#### **TRANSIT TIMING**

MATTHEW J. HOLMAN HARVARD-SMITHSONIAN CENTER FOR ASTROPHYSICS



Matthew J. Holman

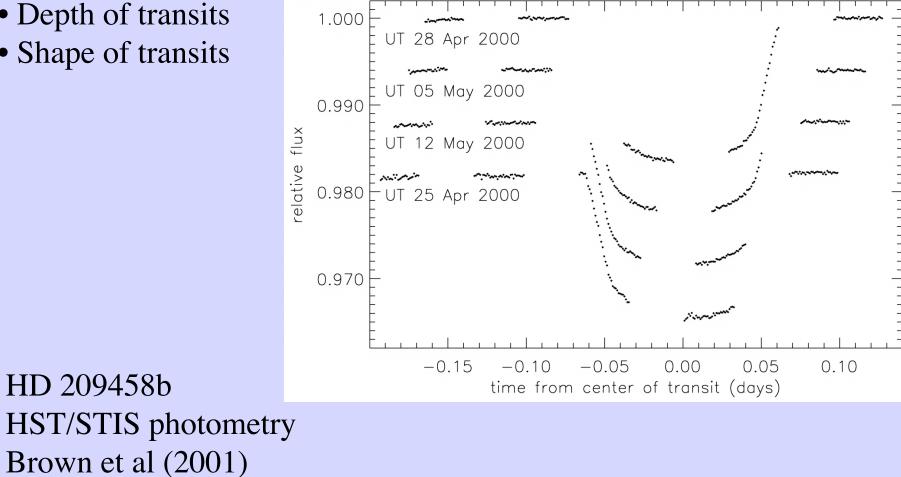
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## Outline

- Transit method and its observables
- Using transit timing to detect other planets
- The Transit Light Curve (TLC) Project
- Summary

## **Transit Observables**

- Times of transit center
- Duration of transits
- Depth of transits
- Shape of transits

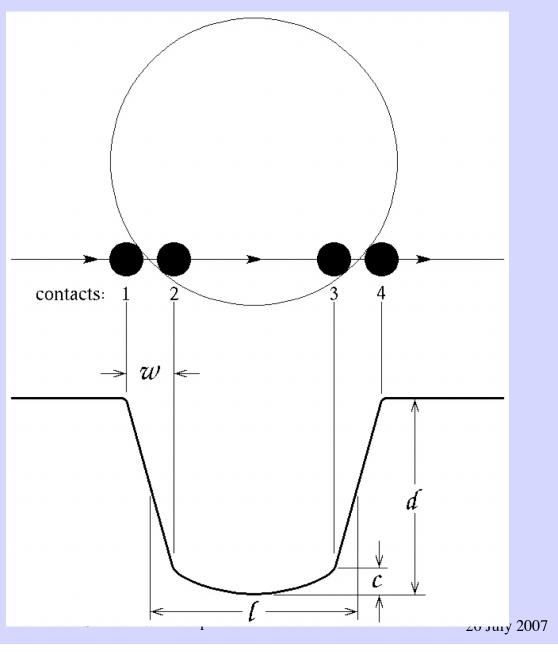


## Transit Observables

- Times of transit center
- Duration of transits
- Depth of transits
- Shape of transits



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## Orbit variations affect transit timings

• The intervals between successive transits of a planet on a fixed Keplerian orbit are constant.

• But the intervals will gradually change for orbits that precess due to the oblateness of the central star, general relativity, or the presence of other mass in the system (Miralda-Escude 2002).

• Tidal dissipation will alter the semimajor axis and eccentricity of a close-in planet, thereby changing the transit timings (Sasselov 2003).

• HOWEVER, the short-term interactions with other planets can have an even more important influence on the intervals between successive transits. This has been suggested for HD209458b (Bodenheimer et al 2004).

## Orbit variations affect transit timings

• Many of the theoretical aspects of the Transit Timing Variations (TTV) method have been worked out in a series of theory papers.

