

A 4D hypercube (tesseract) is depicted with a light blue wireframe. Three Earth globes are positioned at three of its vertices: one at the top, one at the bottom-left, and one at the bottom-right. Each globe is enclosed in a colored oval border (blue, pink, and yellow respectively).

# Habitability in 4-D

A. Adams, C. Colose, S. Kane, A. Merelli, M. Turnbull

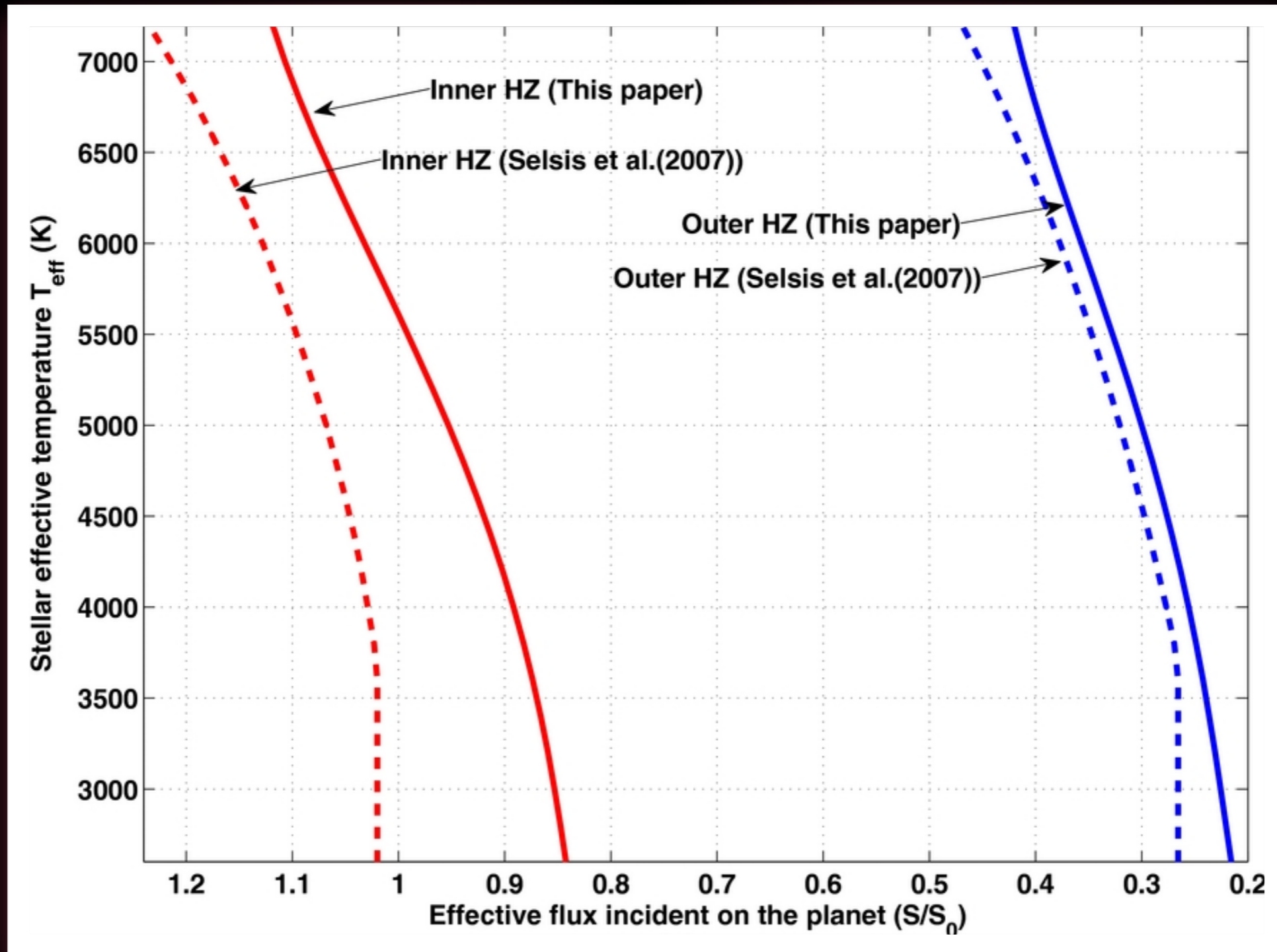
**How does**  
**climate-based habitability**  
**on Earth-like worlds**  
**vary with rotation and orbital state?**

# Key Points

- Rotation period is the primary influence on habitability
  - ➔ Obliquity influences habitability at “faster” rotations ( $\lesssim 20$  days); beyond this there’s a break in habitability where obliquity isn’t as important
  - ➔ Orbital eccentricity has the weakest effect of all (up to our limit of  $e = 0.225$ )
- A Gaussian process regression does a reasonable job of predicting a global+orbit-averaged climate habitability metric

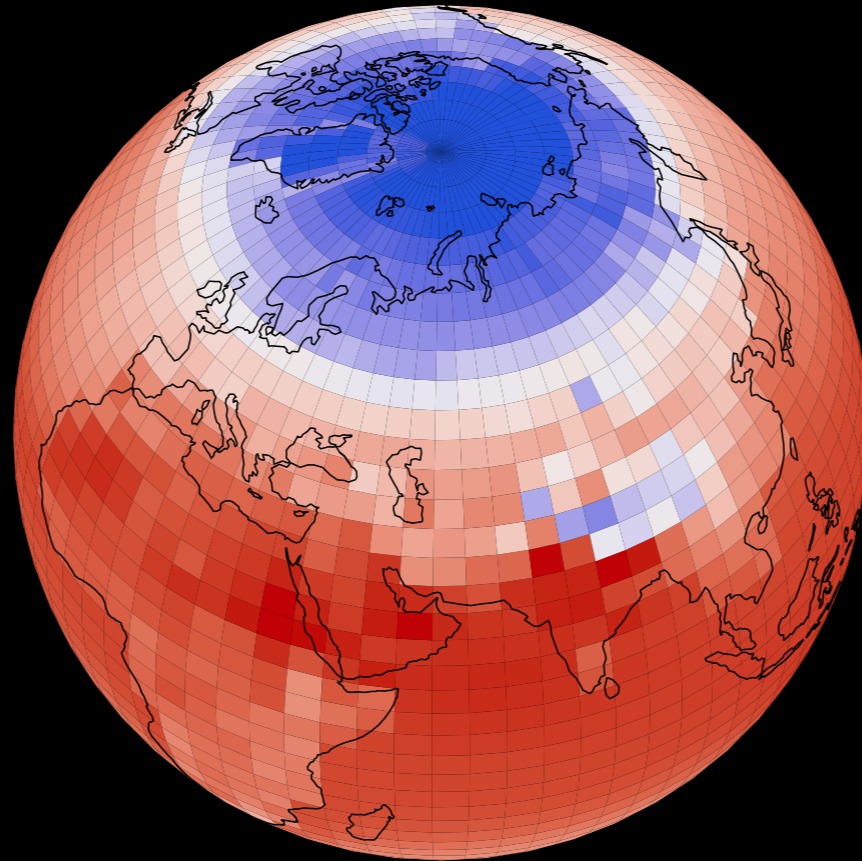
# Defining Habitability

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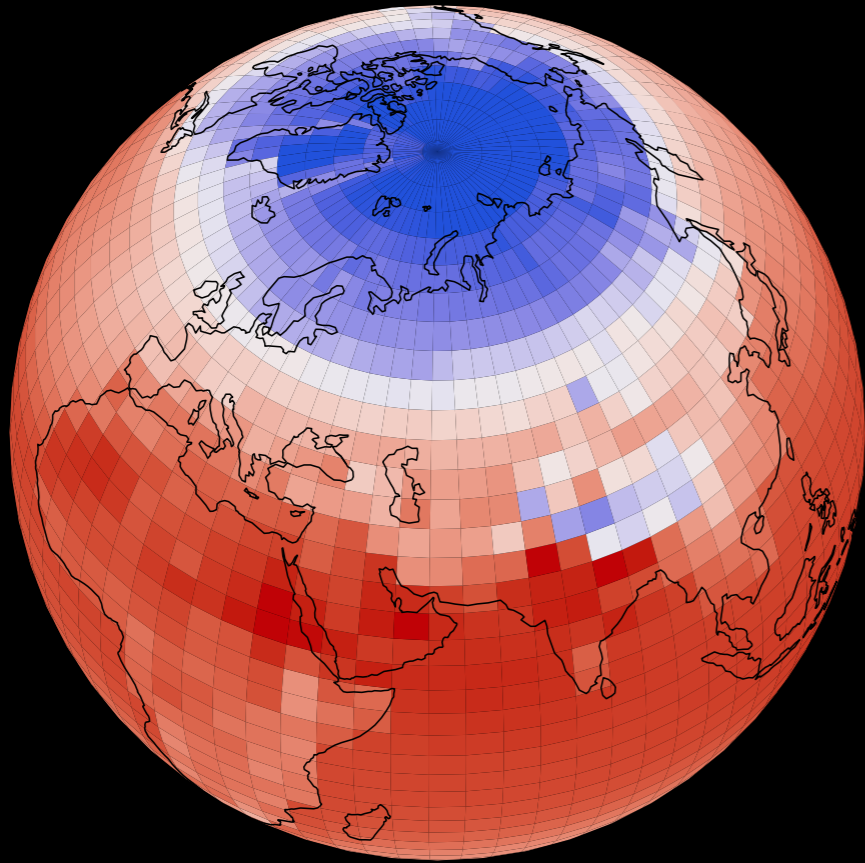
Kopparapu et. al. (2013)

# “Climate” Habitability

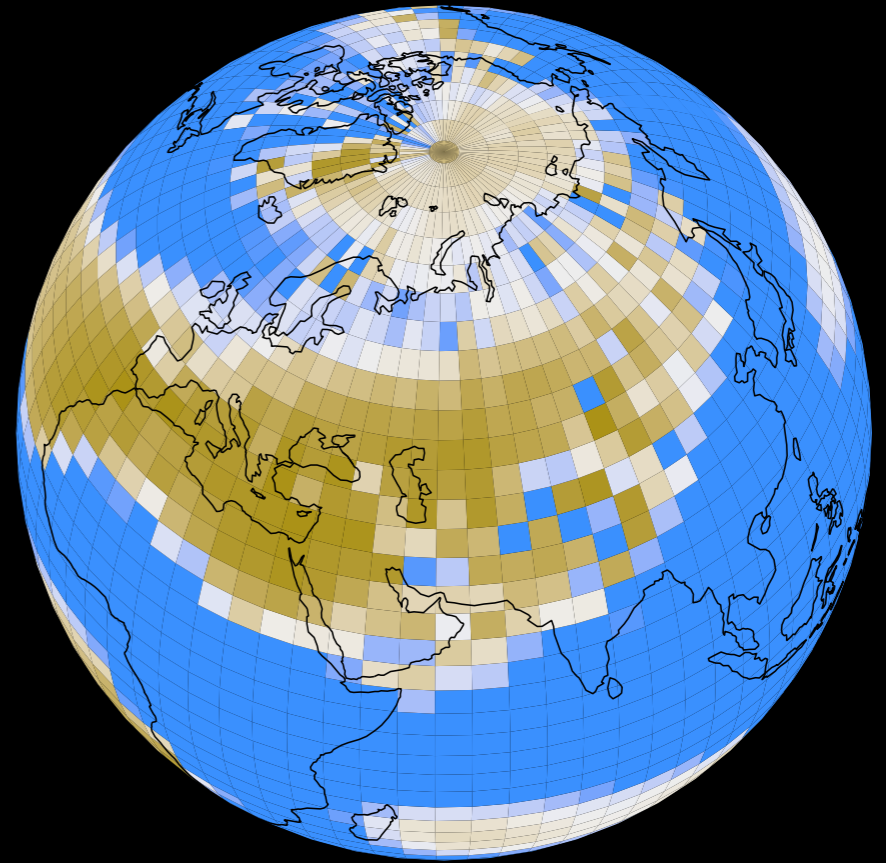


$$0 \leq T_{\text{surf}} \leq 100^\circ \text{C}$$

# “Climate” Habitability

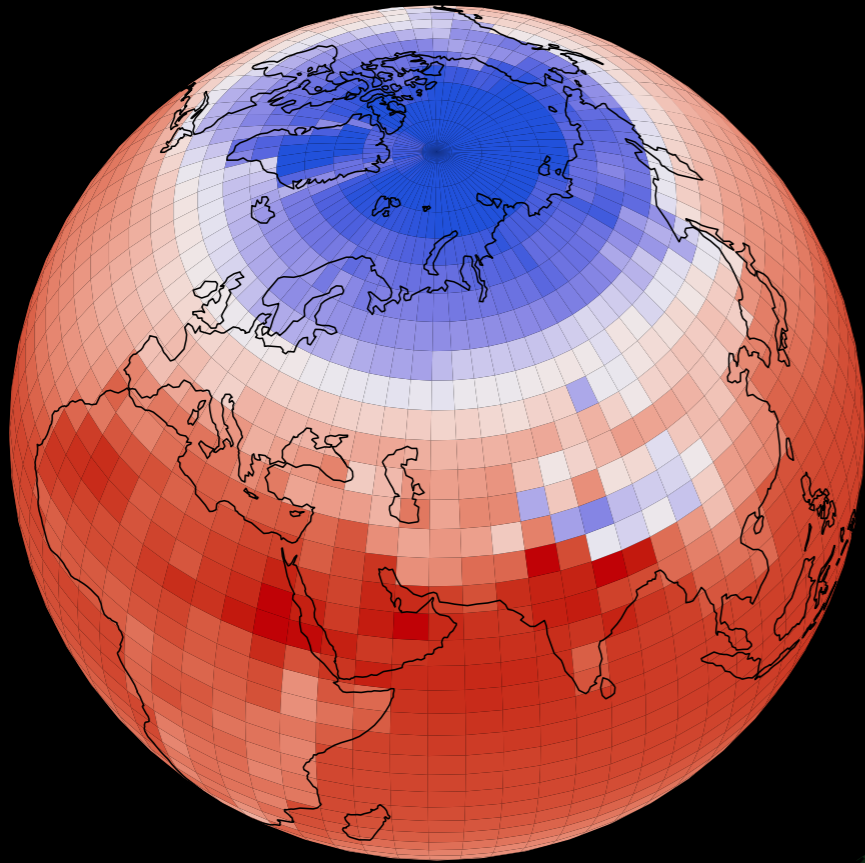


$$0 \leq T_{\text{surf}} \leq 100^\circ \text{C}$$

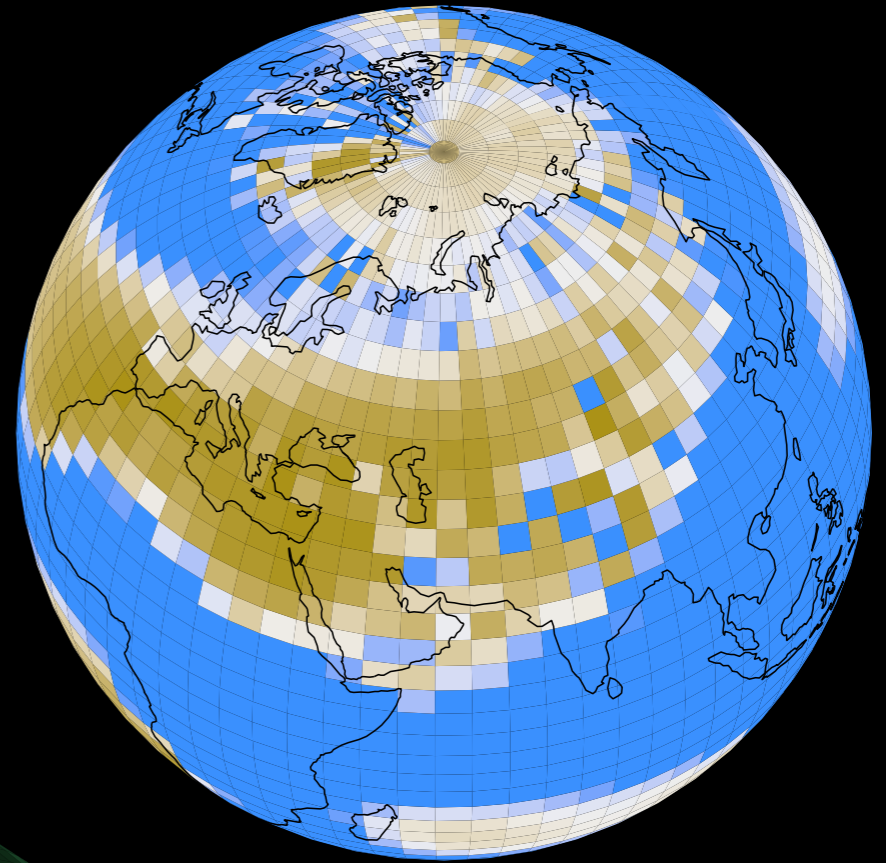


$$\text{Precipitation} \geq 300 \text{ mm/year}$$

# “Climate” Habitability



$$0 \leq T_{\text{surf}} \leq 100^\circ \text{C}$$



$$\text{Precipitation} \geq 300 \text{ mm/year}$$







$$f_X(P_{\text{rot}}, \psi, e, \phi_{\text{peri}}) \equiv \frac{1}{A_{\text{terr}}} \sum_{i=1}^{n_\lambda} \sum_{j=1}^{n_\phi} \frac{1}{n_{\text{orb}} P_{\text{orb}}} \sum_{k=1}^{12n_{\text{orb}}} I_X(\lambda_i, \phi_j, t_k; P_{\text{rot}}, \psi, e, \phi_{\text{peri}}) f_{\text{terr}} A_{ij} \tau_k(e)$$



