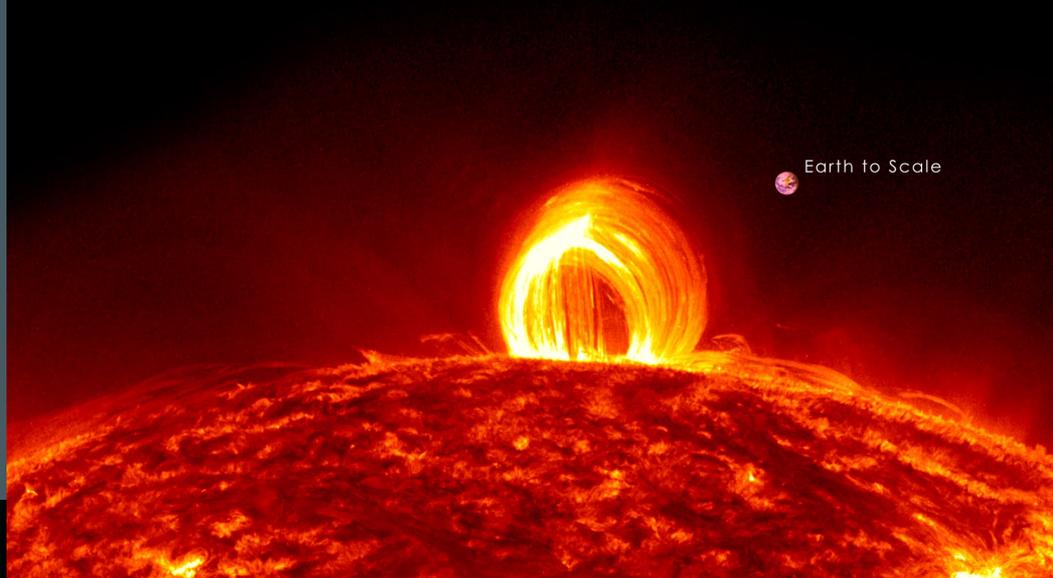
<sup>1</sup>Dept. of Mathematics, CSU Los Angeles

<sup>2</sup>Carnegie Observatories

# Motivation

- Finding (*small*) exoplanets proves difficult ... but possible!
- Existing problems include:
  - Our instrumentation isn't precise enough (*should be 10cm/s*).
  - Stellar activity of host stars complicate our readouts of planetary signals.