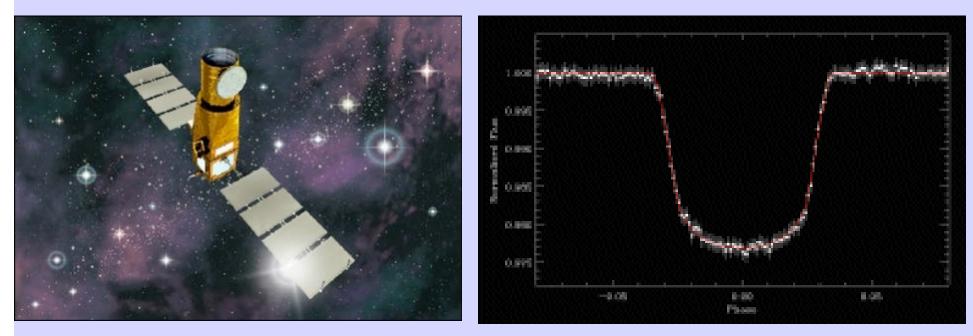
Holman & Murray 2005 **Science** 307, 1288 Agol, Steffen, Sari, and Clarkson 2005 **MNRAS** 359, 567

Heyl & Gladman 2007 MNRAS 377, 1511(long-term variations)Ford & Holman 2007 ApJ 664, 51(Trojans planets)Simon et al. 2007 A&A 470, 727("Exomoons")

The method has already been applied to specific systems TrES-1: Steffen & Agol 2005 MNRAS 364, 96
HD 209458b: Agol & Steffen 2007 MNRAS 374, 941
HD 209458b: Miller-Ricci 2007 (submitted)

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## The CoRoT Mission

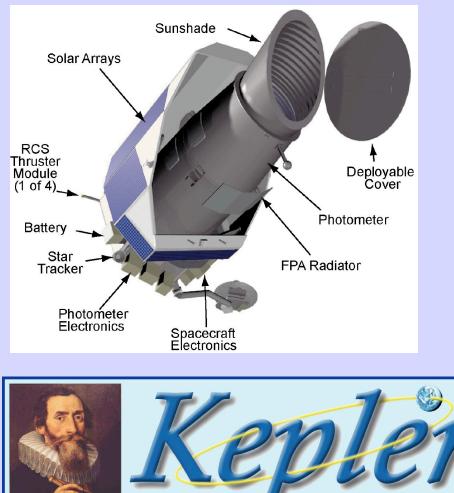


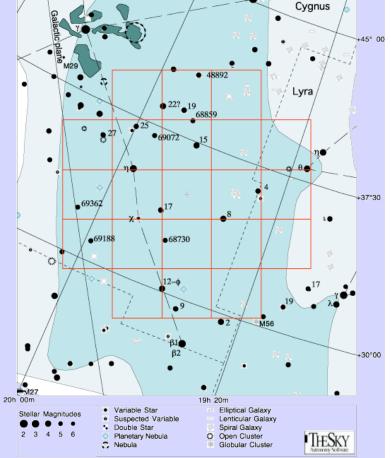
#### CoRoT-Exo-1b

#### Suzanne Aigrain's talk today

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## The Kepler Mission





Center RA: 19h 42m Dec: +34° 57' 5/2/00

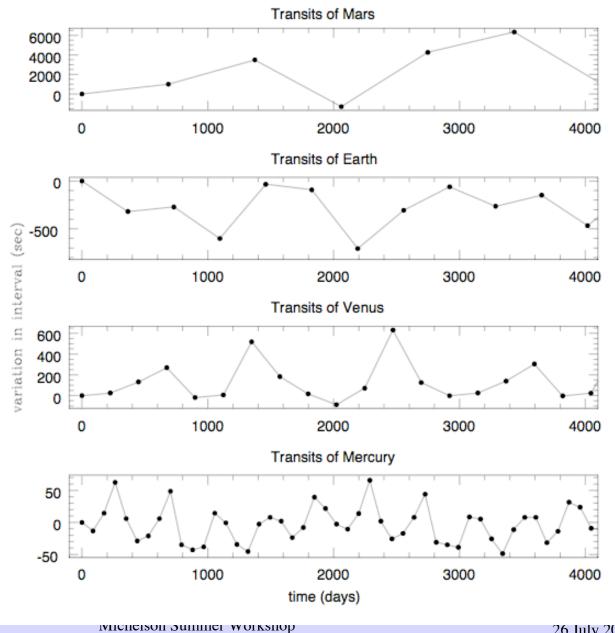
A Search for *Ferrestrial Planets* 

#### Bill Borucki's talk today

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## Our Solar System

Variation in the time between successive transits, recorded by a distant observer in the plane of each planet.