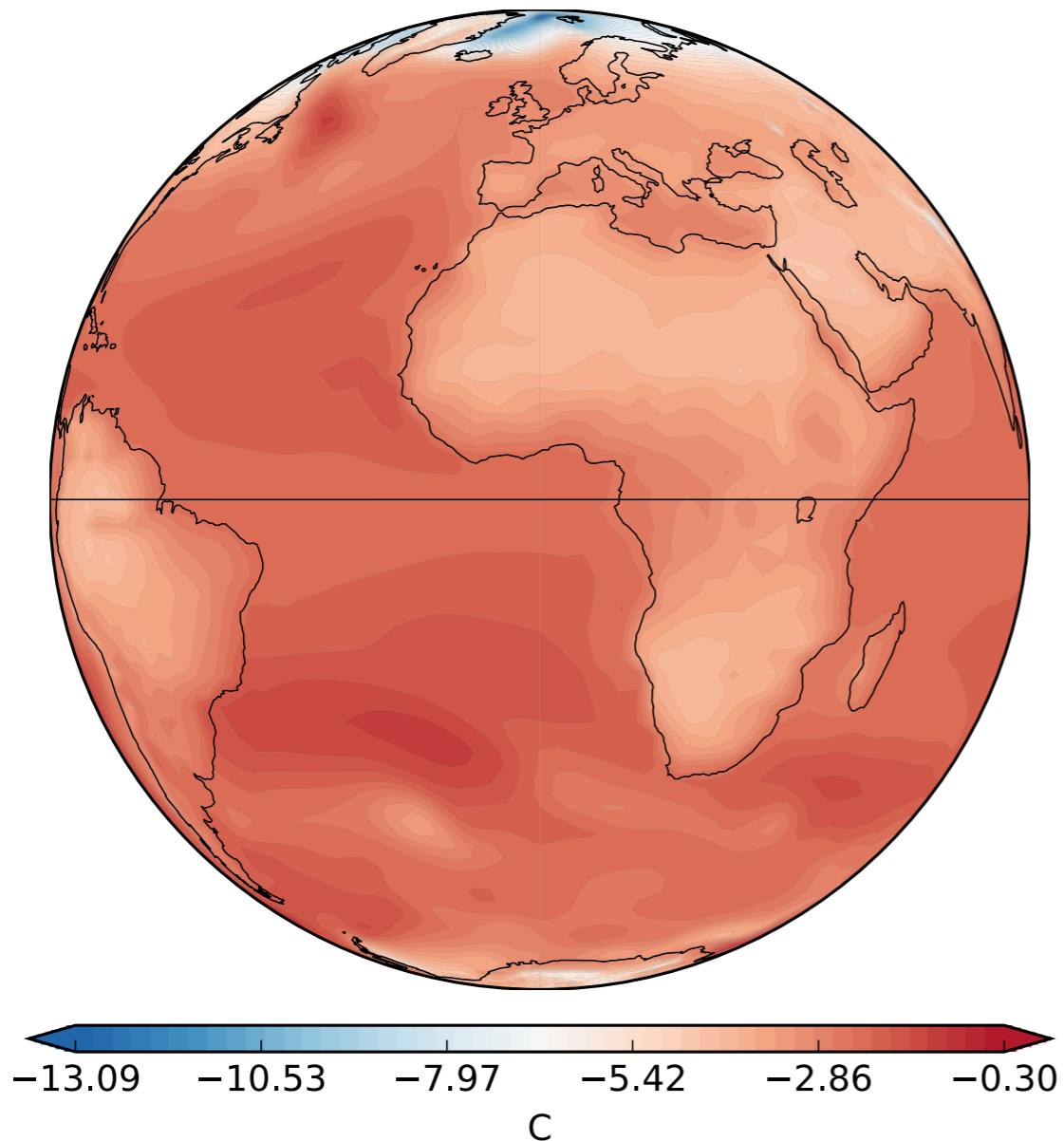
$$f_X(P_{\text{rot}}, \psi, e, \phi_{\text{peri}}) \equiv \frac{1}{A_{\text{terr}}} \sum_{i=1}^{n_\lambda} \sum_{j=1}^{n_\phi} \frac{1}{n_{\text{orb}} P_{\text{orb}}} \sum_{k=1}^{12n_{\text{orb}}} I_X(\lambda_i, \phi_j, t_k; P_{\text{rot}}, \psi, e, \phi_{\text{peri}}) f_{\text{terr}} A_{ij} \tau_k(e)$$

- Each cell gets 0 or 1 per month (**temperate** and **wet**)
- Weight by surface area in land, then take land average
- Weight by month length, then take time average

# ROCKE-3D

Way et. al. (2017)

ANN4751-4800.ajjE200F40oQ40 - ANN2451-2470.ajjE200\_2xCO2aF40oQ40  
SURFACE AIR TEMPERATURE



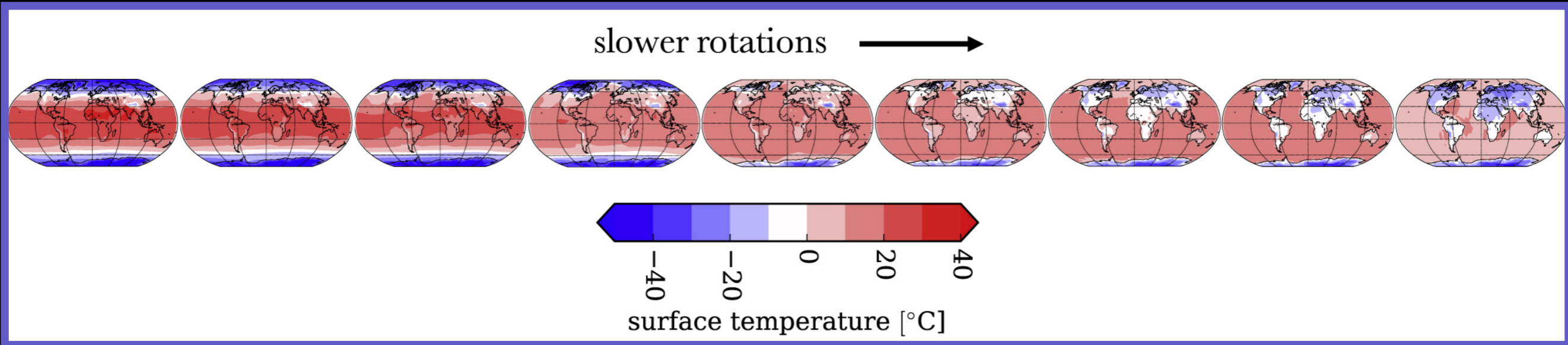
Min: -13.09 Max:-0.3 Means: NH -3.45, SH -2.28, Global -2.86

- $4^\circ \times 5^\circ$  latitude-longitude resolution
- 40 vertical layers ( $10^{-4}$  to 1 bar)
- Dynamic ocean (uniform 1360 m depth)
- Bare soil, ocean, ice (no vegetation)



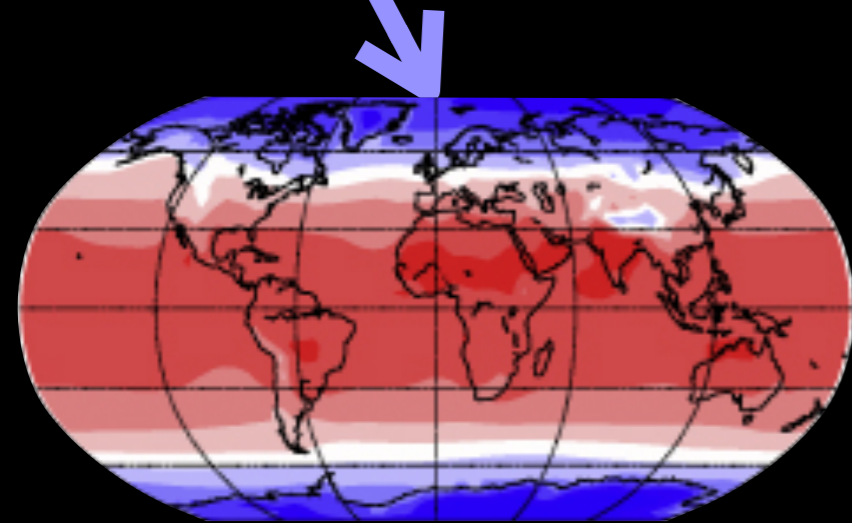
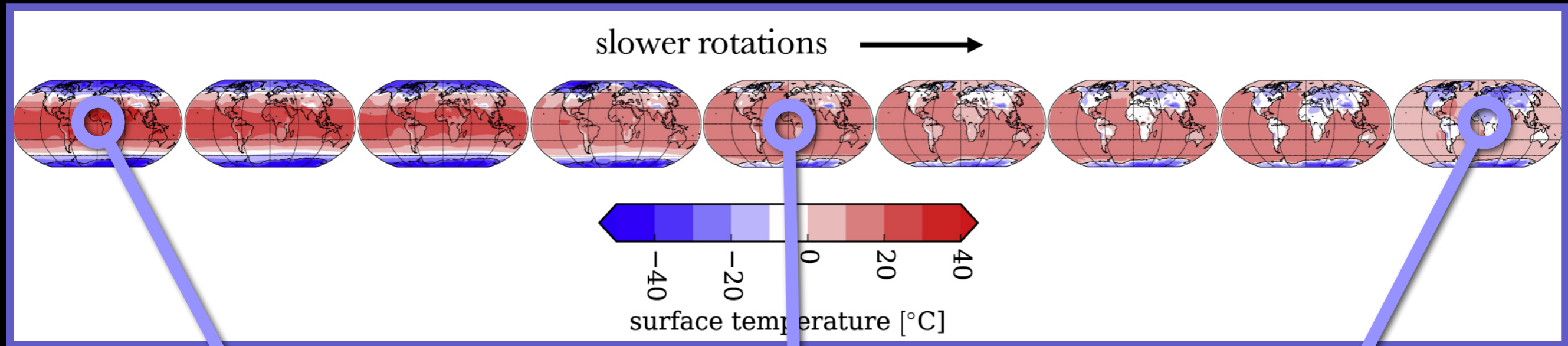