# Stellar Activity Sources



credit: X. Dumusque

Bryce Van Ross, 09/19/17

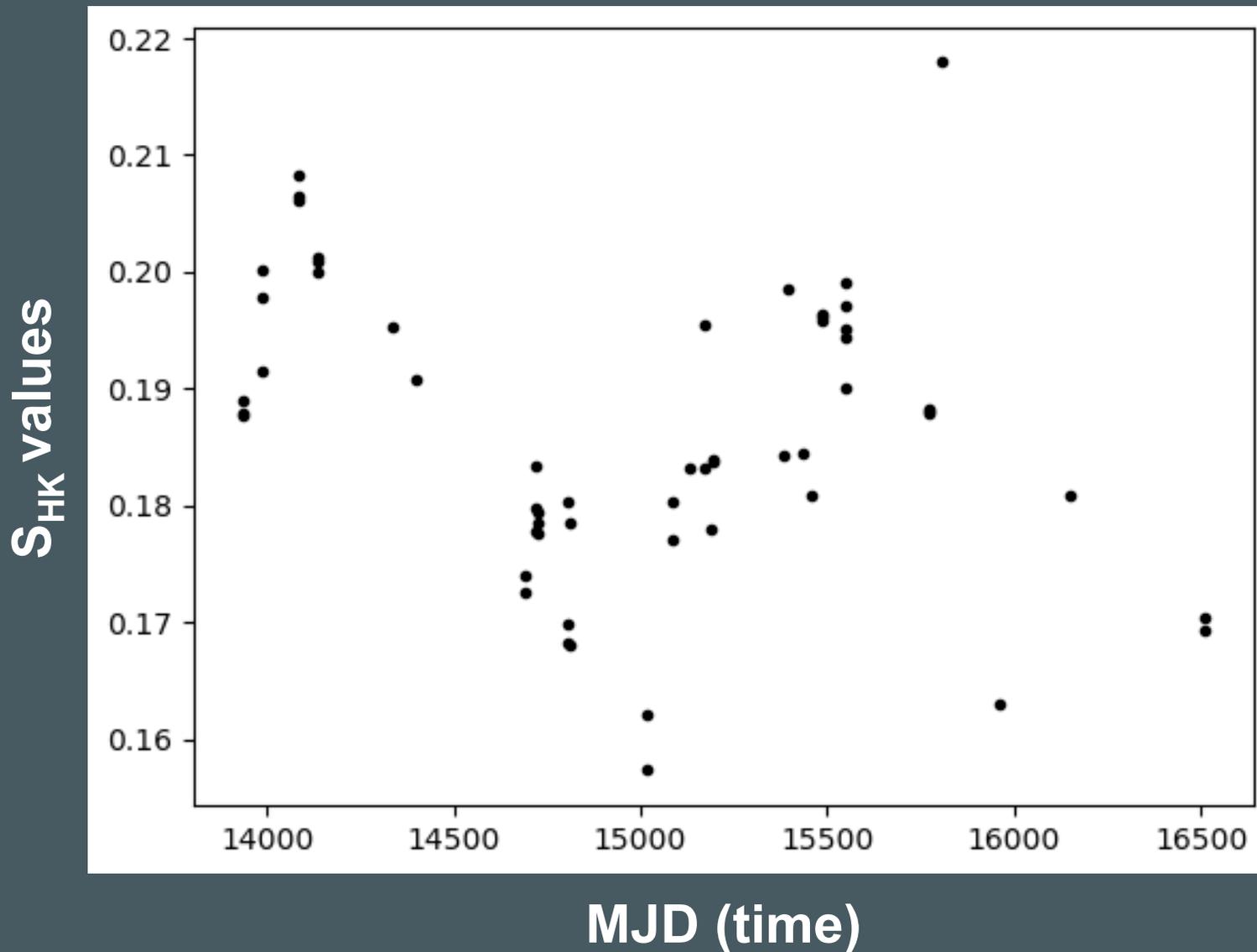
# Solution

- Gaussian Process (GP) fits of stellar data.

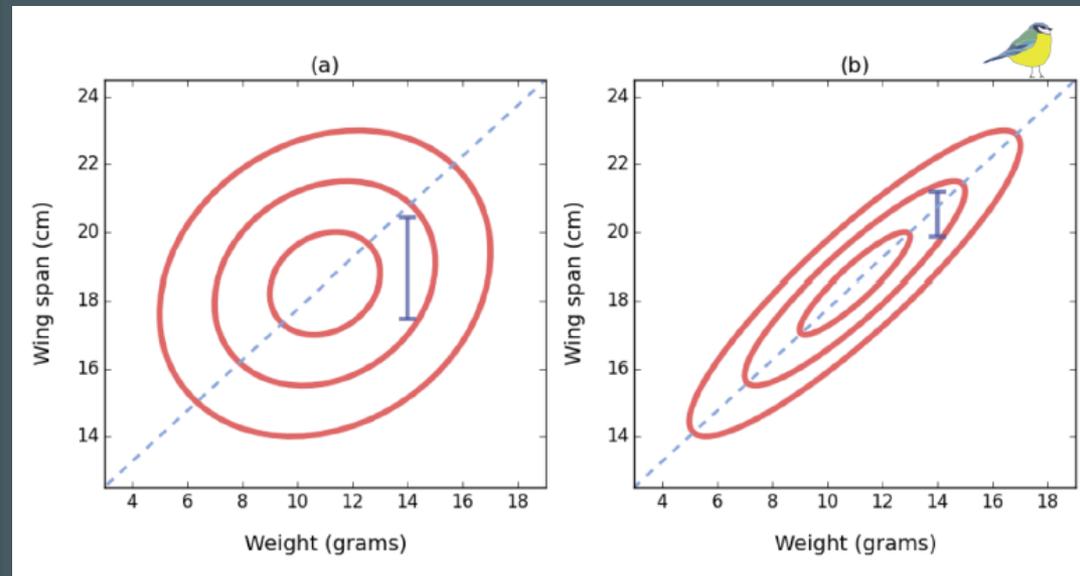
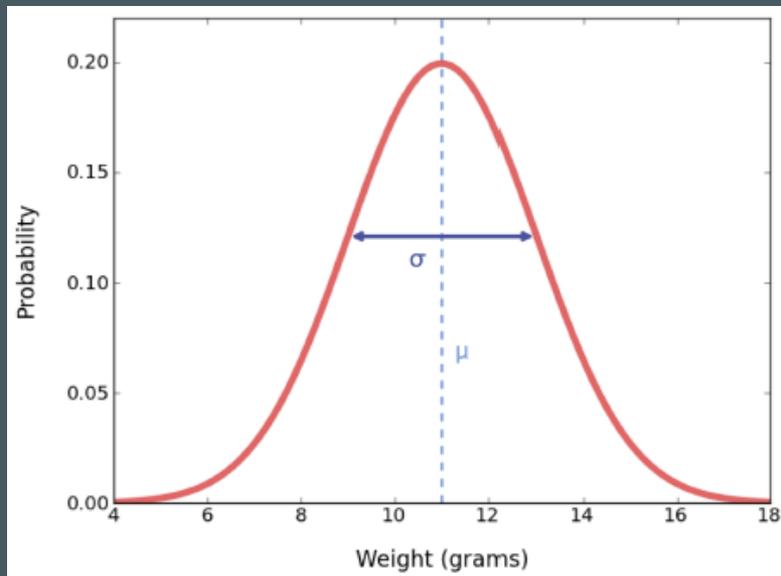
## Why?

- GP has proven itself successful in astrophysical and other fields.
- Ex: time series analyses to infer physical properties; exoplanet population; exoplanet detection via RV data.