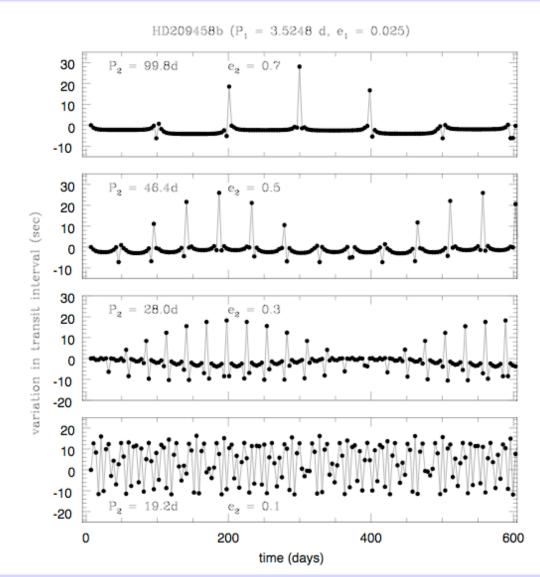


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## HD209458b with a hypothetical additional planet

## Method

- •Three-body problem (star and two planets, co-planar)
- $\bullet M_2 = M_J$
- Numerical integration of the heliocentric equations of motion
  - Bulirsch-Stoer numerical integratorRelative energy error
  - $dE/E \sim 10^{-12}$
- Iteratively search for times of transit center
- Calculate interval between successive transits



#### Not a traditional O-C plot.

## Timing variations vs Period and Eccentricity

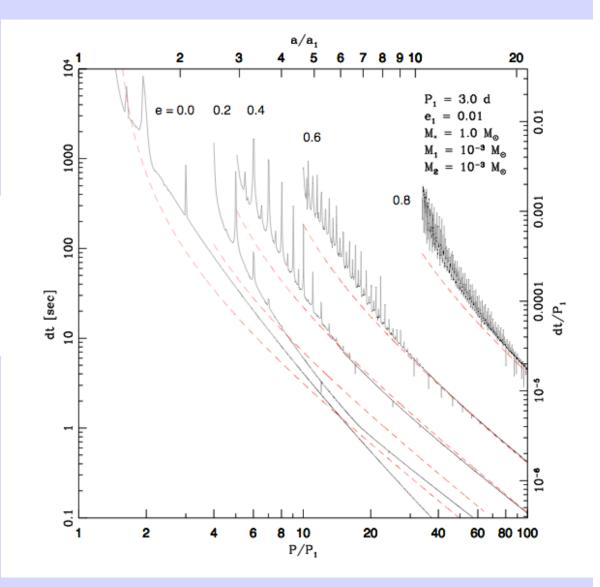
M<sub>J</sub> transiting planet
 M<sub>J</sub> perturber
 Co-planar

Analytic approximation:

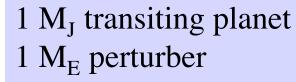
$$\Delta t \sim \frac{45}{16\pi} \left(\frac{M_2}{M_{\star}}\right) P_1 \alpha_e^3 \left(1 - \sqrt{2} \alpha_e^{3/2}\right)^{-1}$$