# Jansen et. al. (2019): Rotational “Goldilocks” Zone

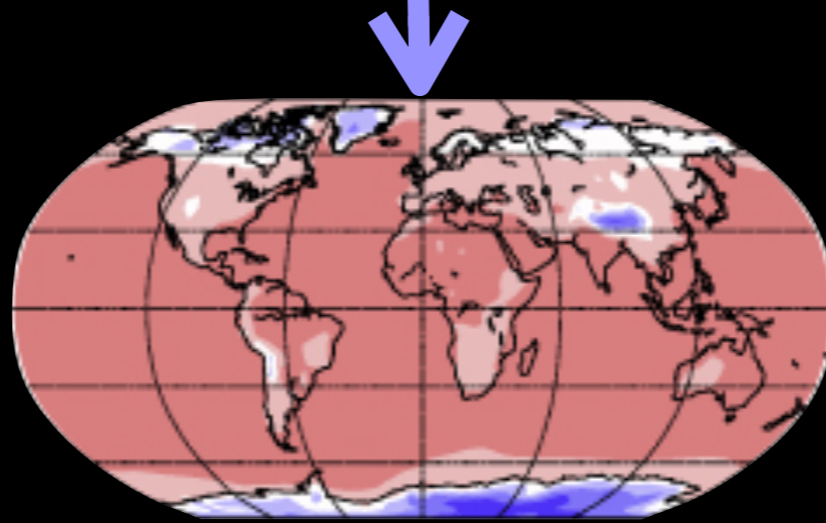




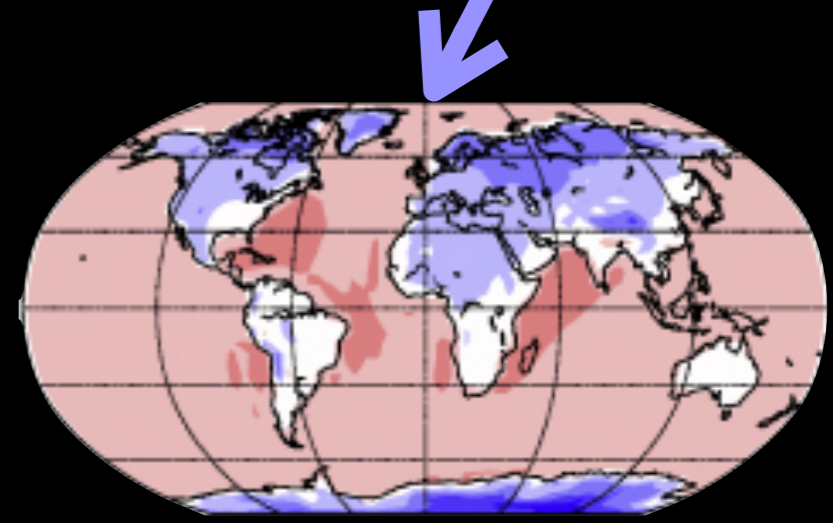
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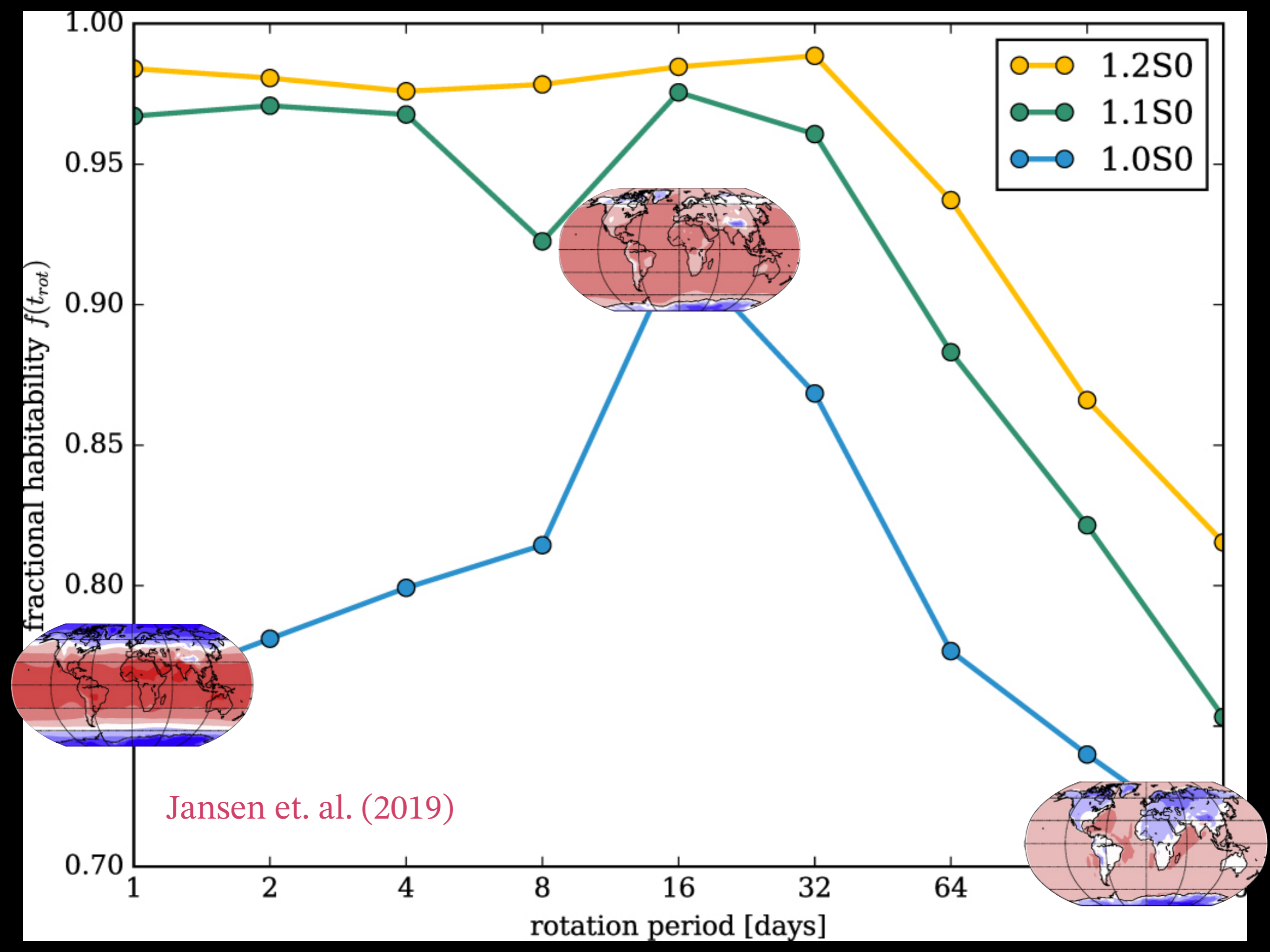
1 day



16 days



256 days



He et. al. (2022):  
**Obliquity Matters**  
at **Fast Rotations**

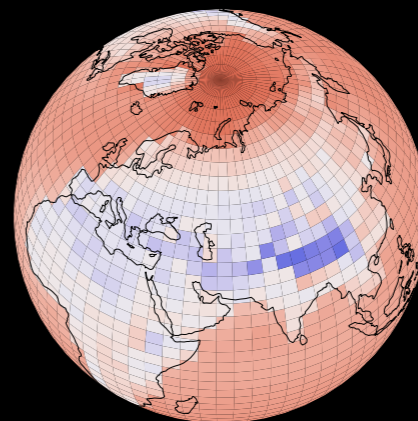
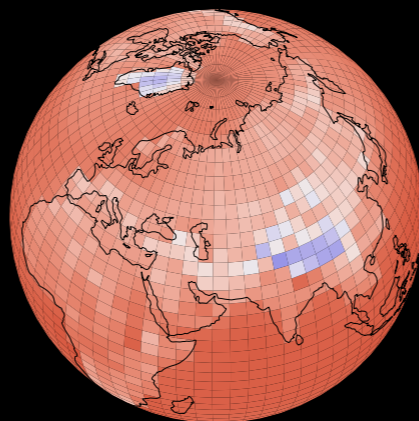
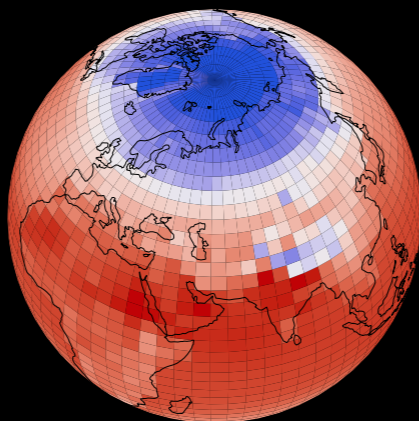


0°

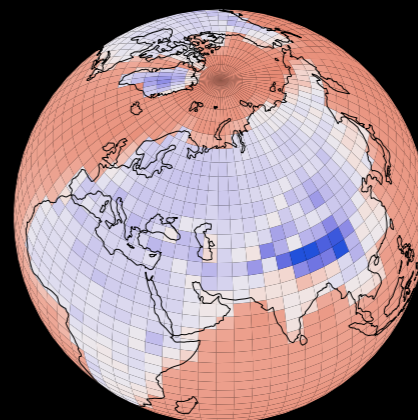
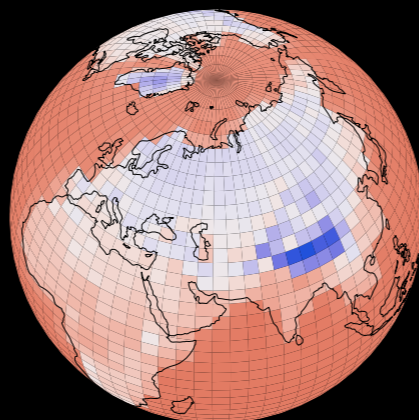
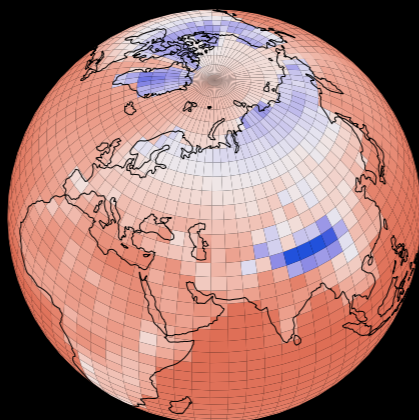
45°

90°

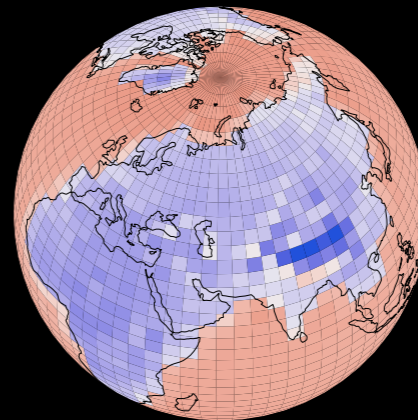
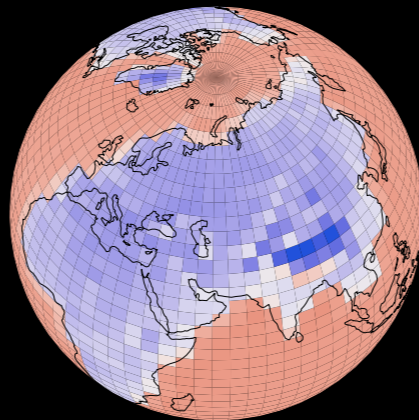
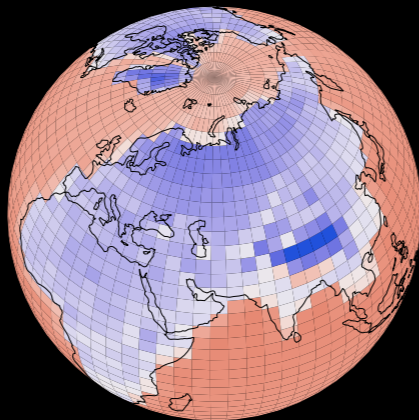
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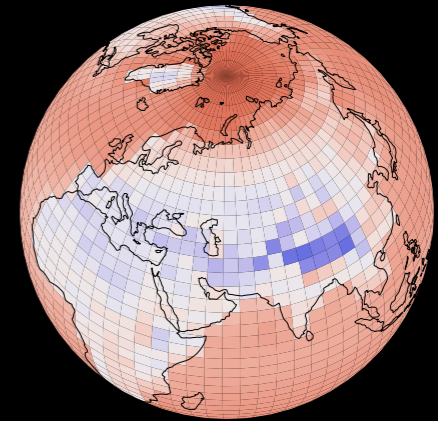
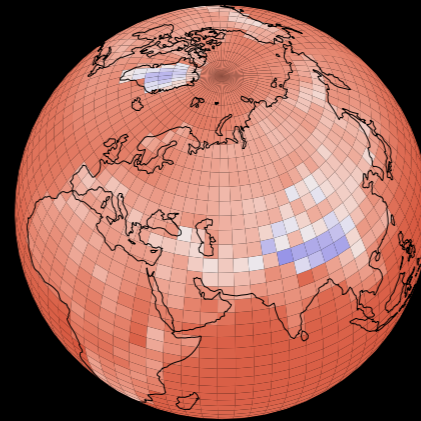
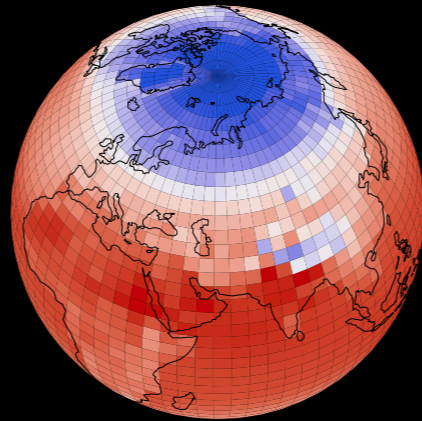


0°

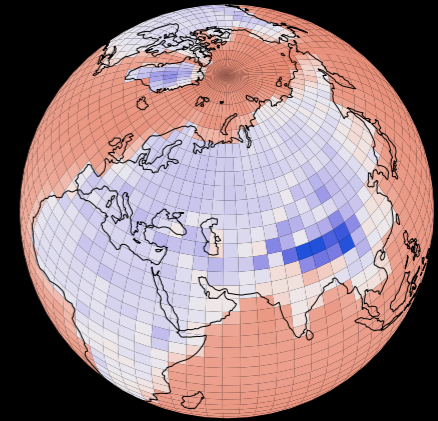
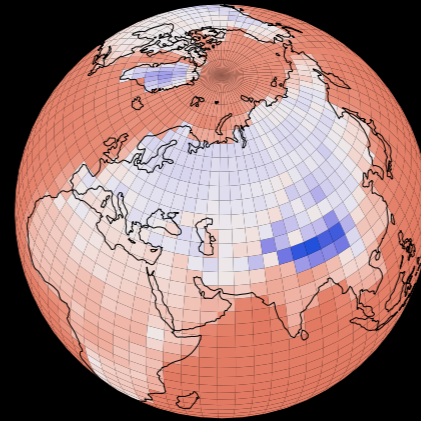
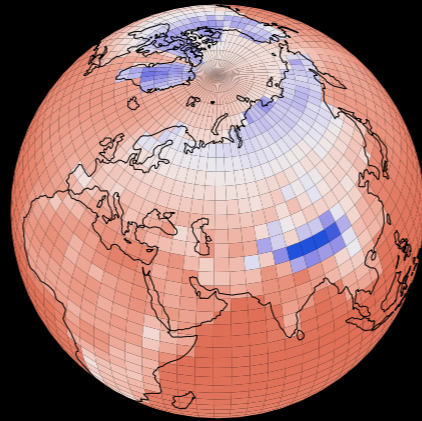
45°

90°

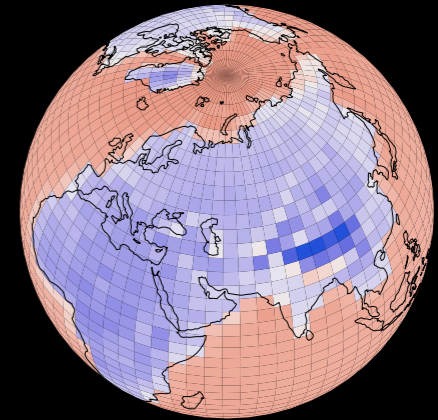
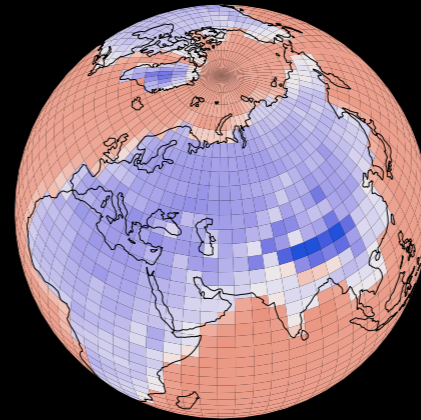
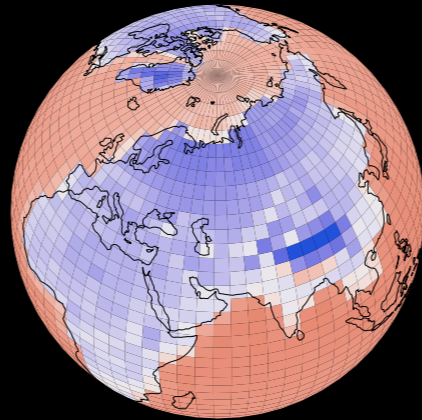
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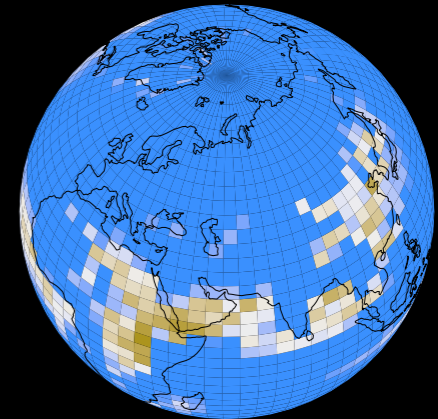
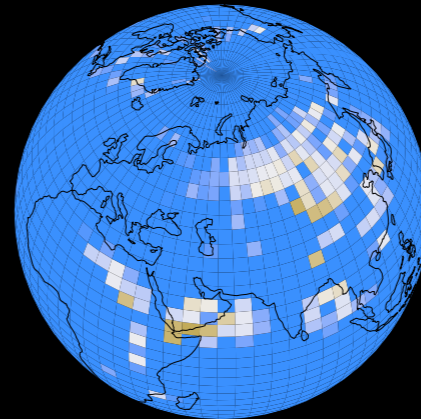
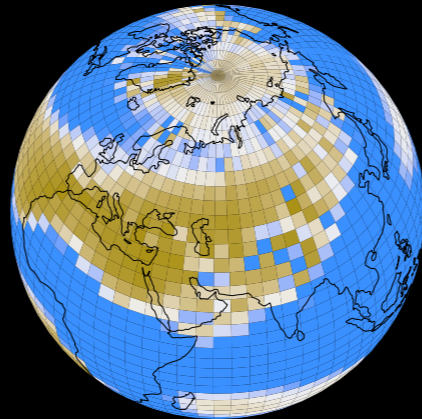