# Example of Measurements



# What are Gaussian Processes?

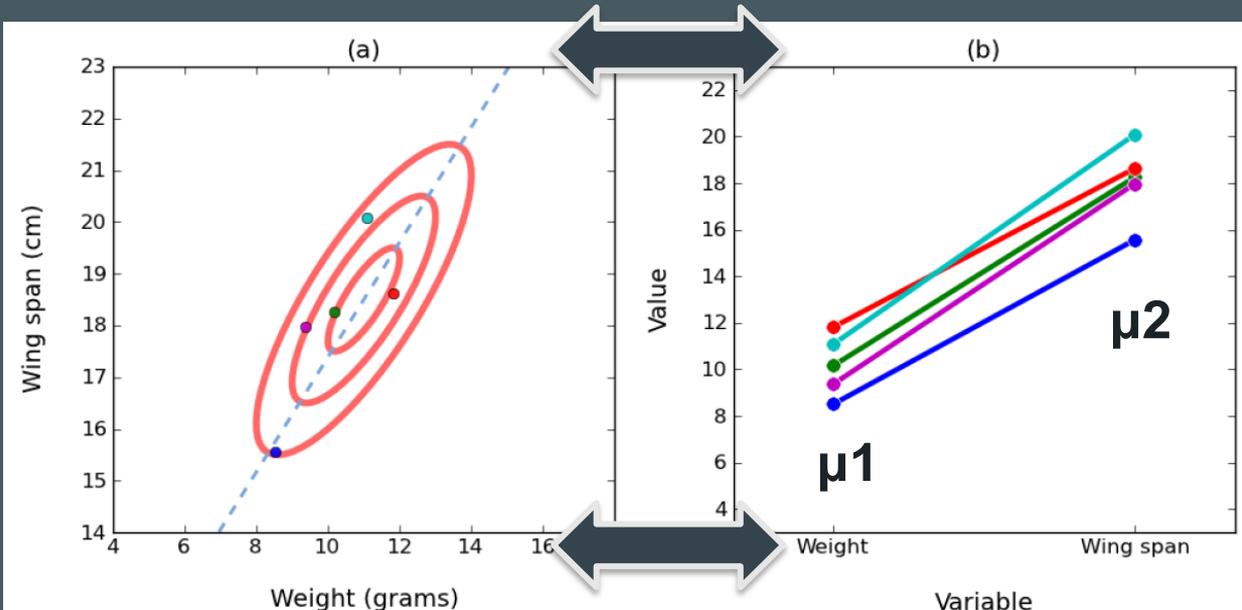


$$P(y) = \frac{1}{\sigma \sqrt{2\pi}} \exp^{-\frac{1}{2} \left( \frac{y-\mu}{\sigma} \right)^2}$$

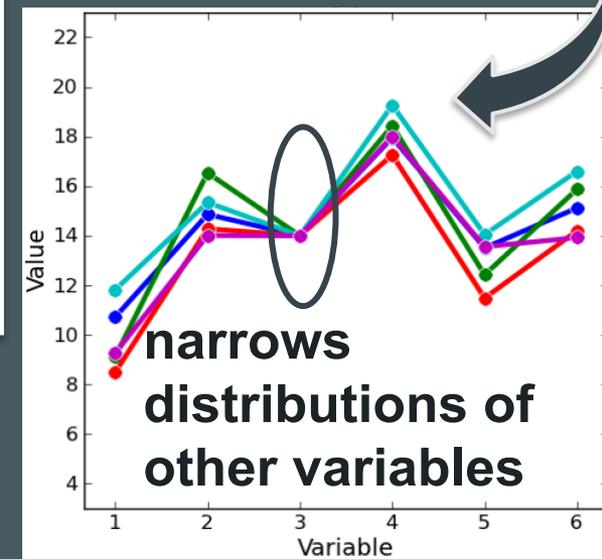
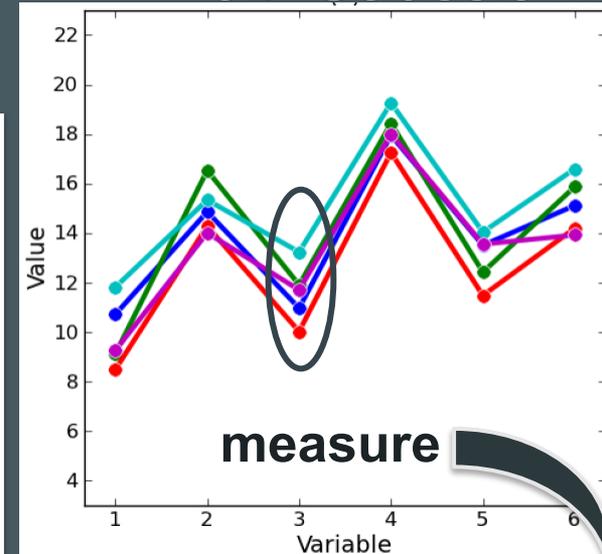
Standard deviation      Mean

2 dimensional Gaussian  
 $\sigma$  is now width of ellipse  
ellipses now centered on  $\mu$