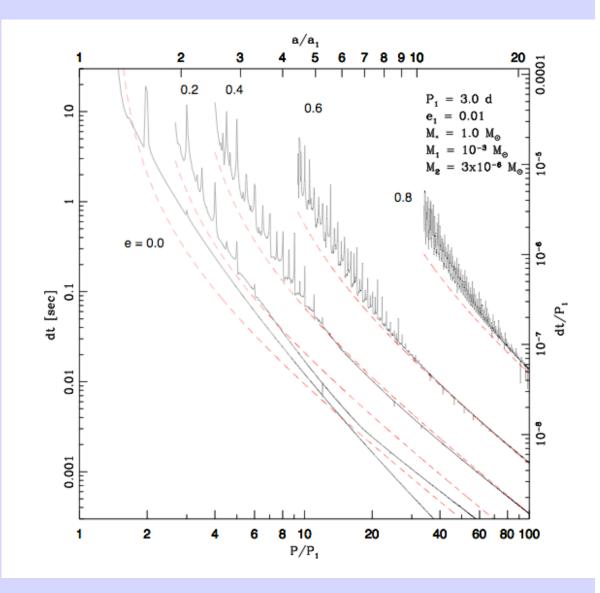
$$\alpha_e = \frac{a_1}{a_2(1-e_2)}$$

Linear in M<sub>2</sub>
Inversely proportional to M<sub>\*</sub>
Factor of P<sub>1</sub>
Factor of (P<sub>1</sub>/P<sub>2</sub>)<sup>2</sup>



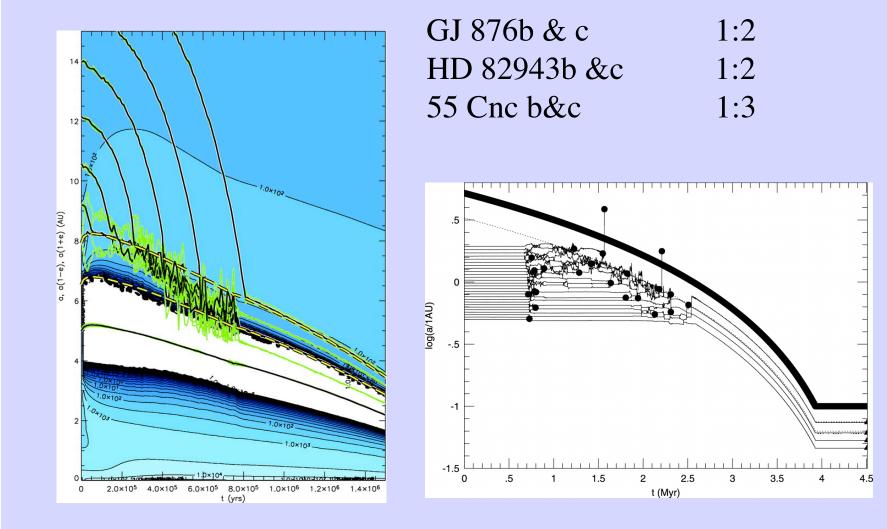
## Timing variations vs Period and Eccentricity





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#### Resonant planets are not uncommon



#### Thommes 2005

#### Zhou et al 2005

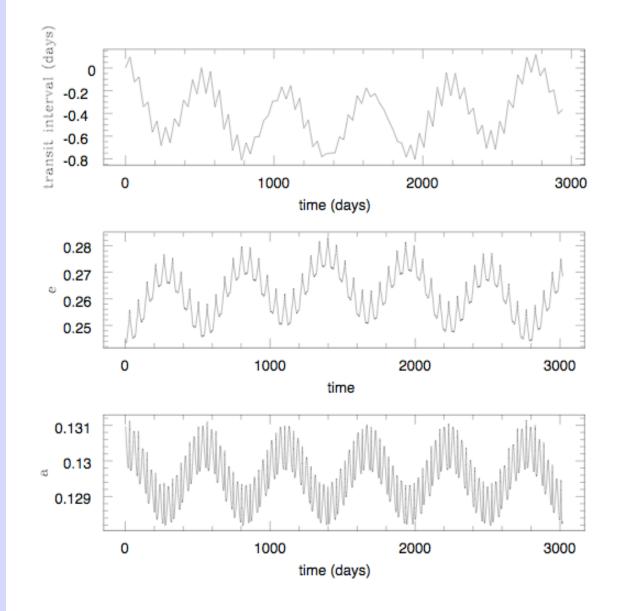
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## Extreme case of GJ876: planets in resonance