0°

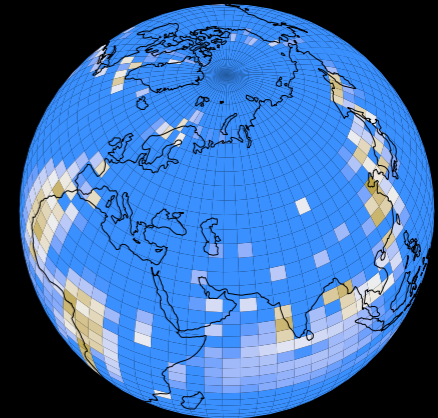
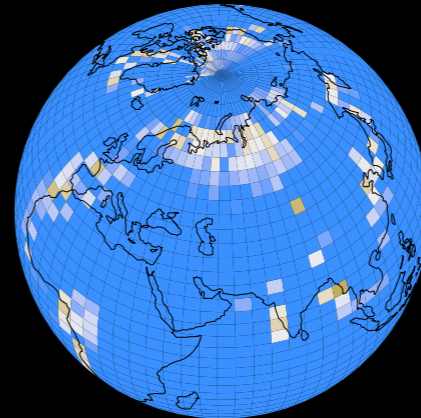
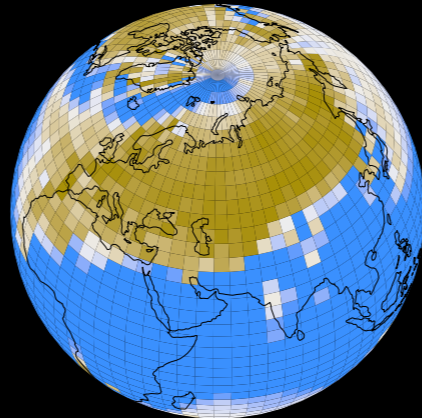
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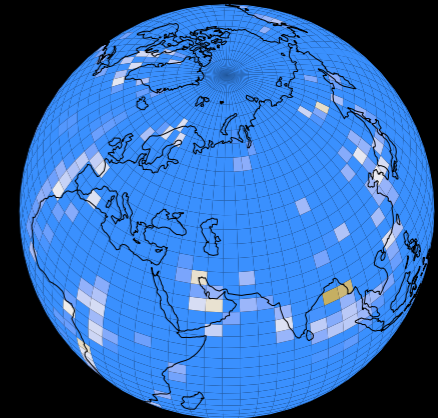
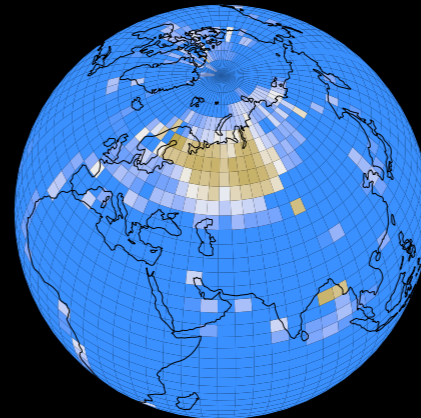
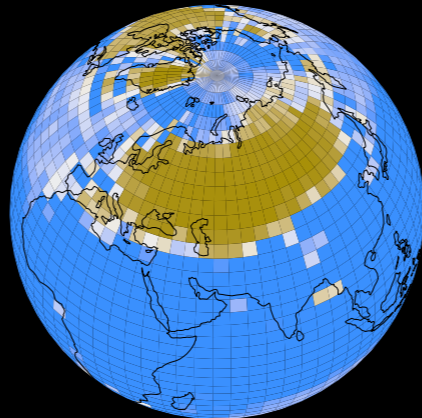
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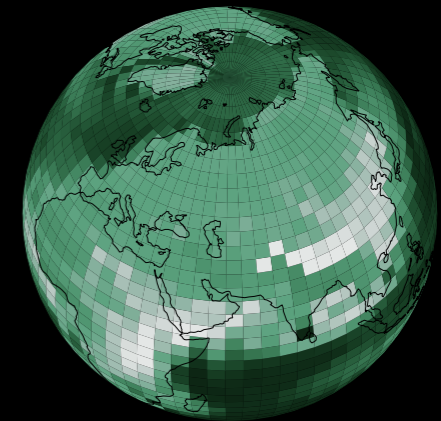
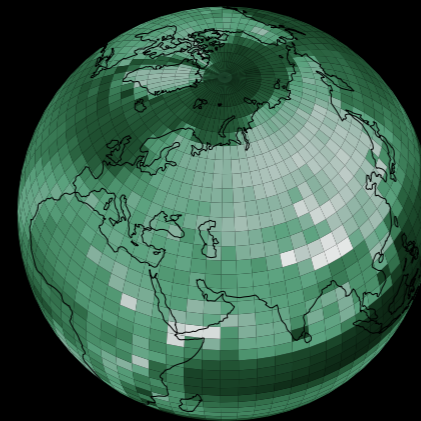
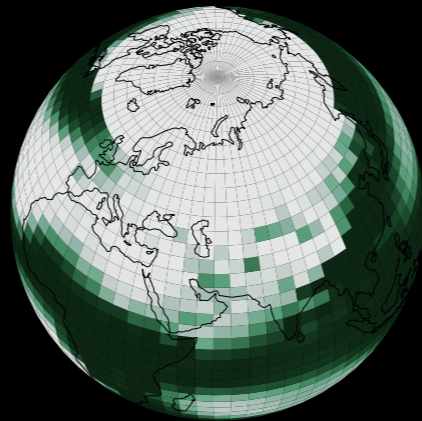


0°

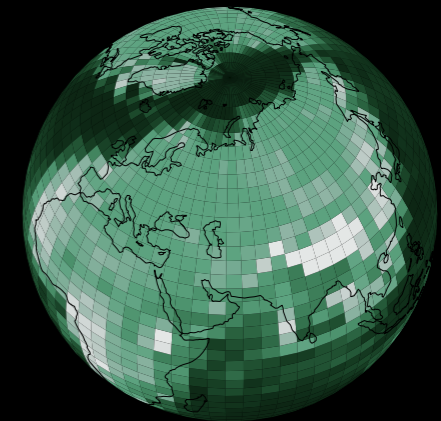
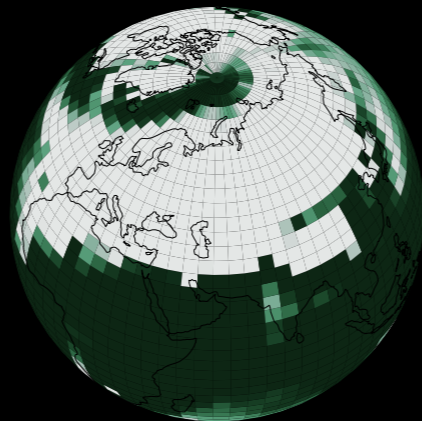
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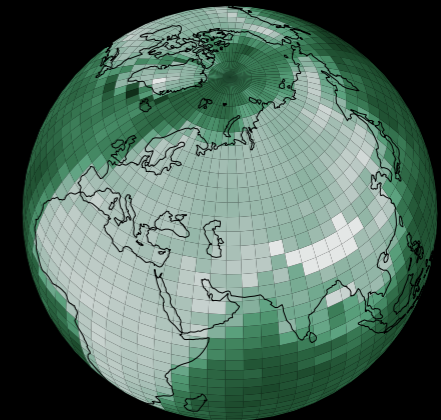
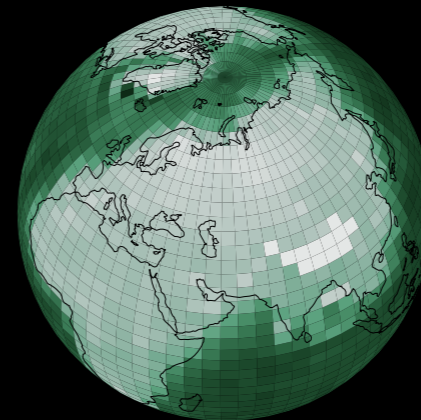
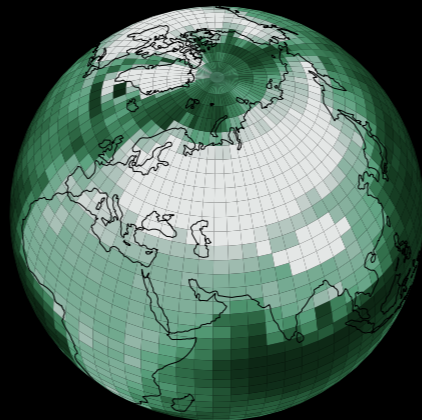
1 day

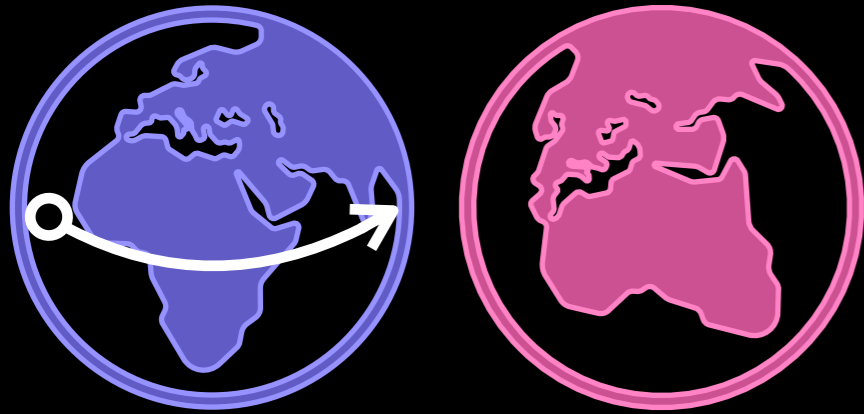


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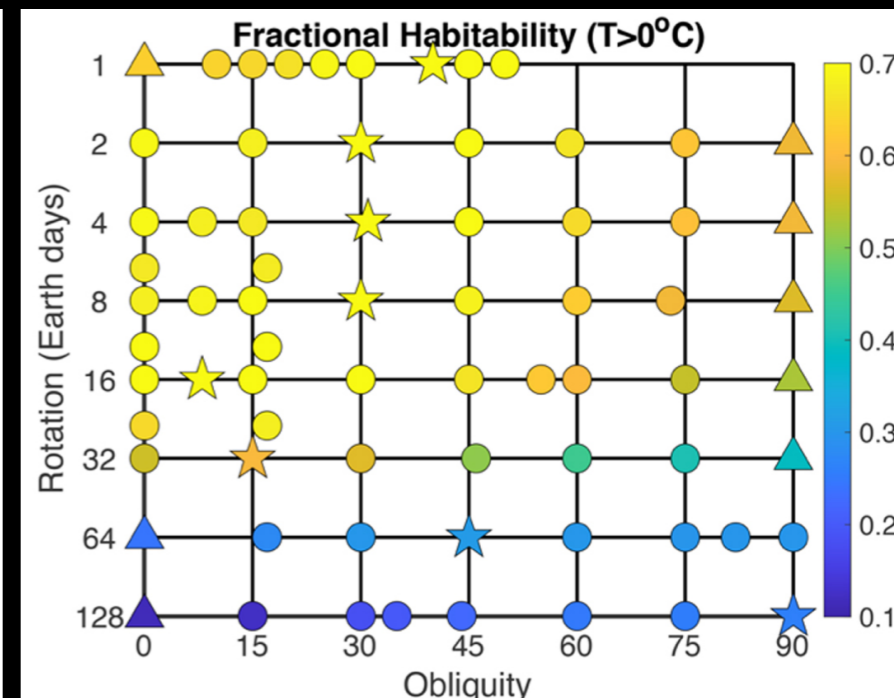
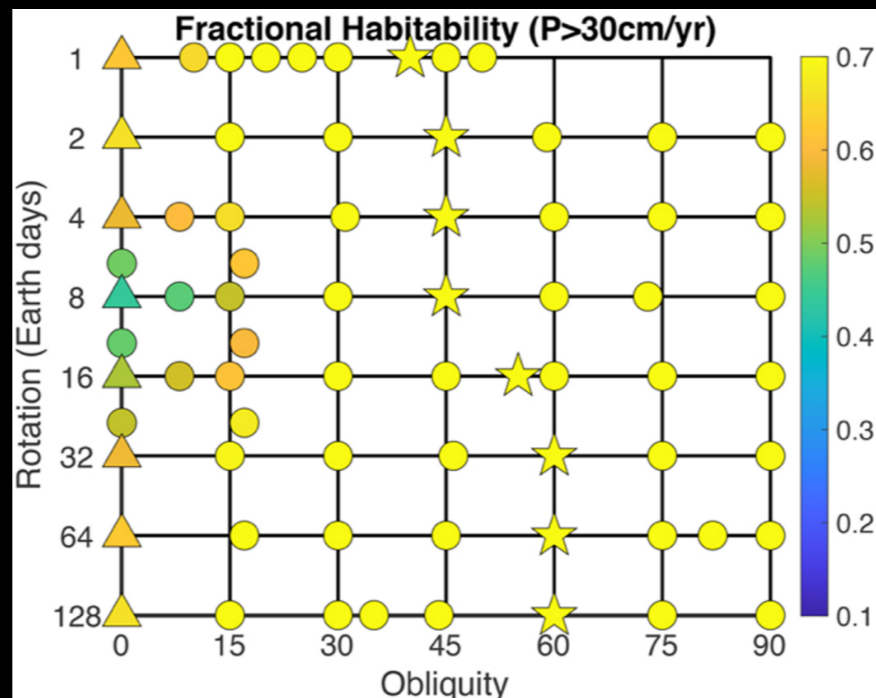
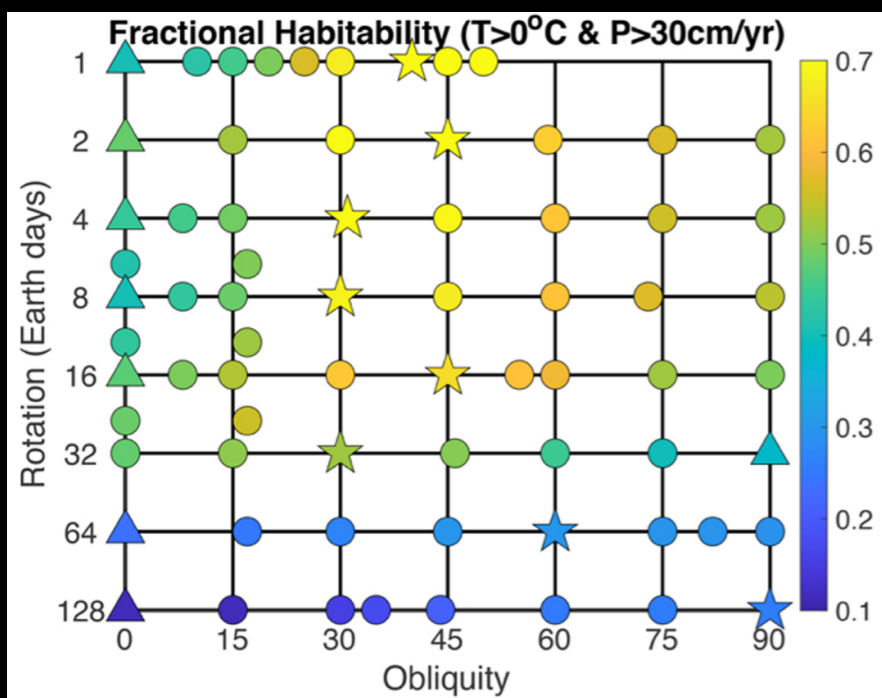