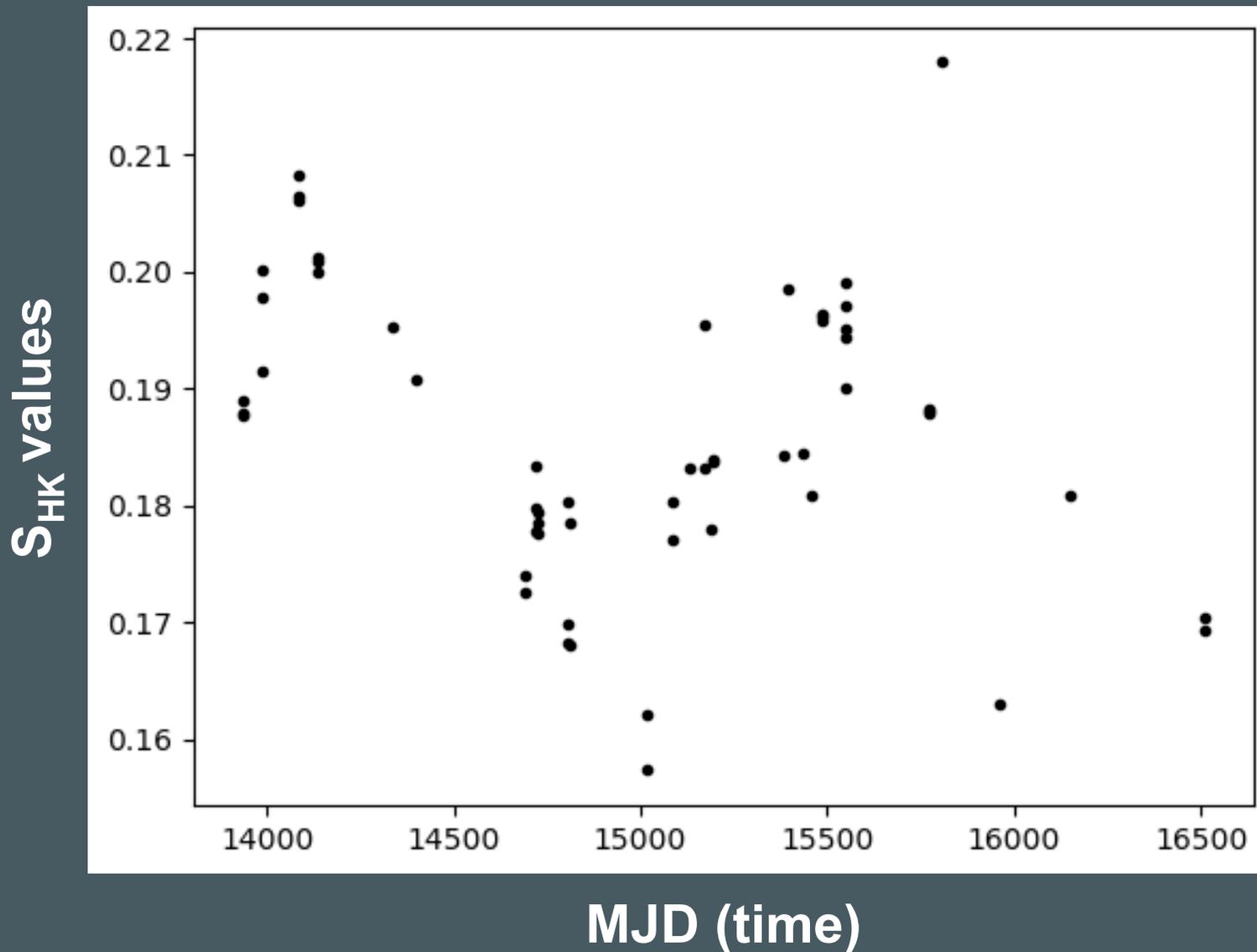
# What are Gaussian Processes? 6D Gaussian!



New way to represent 2D Gaussian:  
5 samples from joint prior distribution of  
two variables



# What are Gaussian Processes?

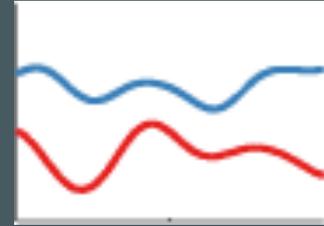


# What are Gaussian Processes?

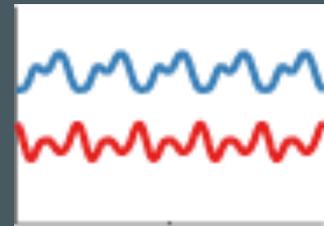
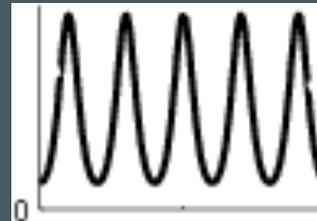
- Definition:
  - Function(s) of covariance amongst variables that change collectively.
- We use GP to measure correlation of our stellar data.
- Different GP's affect the quality of your fits.
  - Difficulty is determining appropriate parameters and models.

# Kernels (covariance functions)

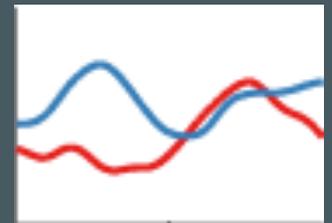
$$k_{\text{SE}}(x, x') = \sigma^2 \exp\left(-\frac{(x-x')^2}{2\ell^2}\right)$$



$$k_{\text{Per}}(x, x') = \sigma^2 \exp\left(-\frac{2 \sin^2(\pi|x-x'|/p)}{\ell^2}\right)$$