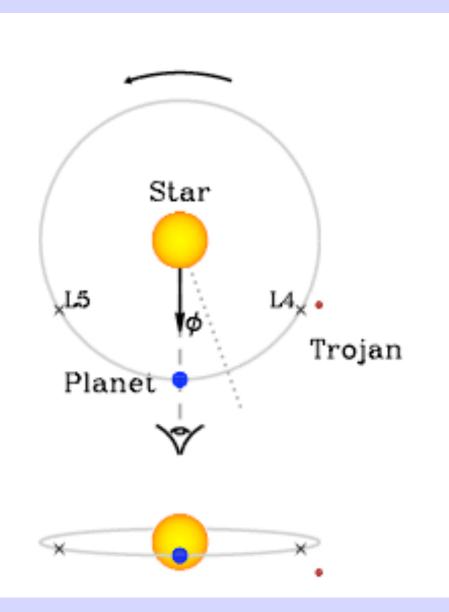
Transit interval variation

Eccentricity

Semimajor axis



## Transit timing of Trojan planets

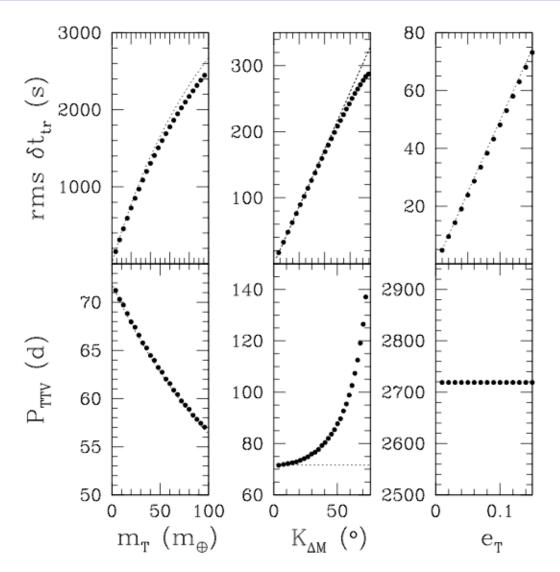


#### Figure from Ford & Gaudi 2007

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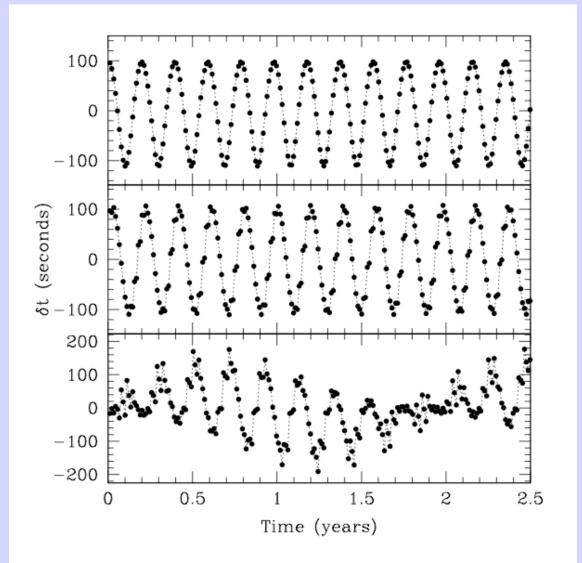
## Transit timing of Trojan planets



Ford & Holman 2007

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## Comparison of TTV signals