# He et. al. (2022): Obliquity Matters at Fast Rotations

$0 \leq T_{\text{surf}} \leq 100^\circ \text{C}$

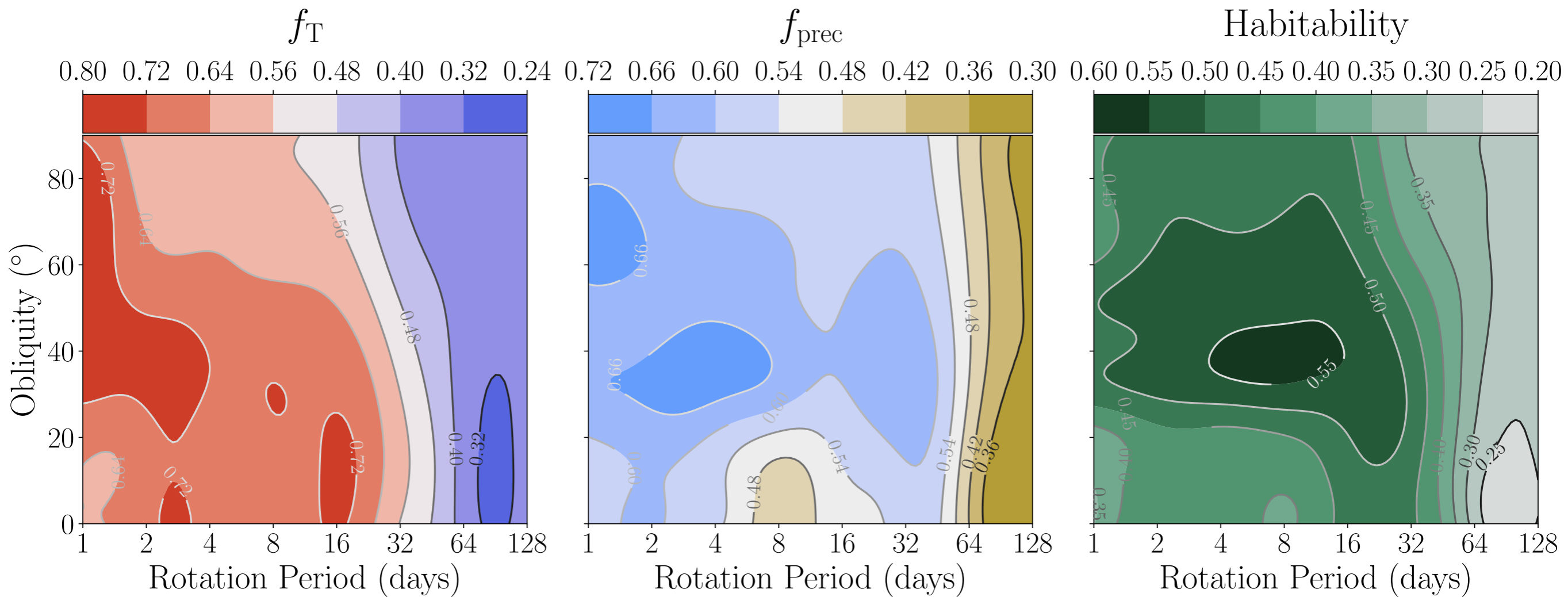
Precipitation  $\geq 300$  mm/year

Both





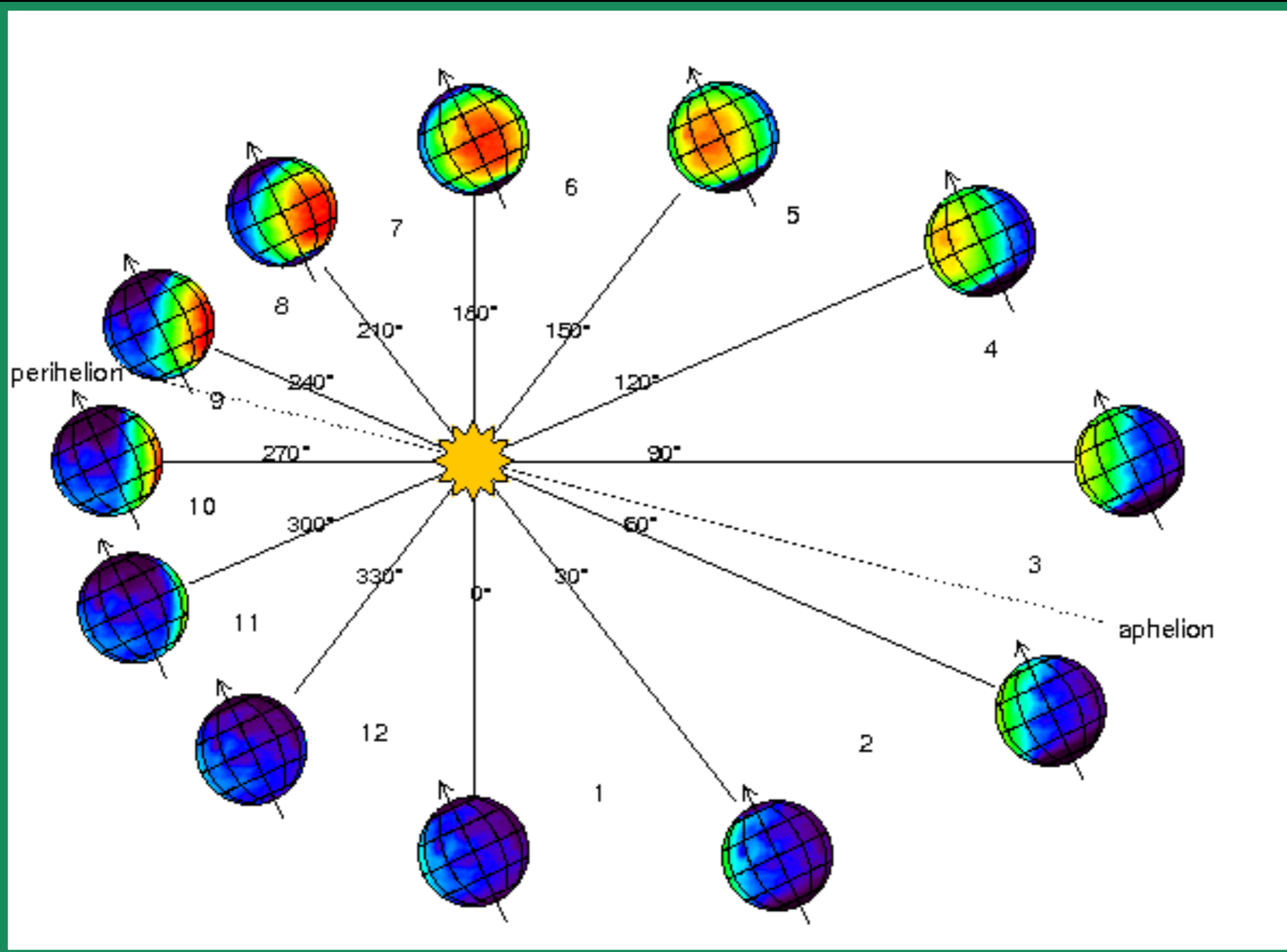
# He et. al. (2022): Obliquity Matters at Fast Rotations





# Adding Eccentricity

[https://www-mars.lmd.jussieu.fr/mars/time/solar\\_longitude.html](https://www-mars.lmd.jussieu.fr/mars/time/solar_longitude.html)

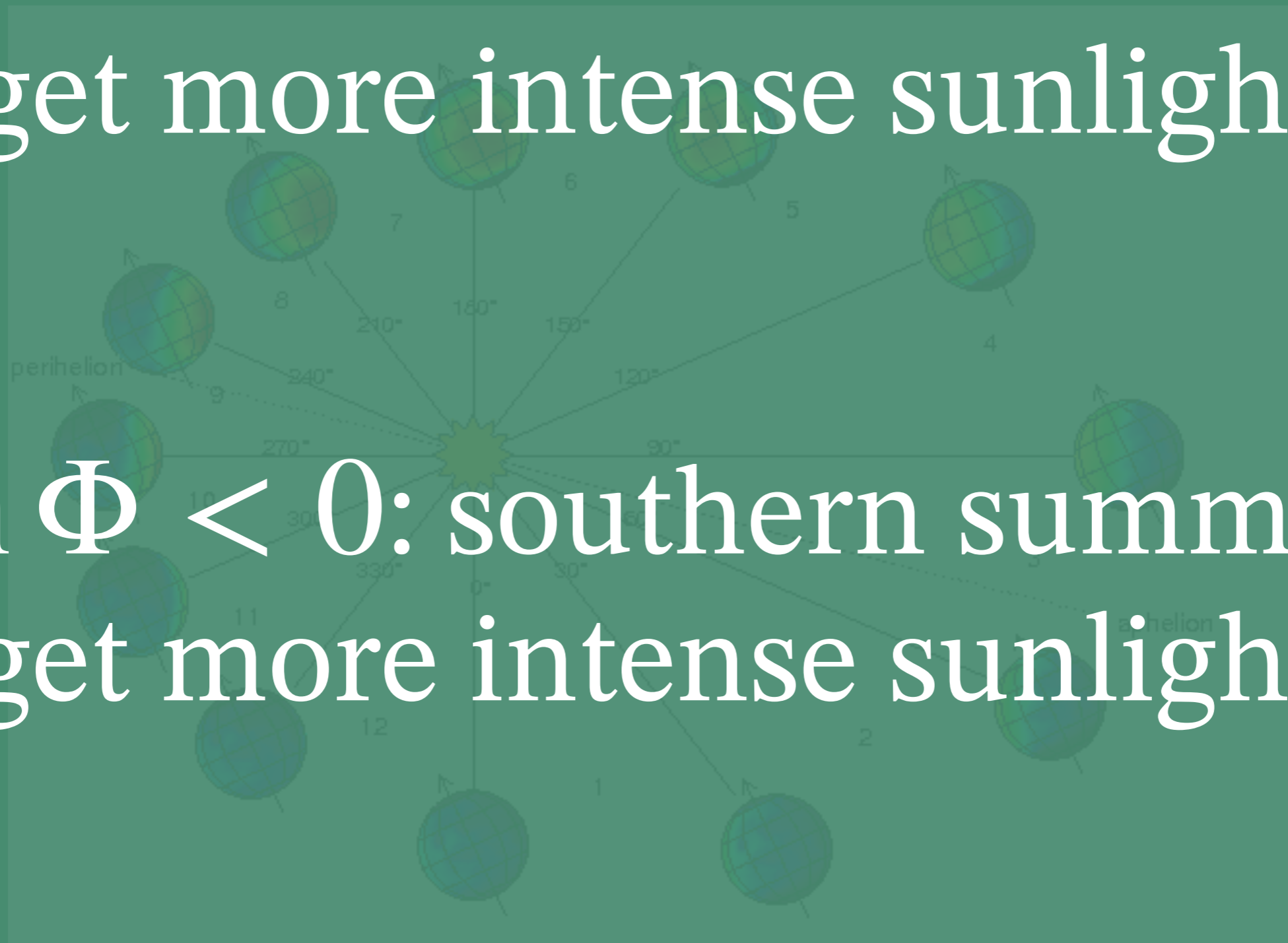


Adding

Eccentricity

$\sin \Phi > 0$ : northern summers  
get more intense sunlight

$\sin \Phi < 0$ : southern summers  
get more intense sunlight



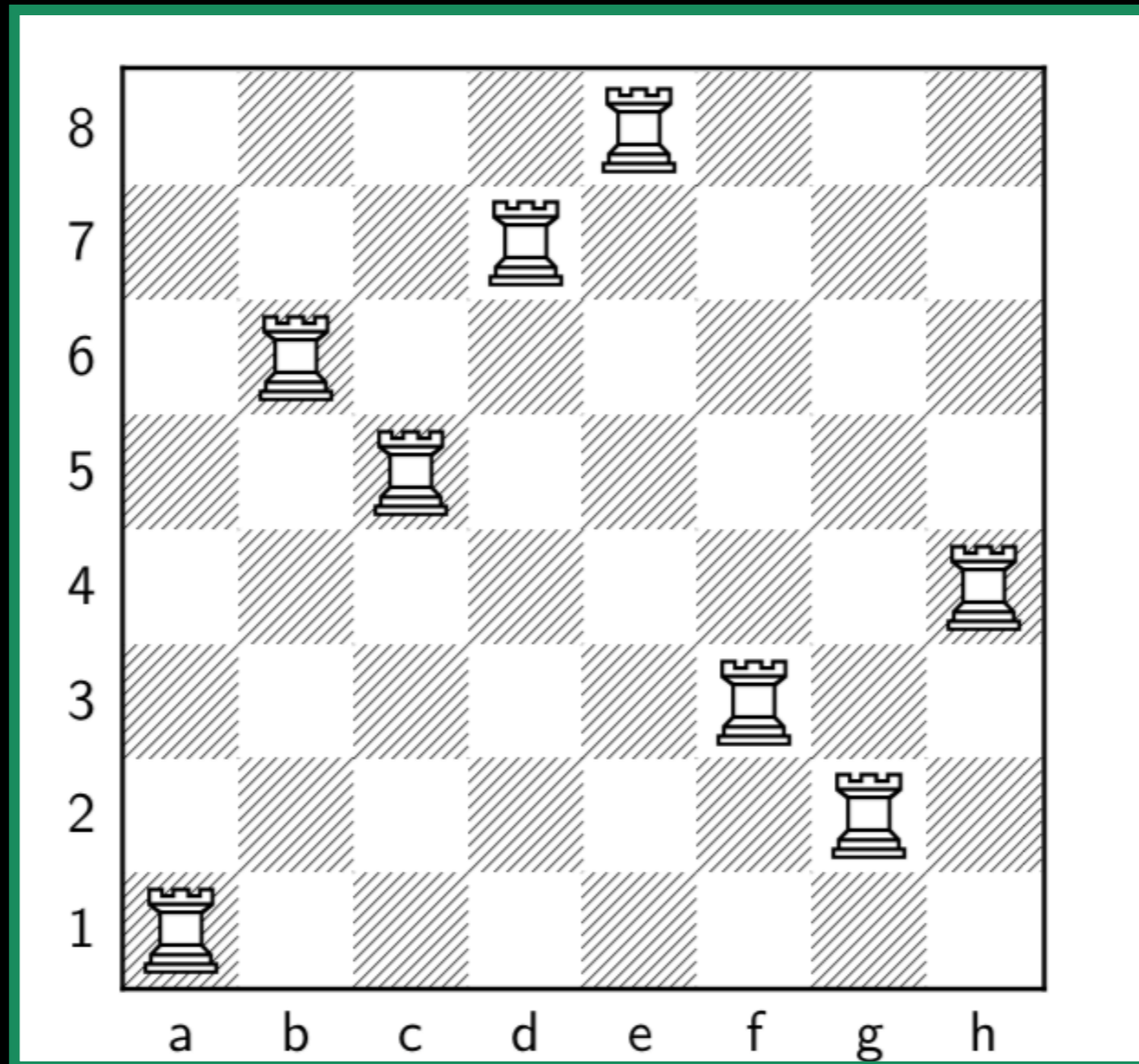




How do we probe a 4-D  
parameter space when  
computation is limited?