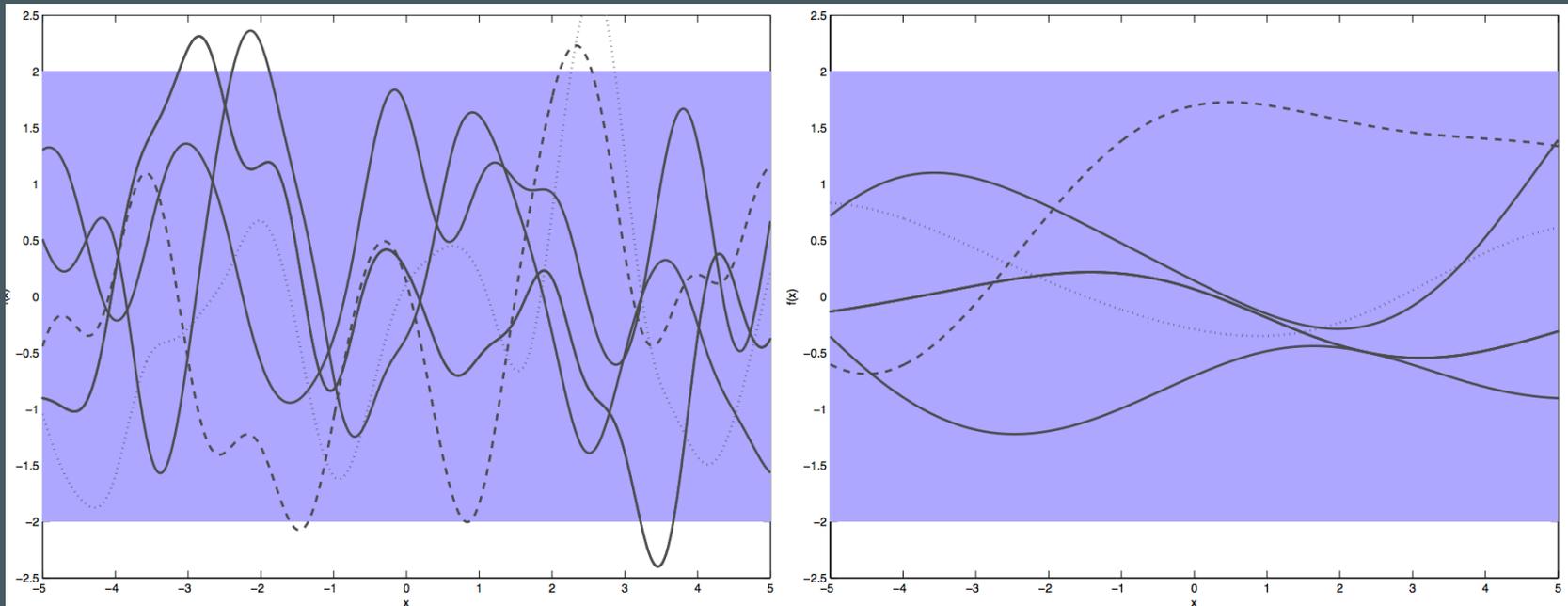


$$k_{\text{RQ}}(x, x') = \sigma^2 \left(1 + \frac{(x-x')^2}{2\alpha\ell^2}\right)^{-\alpha}$$



*Photo Credit: David Duvenaud, "The Kernel Cookbook: Advice on Covariance functions"*

# Hyperparameters (what control kernels)



(a) small length scale

(b) large length scale

**Figure 2.4:** Random samples from a Gaussian process prior with squared exponential covariance function. The left panel shows a small SE with small length scale value (0.5), whereas the right panel has a much larger value (3).

*Photo Credit: Markus Schneider 's Thesis, "Learning from Demonstration with Gaussian Processes"*

# Methods

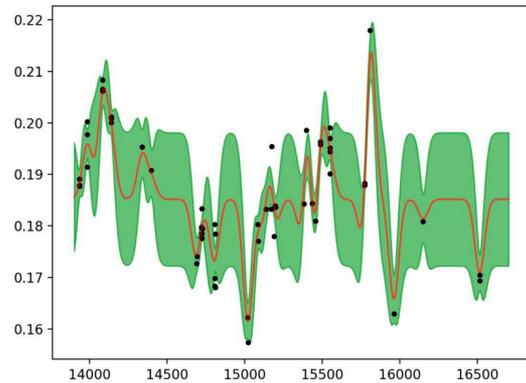
- Sample S-values (Ca II H and K measurements) of stars from Keck/HIRES.
- Apply GP to fit data and measure correlation.
- Adjust hyperparameters and/or consider alternative combination of kernels, until optimized.