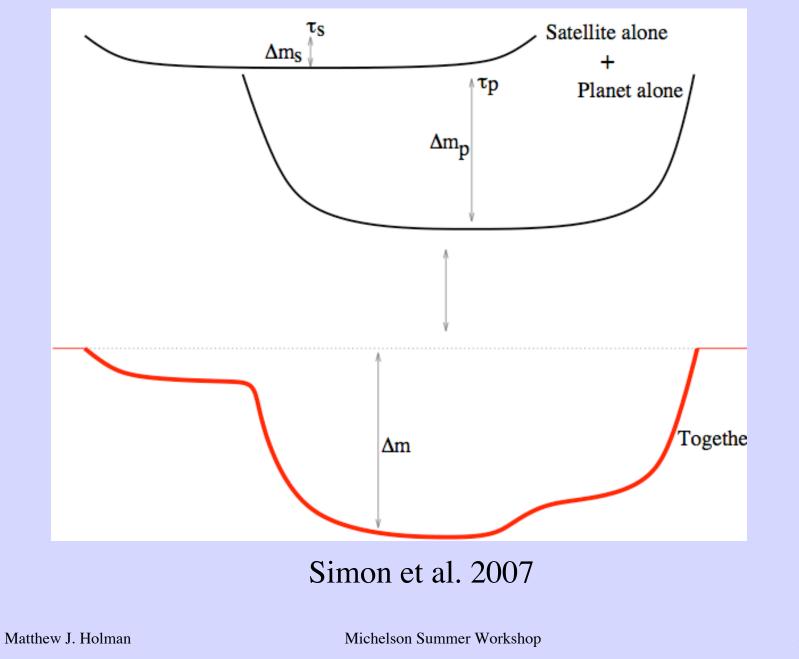
1 M<sub>E</sub> Trojan

#### 28 $M_E$ in exterior 2:1

#### $5 M_{\rm E}$ in interior 3:2

#### Ford & Holman 2007

## Transit timing of "Exomoons"



## **Double Transiting Systems**

If one sees transits of one planet in a multiple planet system, what is the probability of seeing transits of a second planet?
Can obtain estimates of masses and radii of both planets

• This allows estimates of the densities of the planets, without radial velocity measurements. Co-planar Orbits

$$P_{t_2} = a_1/a_2$$

• Mutually inclined orbits, with the inner planet transiting the center of the star.

$$P_{t_2} = rac{2}{\pi} rcsin\left(rac{R_*}{a_2 \sin i'}
ight)$$

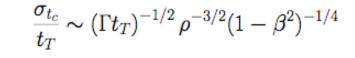
i' = mutual inclination of the two planets Assumes  $\sin i' > R_*/a_2$ , otherwise transits of the second planet are certain.

For 
$$R_* = R_{\odot}$$
,  $i' \sim 5^{\circ}$ , and  $a_2 \sim 1 \text{ AU}$ ,  
 $P_{t_2} \sim 10\%$ .

(also David Koch's 1995 DPS abstract and poster)

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## **Detection limits**



 $\sigma_{t_c}$  = error in measurement of transit center  $t_T$  = transit duration  $\Gamma$  = stellar photon count rate  $\rho = R_p/R_*$  $\beta$  = impact parameter (in stellar radii) Assumes photon noise limited observations For Kepler (D = 0.95 m, broad filter):  $\Gamma = 7.8 \times 10^8 \, 10^{-0.4(V-12)} \, \mathrm{hr}^{-1}$ • For a hot Jupiter orbiting a V = 12 solar-type star, ( $\rho \sim 0.1$ ,  $t_T \sim 3hr$ ):  $\bullet$   $\sigma_{tc} \sim 10 \, s$ • For an Earth-sized planet in a 1-year orbit about a V = 12solar-type star, ( $\rho \sim 0.01, t_T \sim 13$ hr):  $\bullet$   $\sigma_{t_c} \sim 500 \, \mathrm{s}$ For Magellan (D = 6.5 m, broad filter):  $\Gamma = 3.7 \times 10^{10} \ 10^{-0.4(V-12)} \ hr^{-1}$ • For a hot Jupiter orbiting a V = 12 solar-type star, ( $\rho \sim 0.1$ ,

 $t_T \sim 3hr$ ):