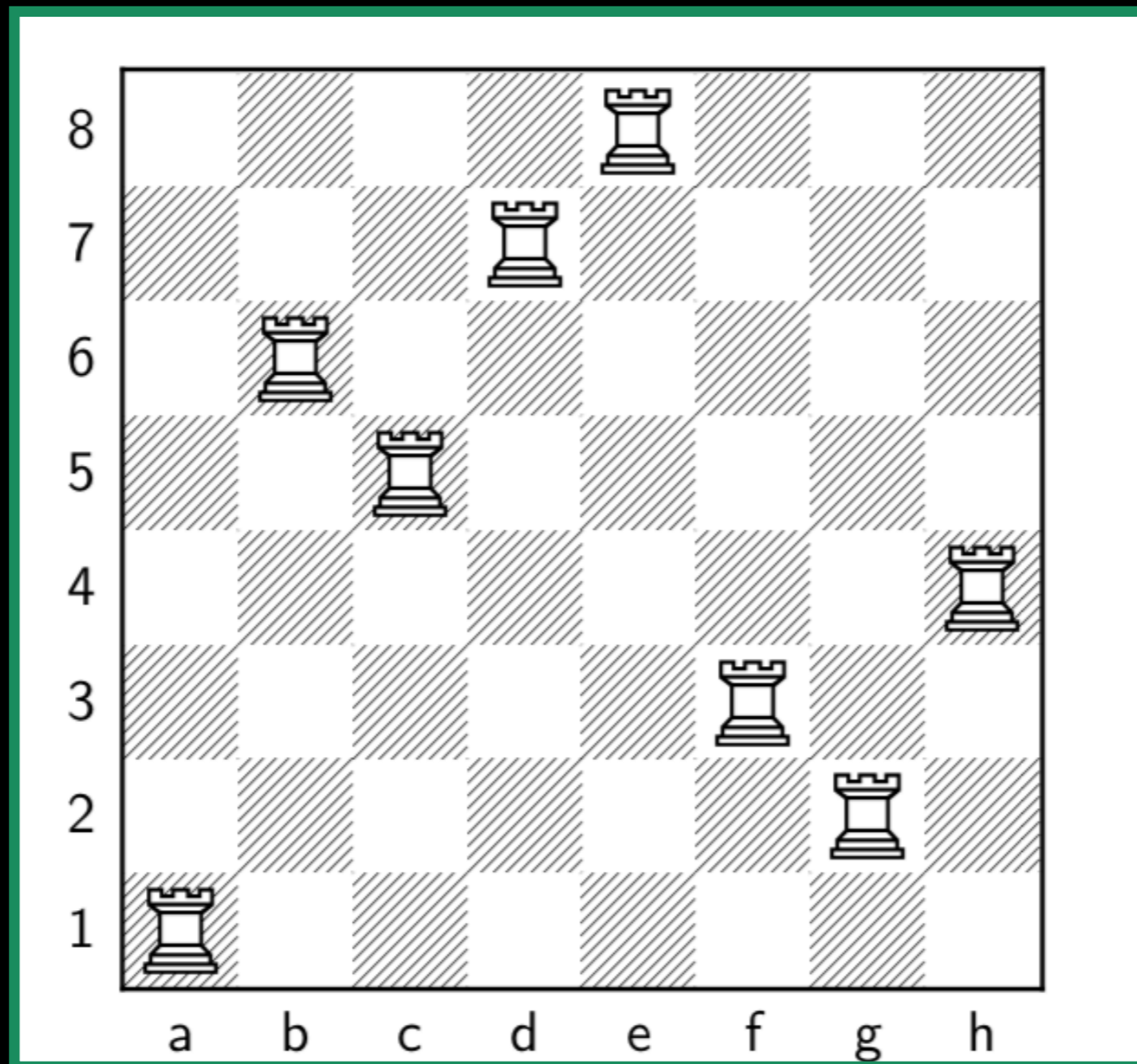
# Latin Hypercubes!





# Latin Hypercubes!

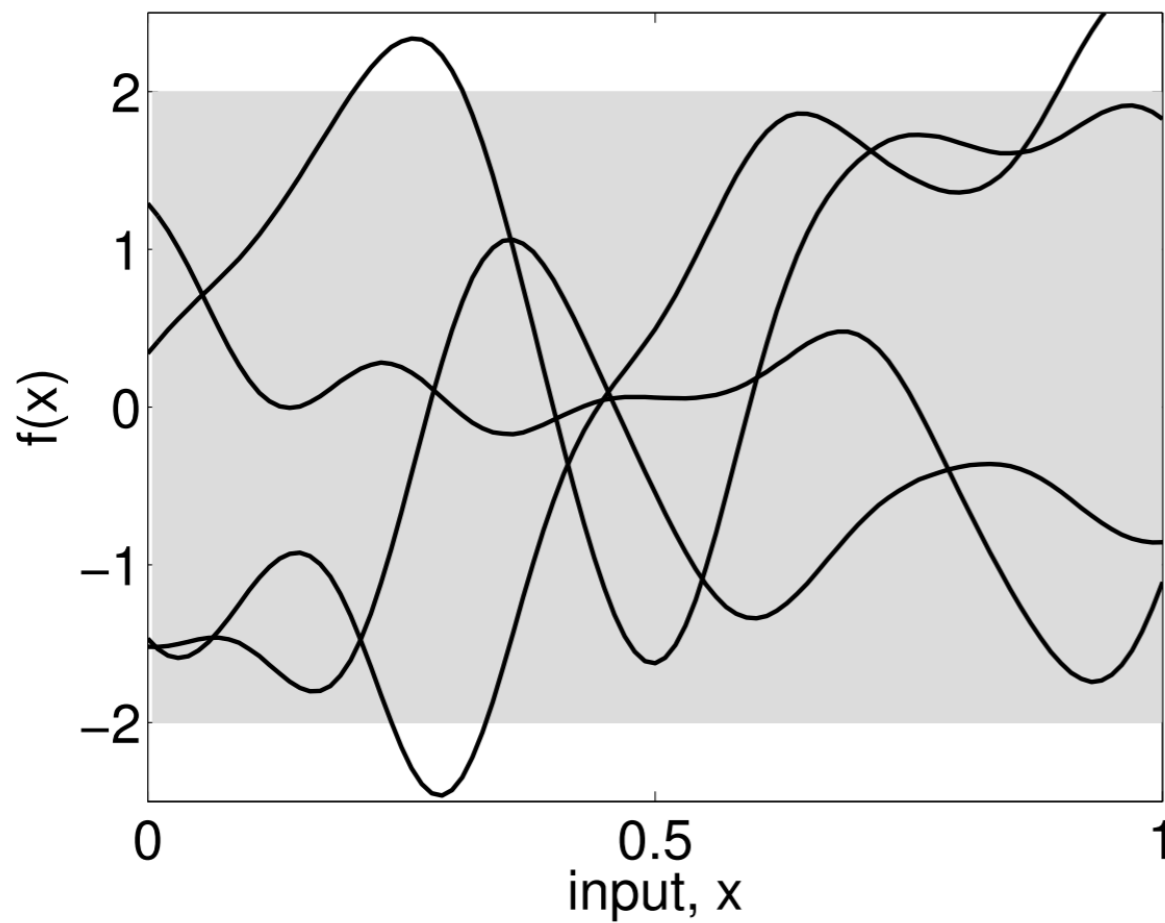
*Obliquity*



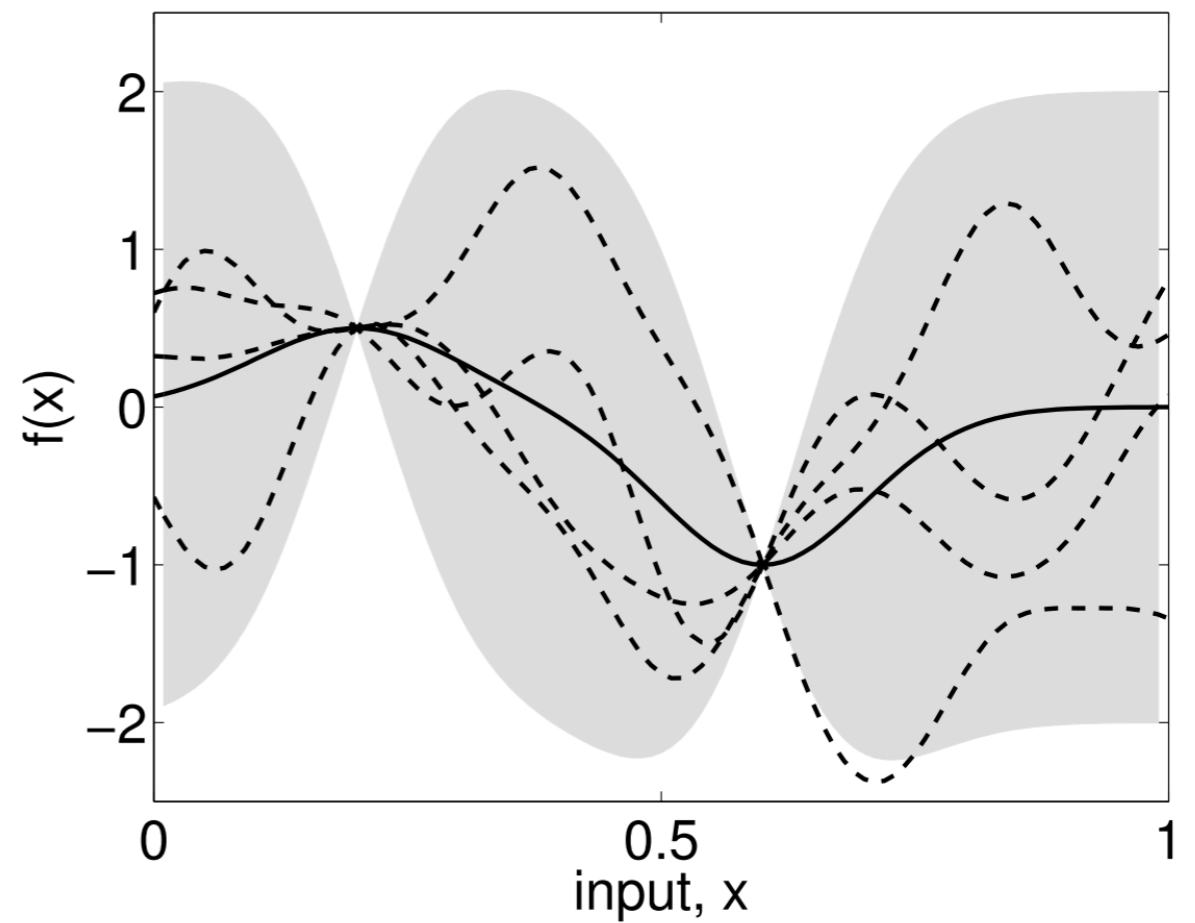
*Rotation Period*



# Emulating Habitability



(a), prior

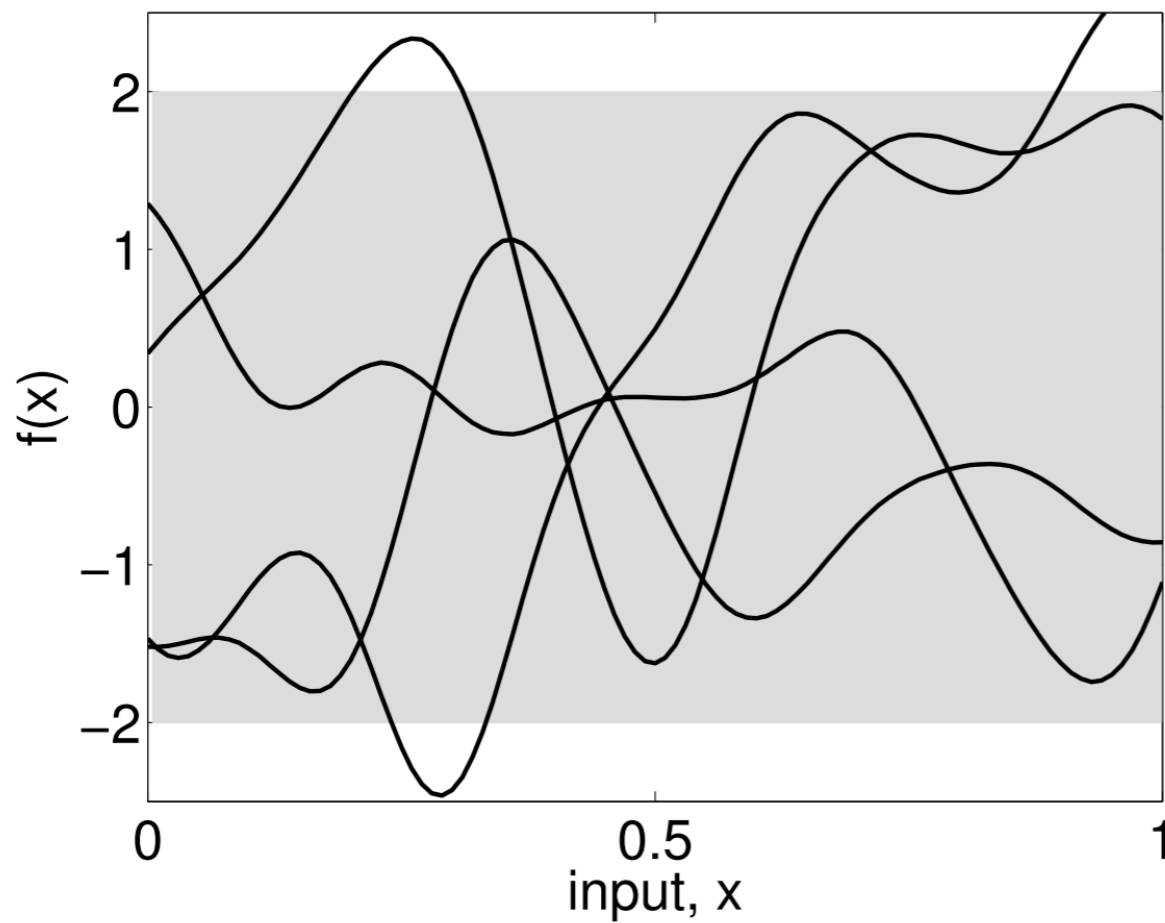


(b), posterior

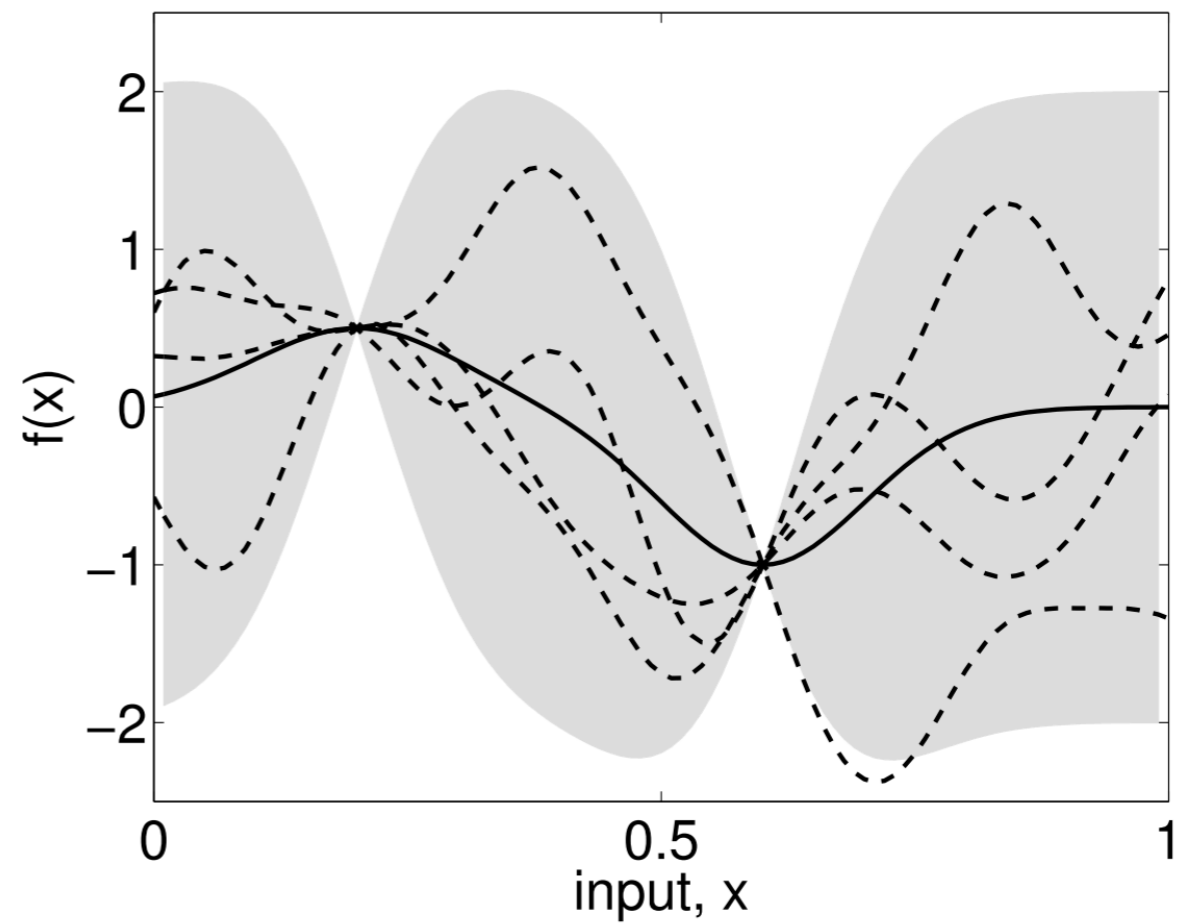


# Emulating Habitability

Non-parametric?