Method

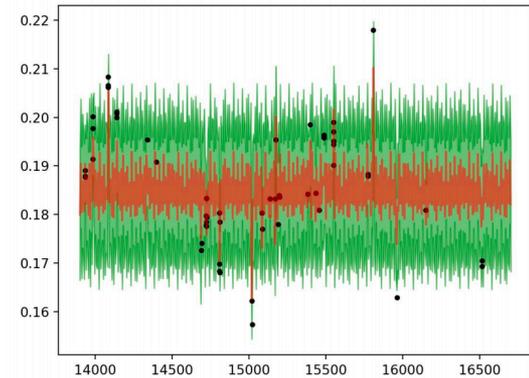


# Qualitative GP Fits

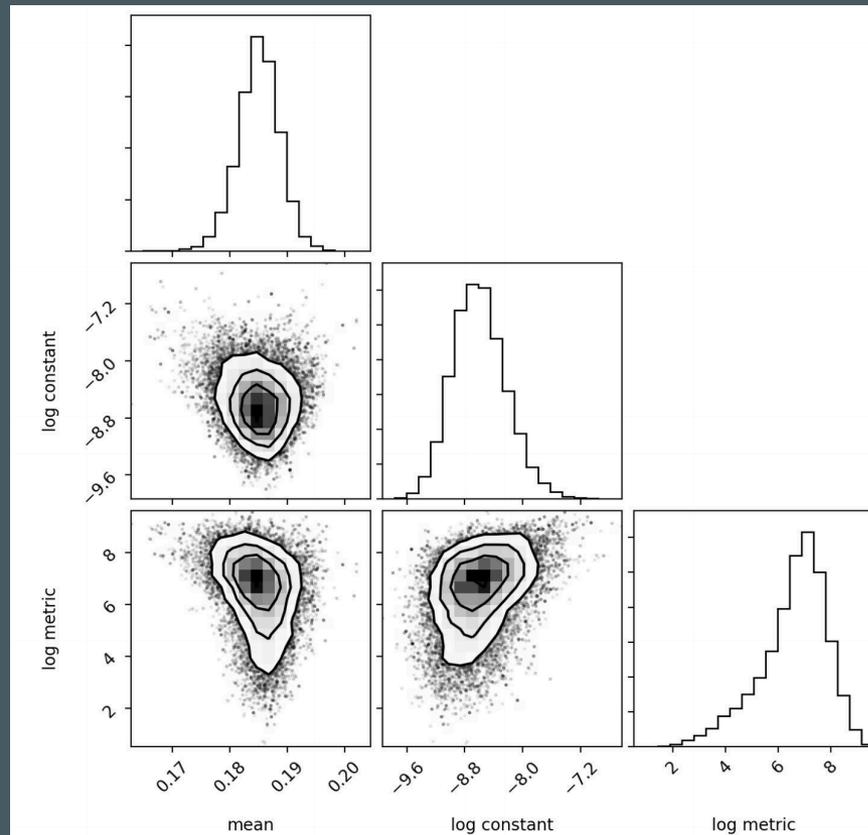
**HD 4915 SE**



**HD 4915 SE+Per (w.n.)**



# Corner Plots



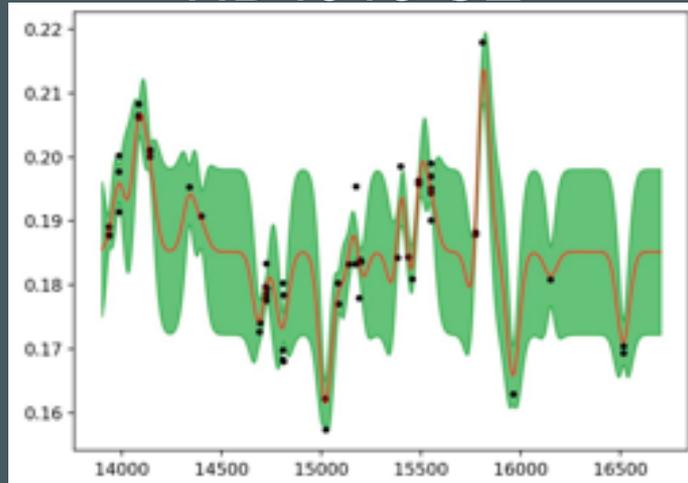
# Likelihood

$$\text{BIC} = \ln(\text{sample size}) * \text{parameters} + (\text{max log likelihood})$$

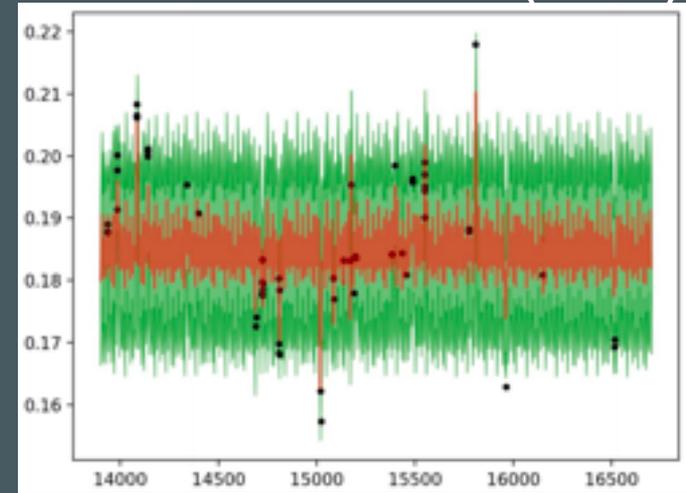
| Star, Kernel (White Noise)        | Fun Value | BIC       | Delta BIC |
|-----------------------------------|-----------|-----------|-----------|
| HD4915, SE                        | -197.654  | -383.179  | 0         |
| HD4915, SE (White Noise)          | -197.654  | -379.136  | 4.043     |
| HD4915, Per                       | -186.594  | -357.016  | 26.163    |
| HD4915, Per (White Noise)         | -187.684  | -355.153  | 28.026    |
| HD4915, SE+Per                    | -181.964  | -339.670  | 43.509    |
| HD4915, SE+Per (White Noise)      | -173.01   | -317.719  | 65.460    |
| HD4915, RQ                        | -198.388  | -380.604  | 2.575     |
| HD4915, RQ (White Noise)          | -198.388  | -376.561  | 6.618     |
| HD4915, SE+Per+RQ                 | -198.967  | -361.547  | 21.632    |
| HD4915, SE+Per+RQ (White Noise)   | -198.927  | -357.423  | 25.755    |
|                                   |           |           |           |
| HD10700, SE                       | -2677.292 | -5334.680 | 119.253   |
| HD10700, SE (White Noise)         | -2706.79  | -5387.041 | 66.892    |
| HD10700, Per                      | -2492.059 | -4957.579 | 496.354   |
| HD10700, Per (White Noise)        | -2593.152 | -5153.131 | 300.803   |
| HD10700, SE+Per                   | -2677.292 | -5314.776 | 139.157   |
| HD10700, SE+Per (White Noise)     | -2677.292 | -5308.142 | 145.792   |
| HD10700, RQ                       | -2740.236 | -5453.933 | .000      |
| HD10700, RQ (White Noise)         | -2740.236 | -5447.299 | 6.635     |
| HD10700, SE+Per+RQ                | -2677.292 | -5294.872 | 159.061   |
| HD10700, SE+Per+RQ (White Noise)  | -2752.542 | -5438.738 | 15.196    |
|                                   |           |           |           |
| HD154345, SE                      | -654.593  | -1293.145 | 49.253    |
| HD154345, SE (White Noise)        | -654.593  | -1287.798 | 54.600    |
| HD154345, Per                     | -536.803  | -1052.218 | 290.180   |
| HD154345, Per (White Noise)       | -539.691  | -1052.646 | 959.219   |
| HD154345, SE+Per                  | -668.098  | -1304.113 | 38.284    |
| HD154345, SE+Per (White Noise)    | -654.593  | -1271.756 | 70.641    |
| HD154345, RQ                      | -681.893  | -1342.398 | .000      |
| HD154345, RQ (White Noise)        | -681.893  | -1337.050 | 5.347     |
| HD154345, SE+Per+RQ               | -682.329  | -1316.534 | 25.864    |
| HD154345, SE+Per+RQ (White Noise) | -692.065  | -1330.659 | 11.739    |