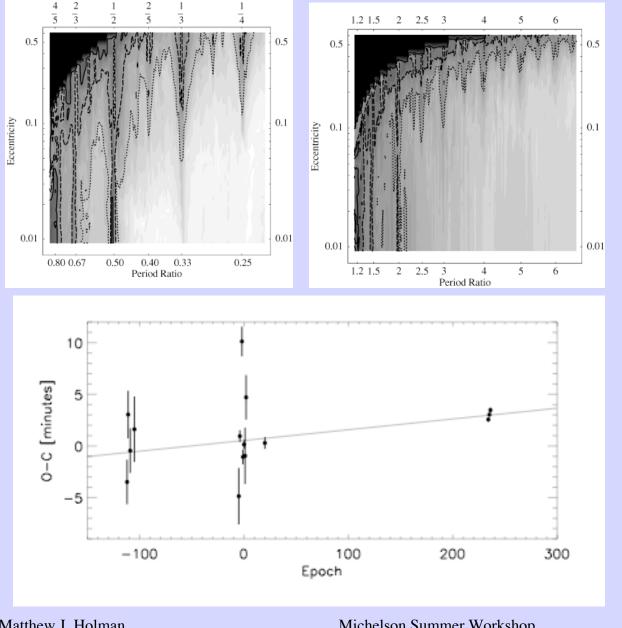
 $\sigma_{t_c} \sim 1 \,\mathrm{s}$ 

Requires control of systematic effects 26 July 2007

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# What can we do while we wait for results from CoRoT and Kepler?

#### We can use existing ground-based observations: TrES-1



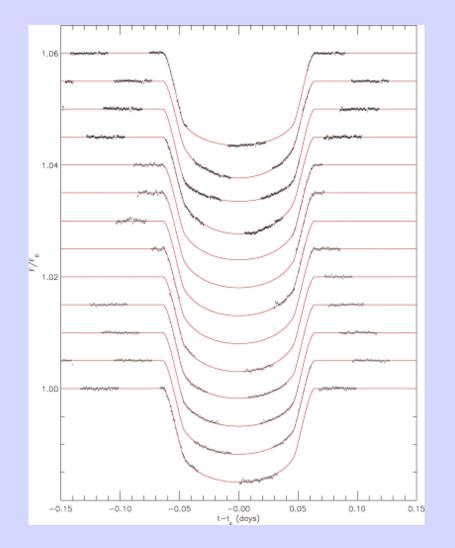
Steffen & Agol 2005

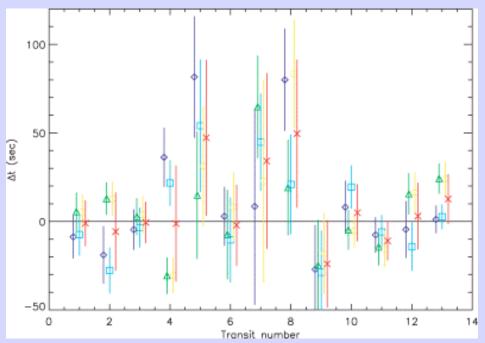
Winn, Holman, Roussanova 2007

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# We can use existing space-based observations: HD 209458b