(a), prior

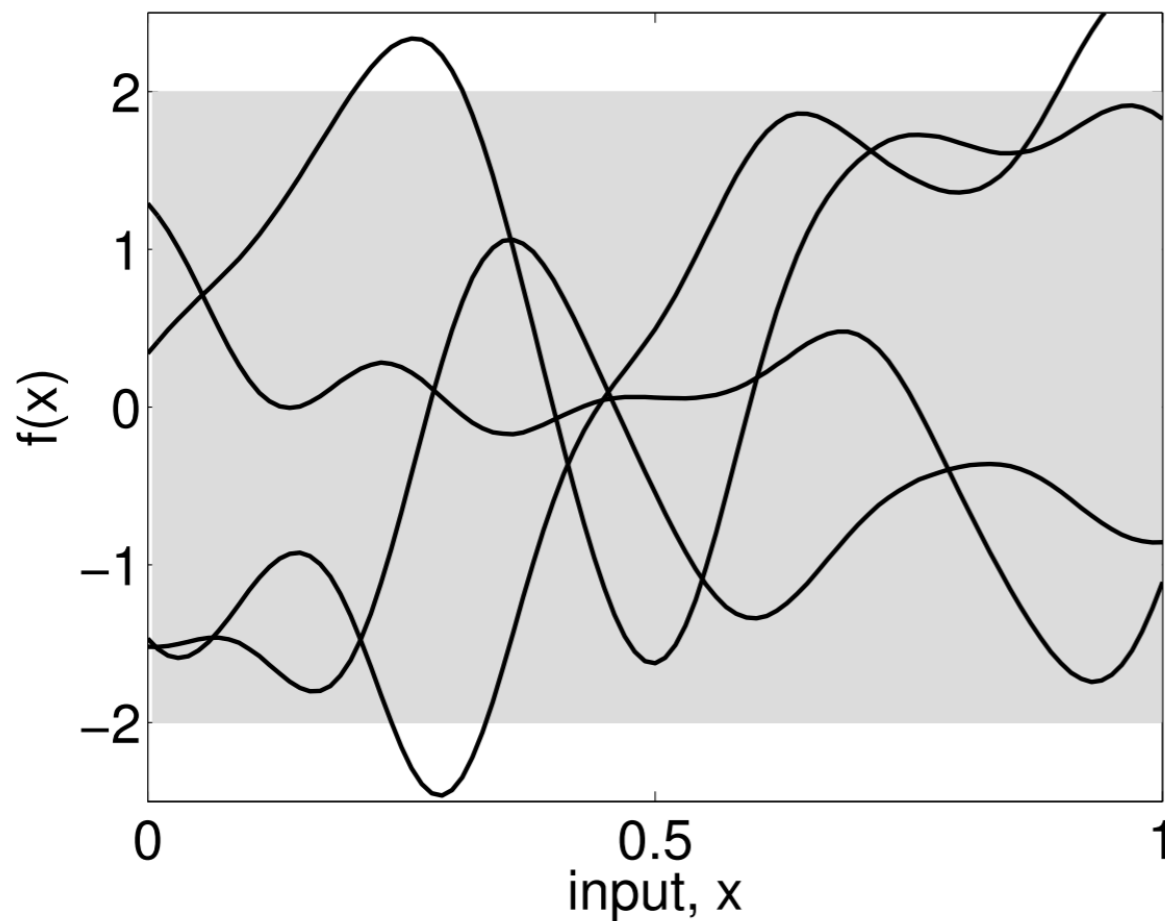


(b), posterior

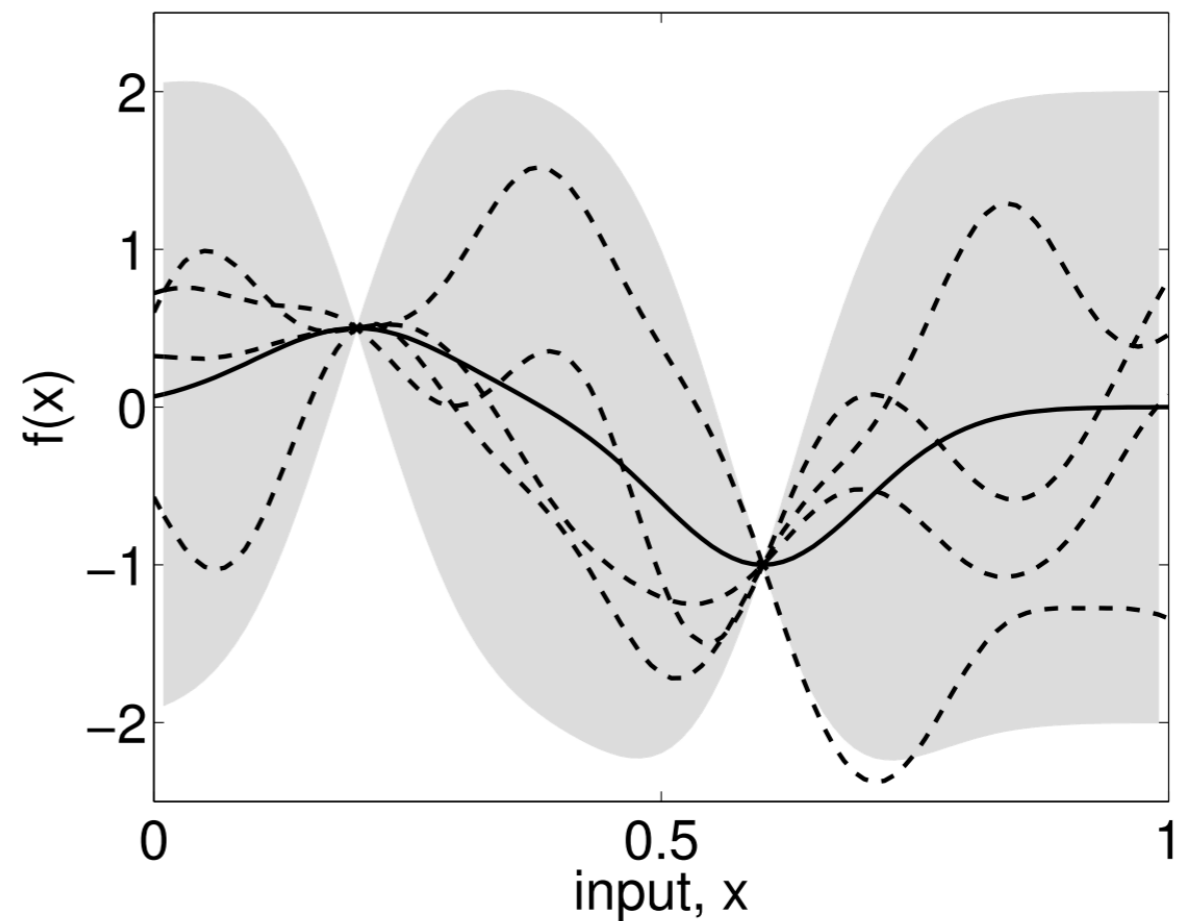


# Emulating Habitability

Non-parametric? Bayesian?



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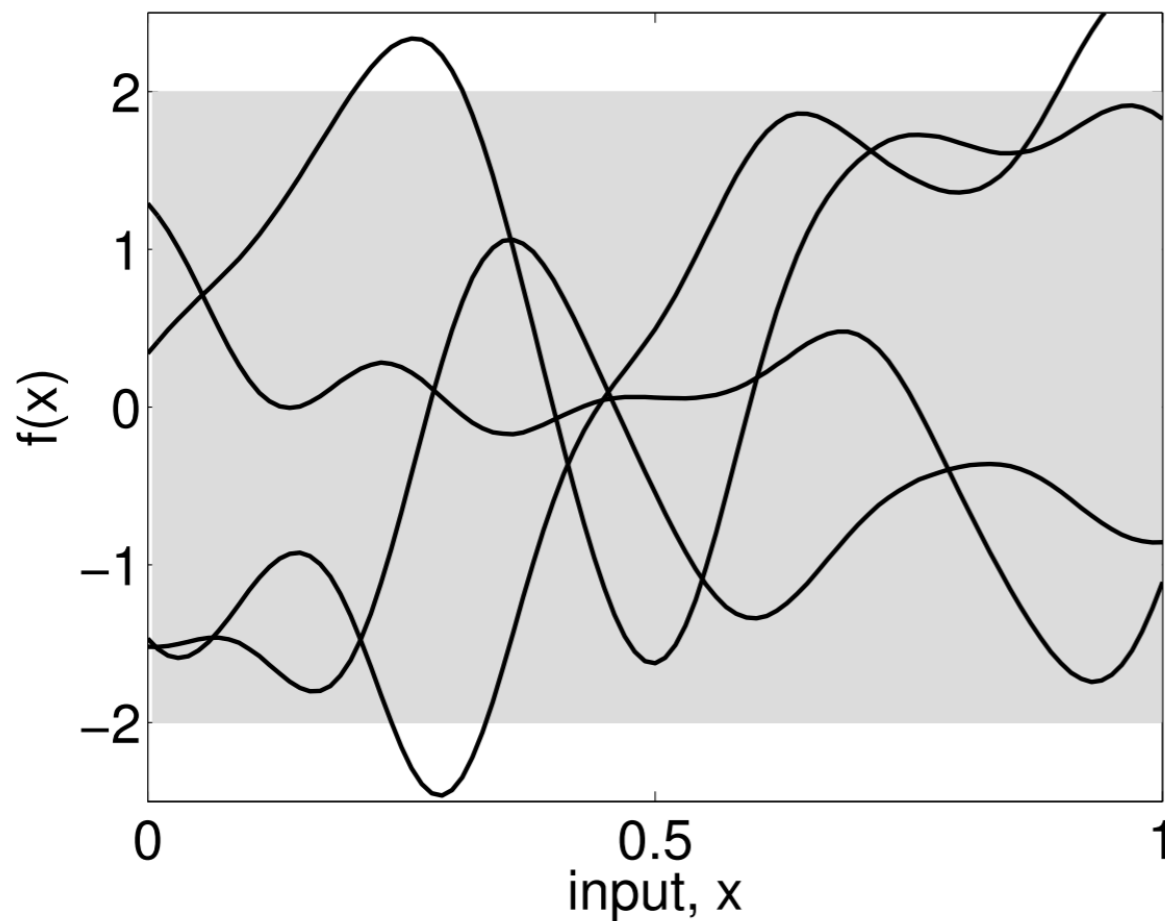


(b), posterior

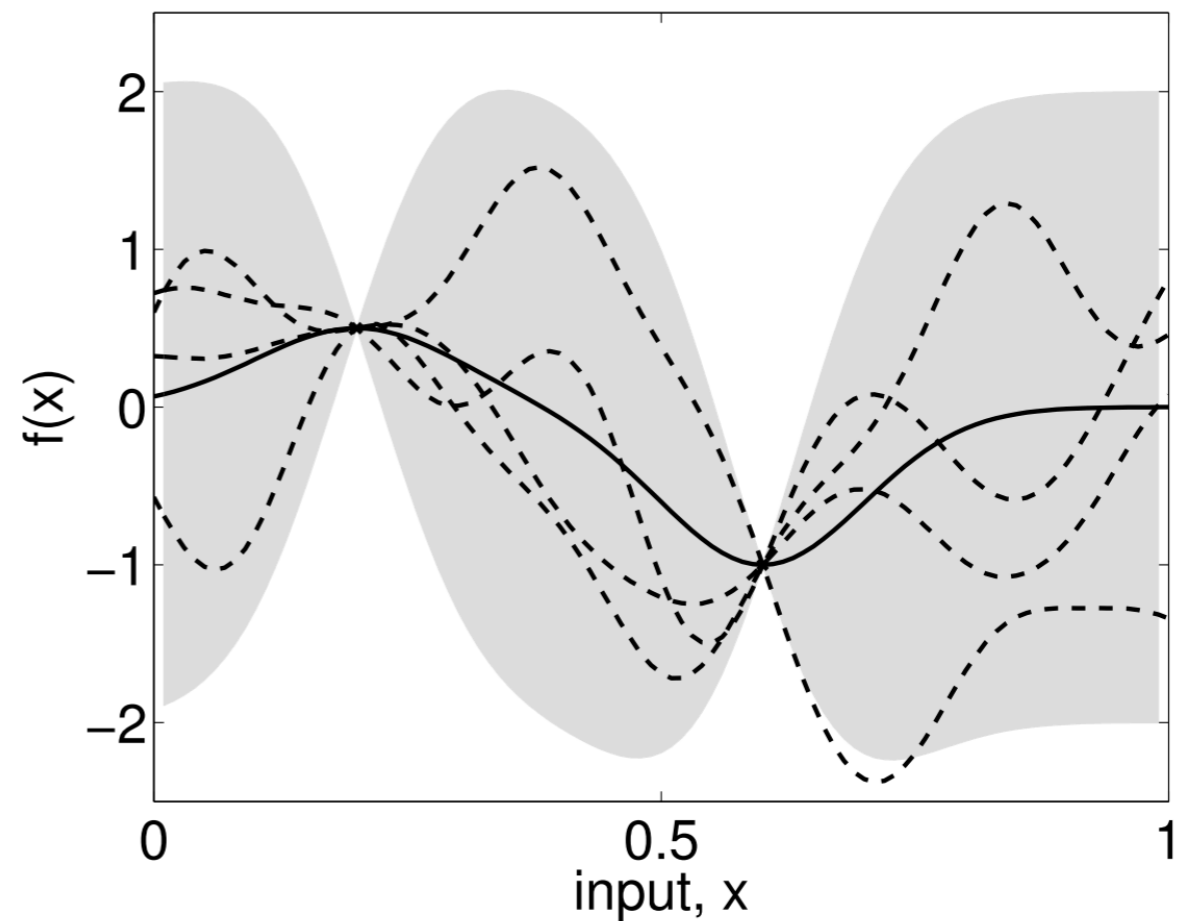


# Emulating Habitability

Non-parametric? Bayesian? Gaussian processes!?