# Results

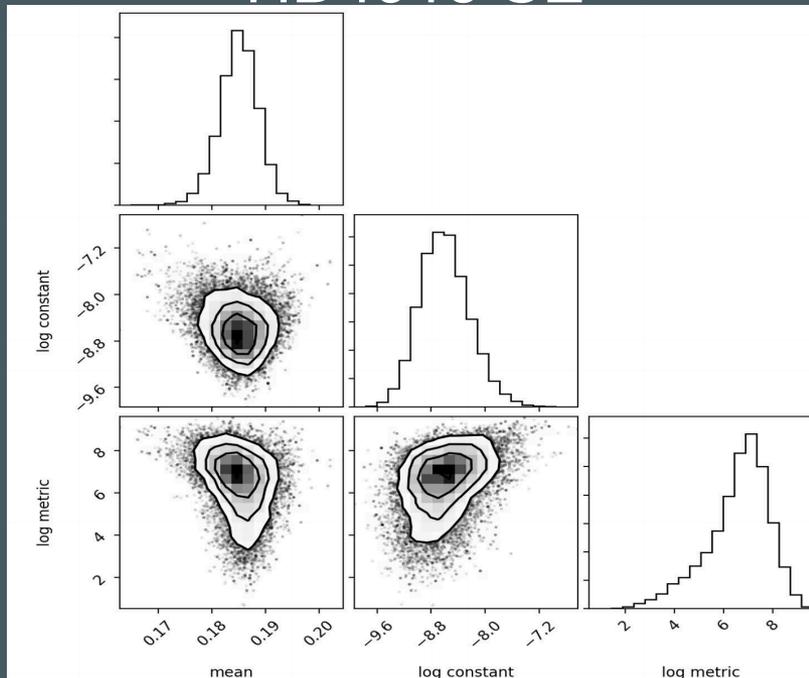
HD4915 SE



HD4915 SE+Per (w.n.)



HD4915 SE

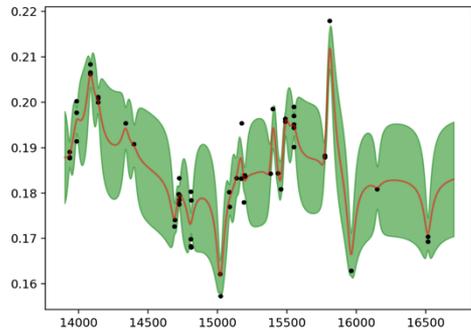


Bayesian Information Criterion  
(BIC):

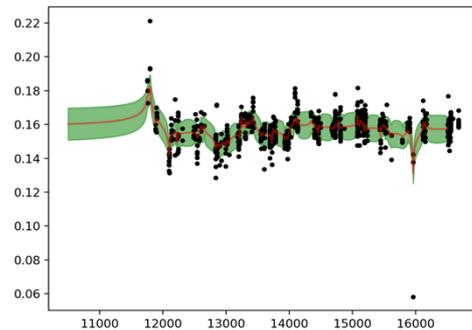
$\ln(\text{sample size}) \times \text{parameters} +$   
 $\text{max log likelihood}$

# What's the Best Fit?

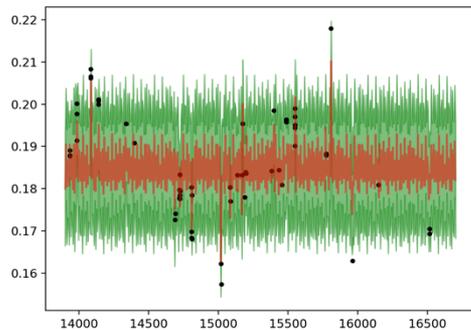
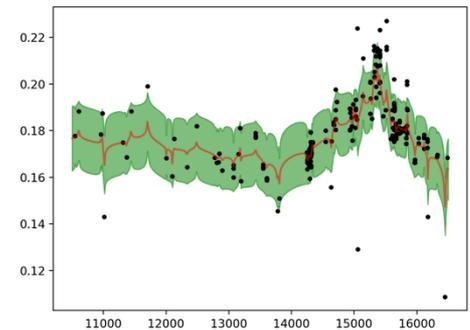
HD4915 RQ



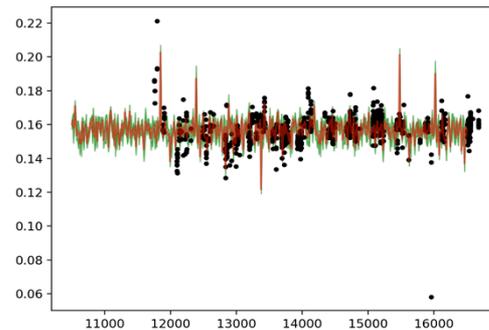
HD10700 RQ



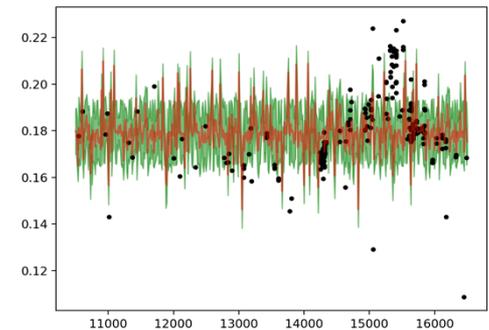
HD154345 RQ



HD4915 SE+Per  
(w. noise)



HD10700 Per

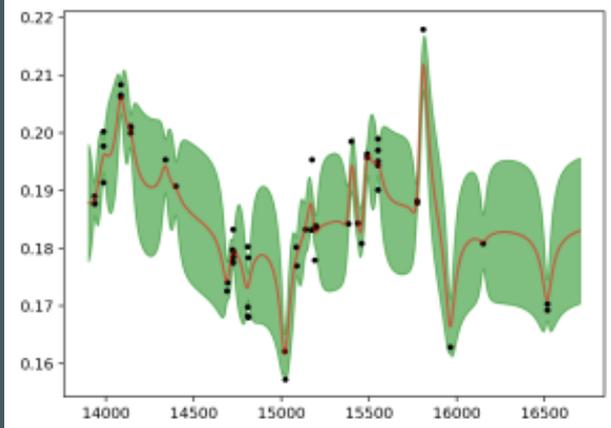


HD154345 Per (w.  
noise)

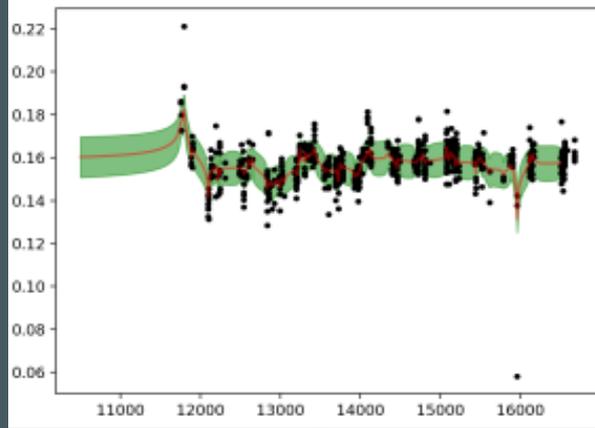
# Conclusions Thus Far

- Per and Per(w. noise) fit the data poorly.
- RQ, RQ(w. noise), and SE+Per+RQ(w. noise) are likely the best kernels.
- Hyperparameters need reevaluation, but some are well constrained.

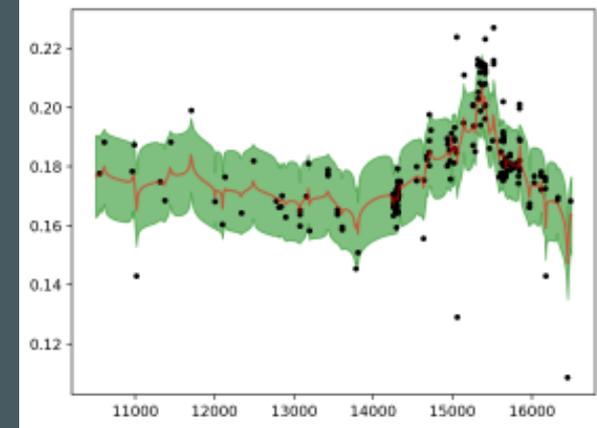
HD4915 RQ



HD10700 RQ



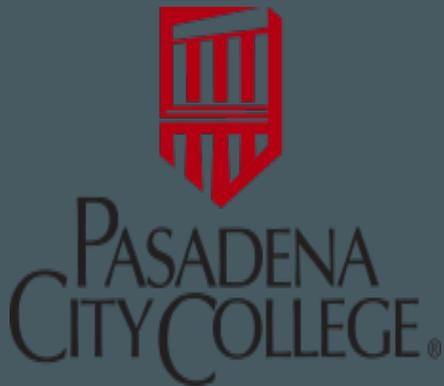
HD154345 RQ



# Next Steps

- Can we infer the same results with H-alpha?
- Apply to RV data of same stars
  - **Method 1:** Subtract our stellar fit from RV model, then fit residuals using Keplerian parameters.
  - **Method 2:** Simultaneously unite our stellar fit with Keplerian.
  - Interpret Keplerian parameters.
- GP fits to the stellar activity data not well constrained?  
Maybe need more observations to reliably remove the stellar activity signal, reveal real planetary signals in RVs.

# Acknowledgements



*Further Questions?*

Feel free to email me at:

[bvanros@calstatela.edu](mailto:bvanros@calstatela.edu)

Bryce Van Ross, 09/19/17