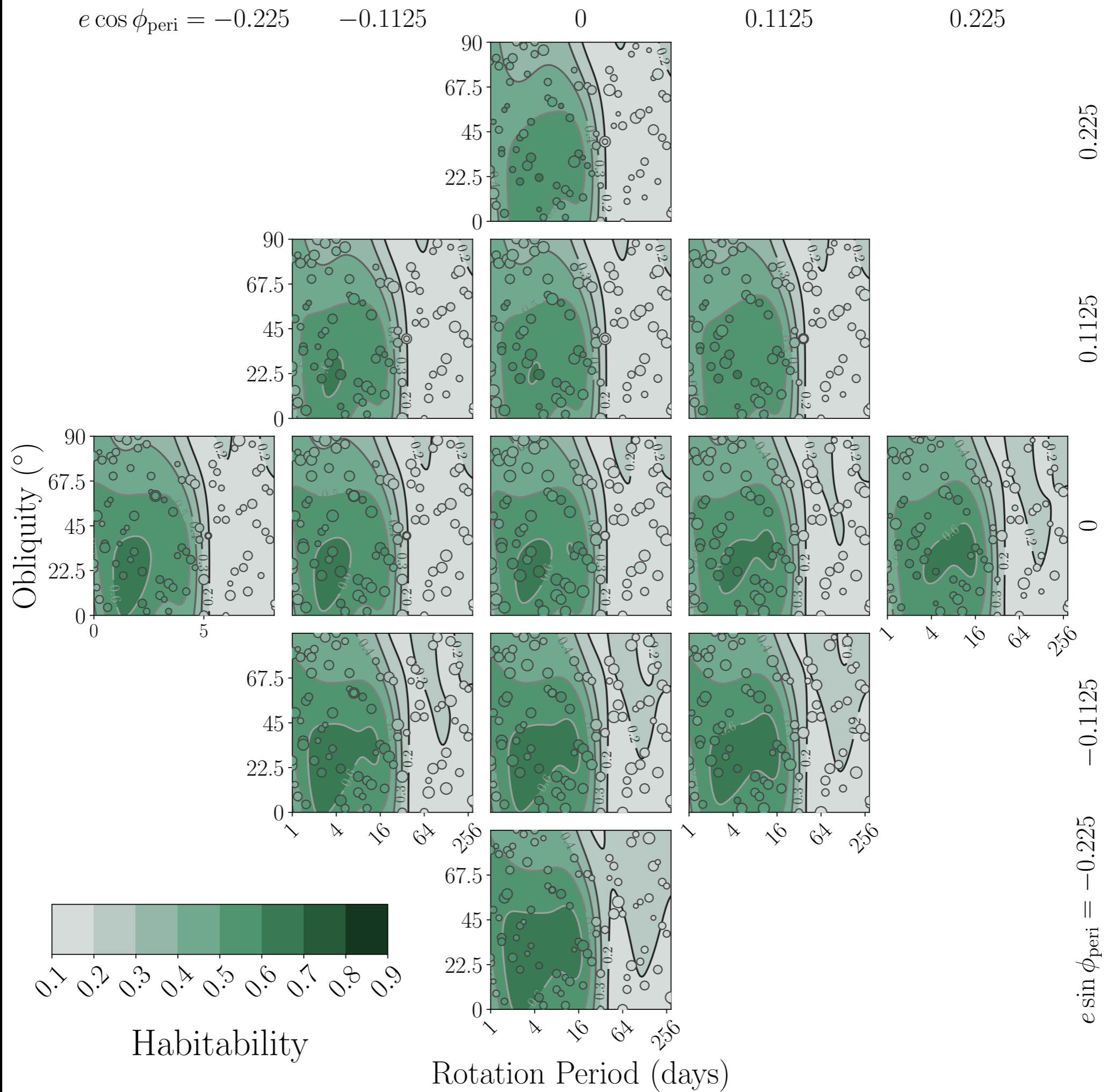
(a), prior



(b), posterior





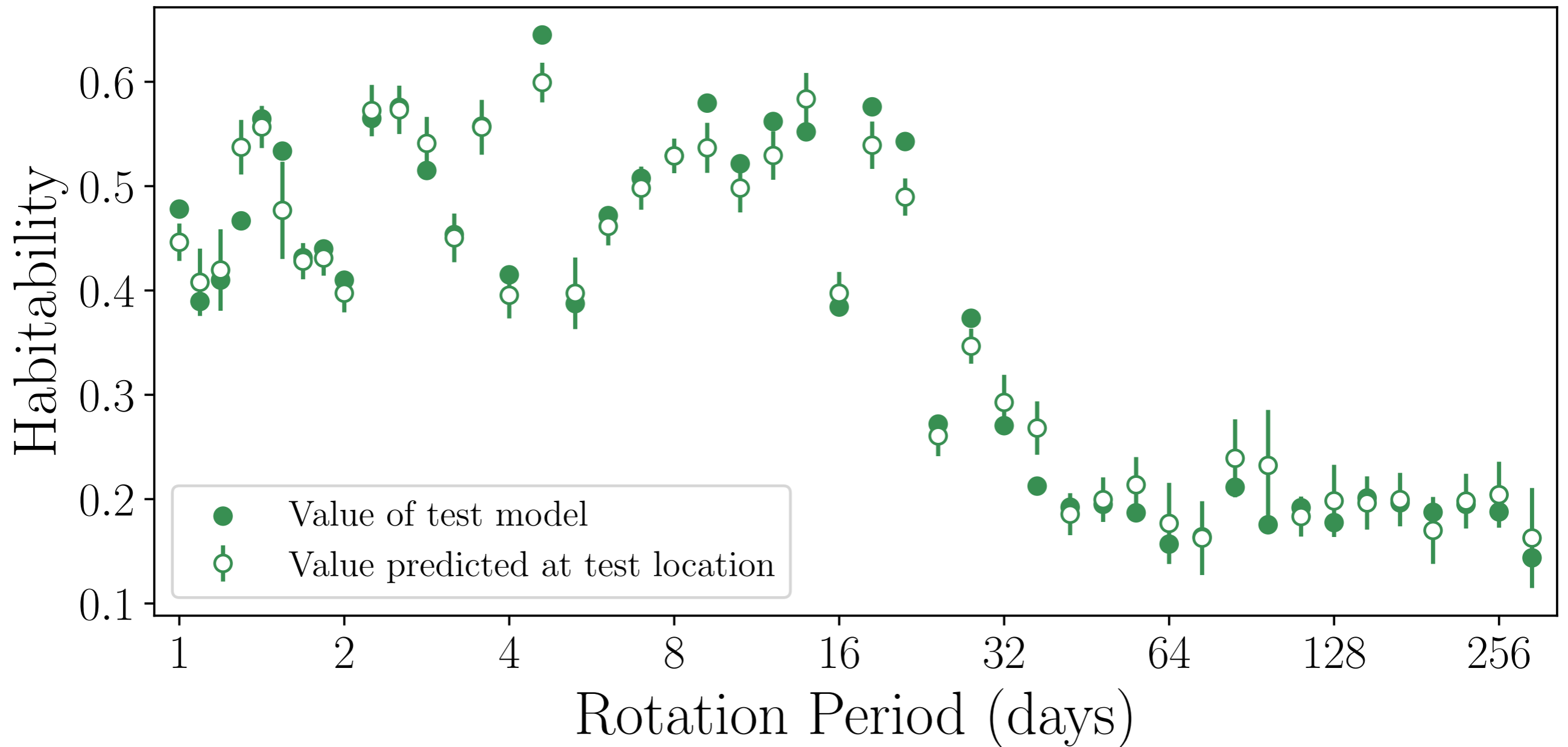


$\sin \Phi$

$\uparrow$



**Emulator does a  
pretty good job**



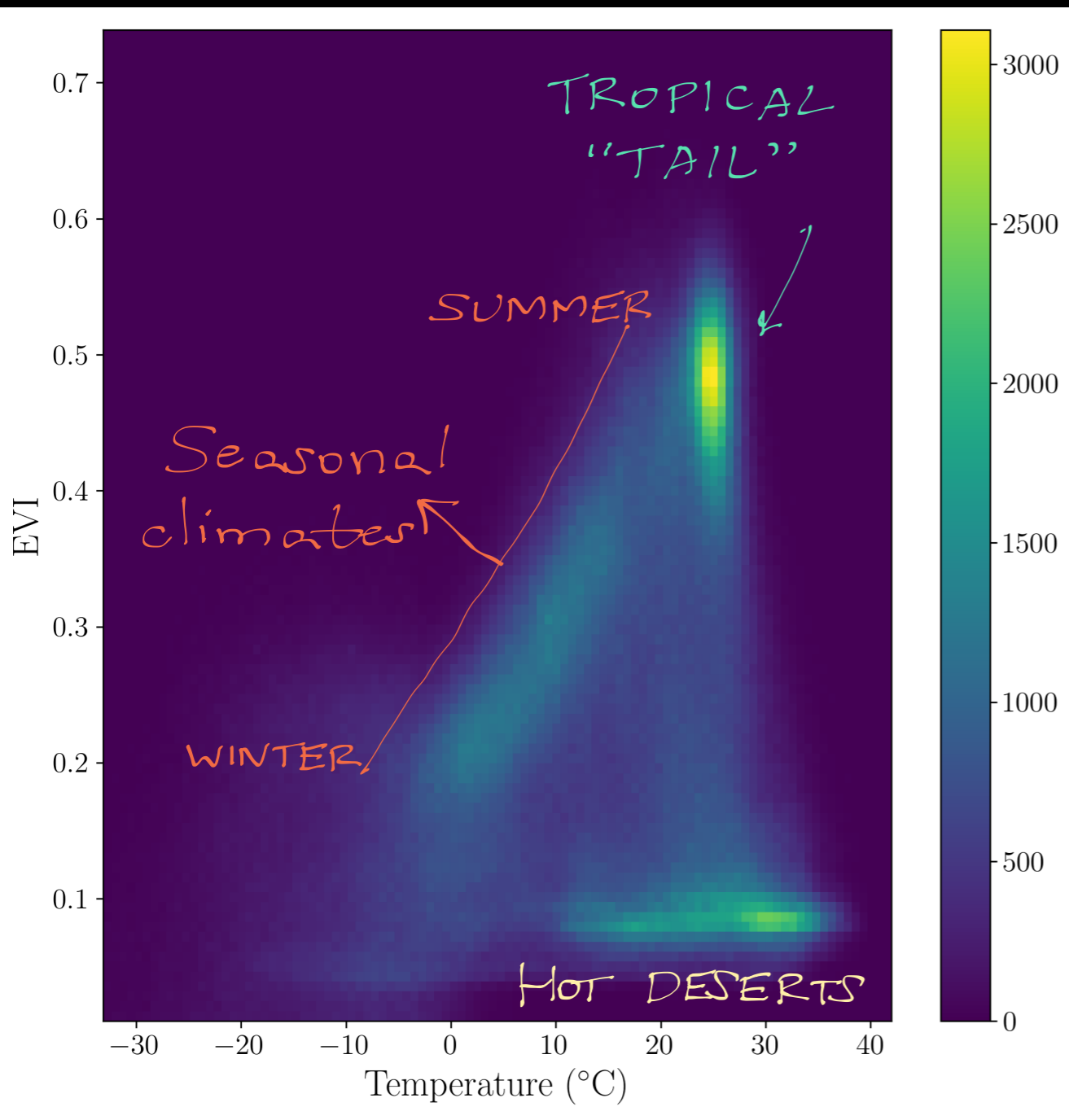


# Key Points

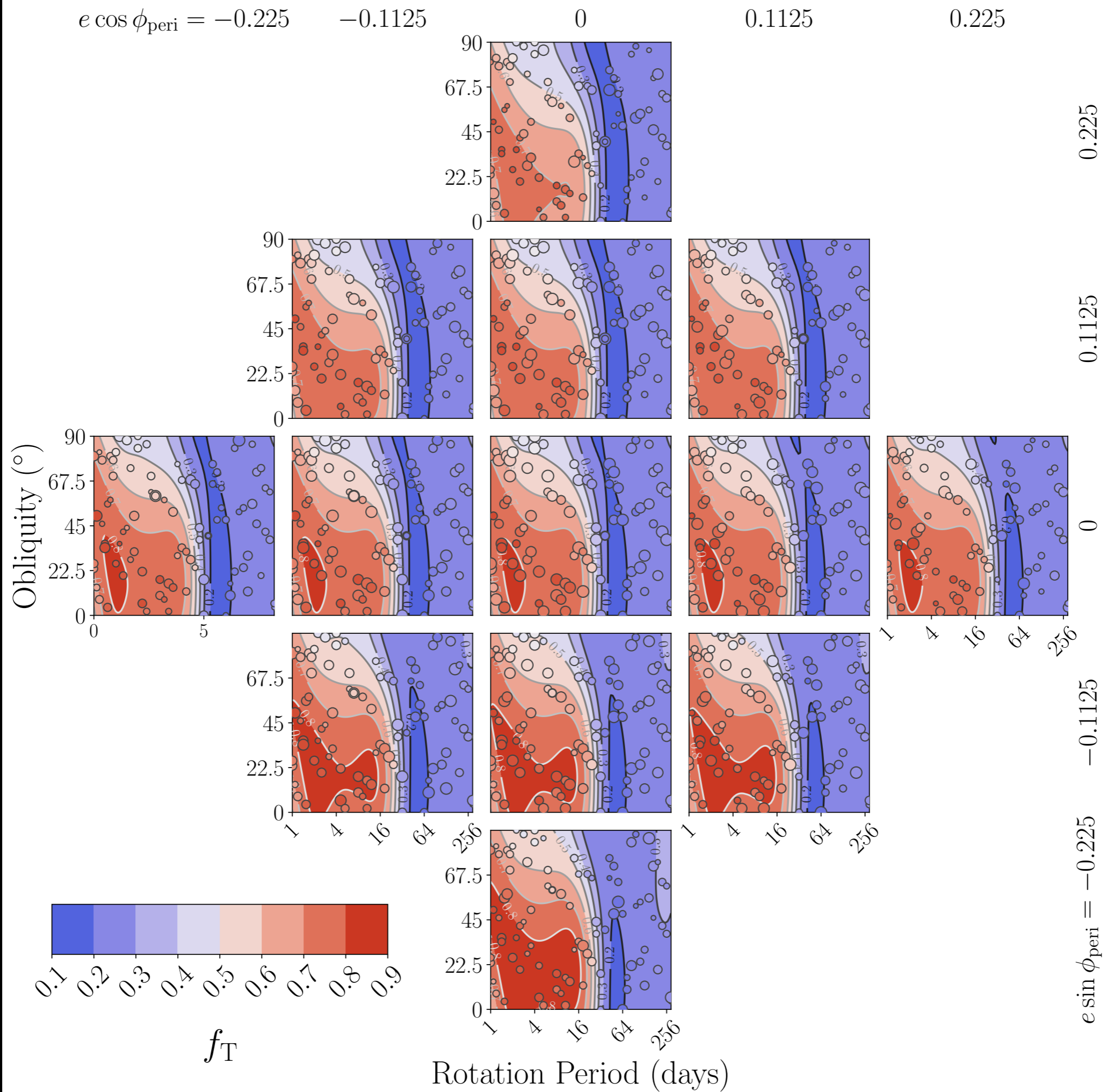
- Rotation period is the primary influence on habitability
  - ➔ Obliquity influences habitability at “faster” rotations ( $\lesssim 20$  days); beyond this there’s a break in habitability where obliquity isn’t as important
  - ➔ Orbital eccentricity has the weakest effect of all (up to our limit of  $e = 0.225$ )
- A Gaussian process regression does a reasonable job of predicting a global+orbit-averaged climate habitability metric

# Future/Parallel Directions:

Vegetation index as a habitability metric?



**Annie Shelton**  
(former undergrad at UCR, now at Cornell)



$\sin \Phi$

$\uparrow$