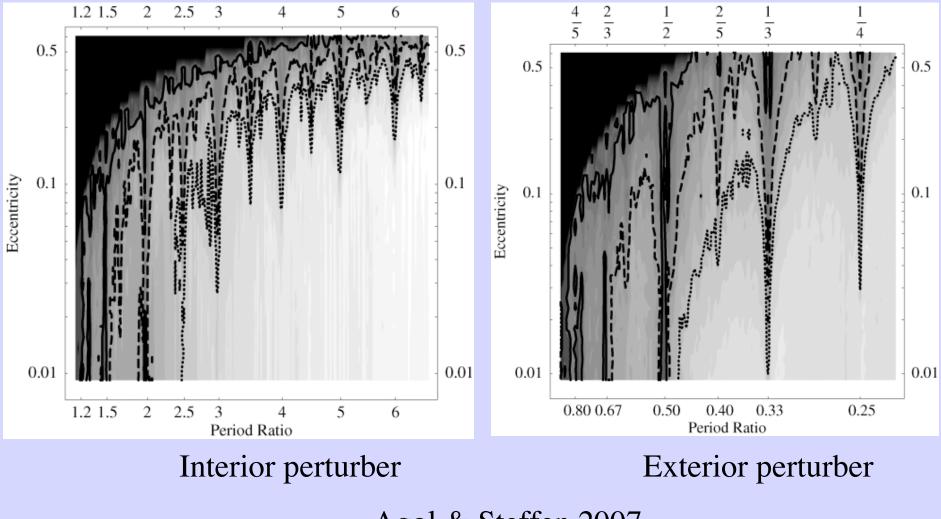




Agol & Steffen 2007

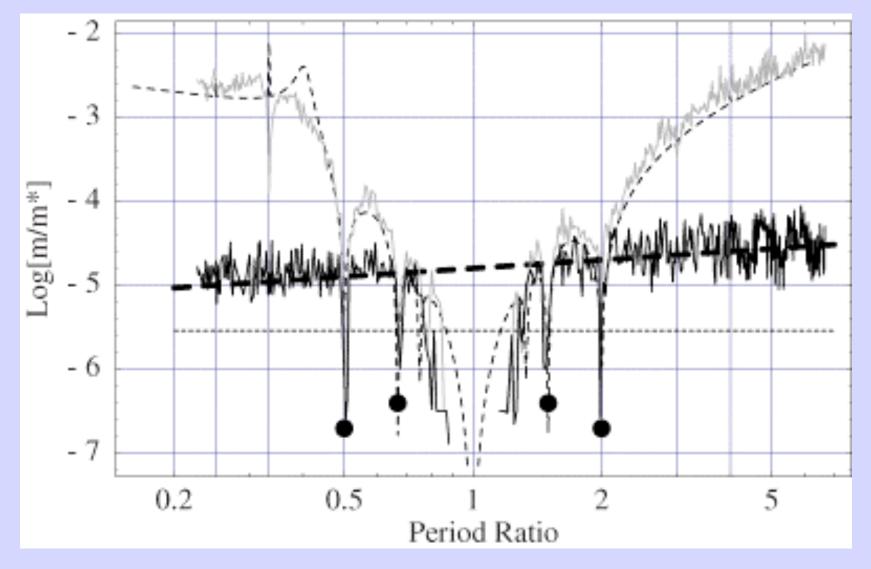
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## HD 209458b perturber mass limits



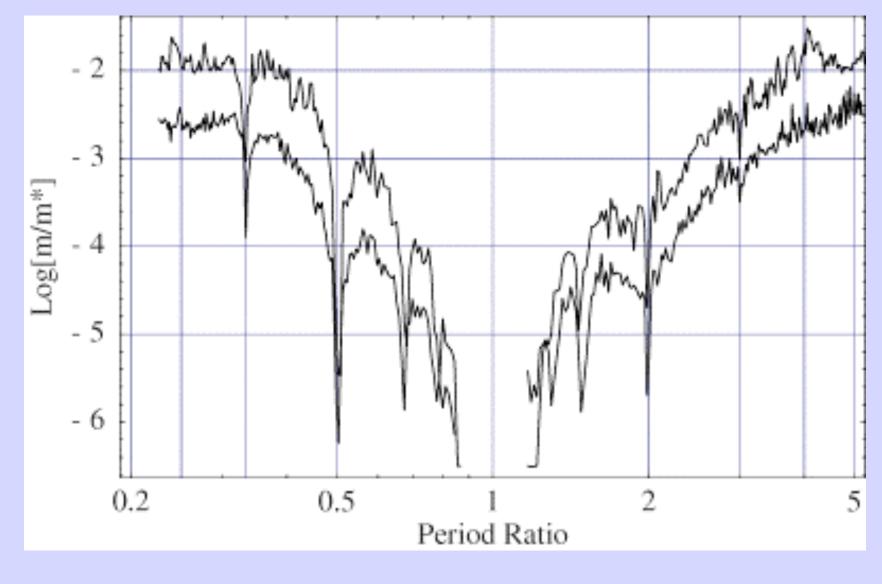
Agol & Steffen 2007

HD 209458b



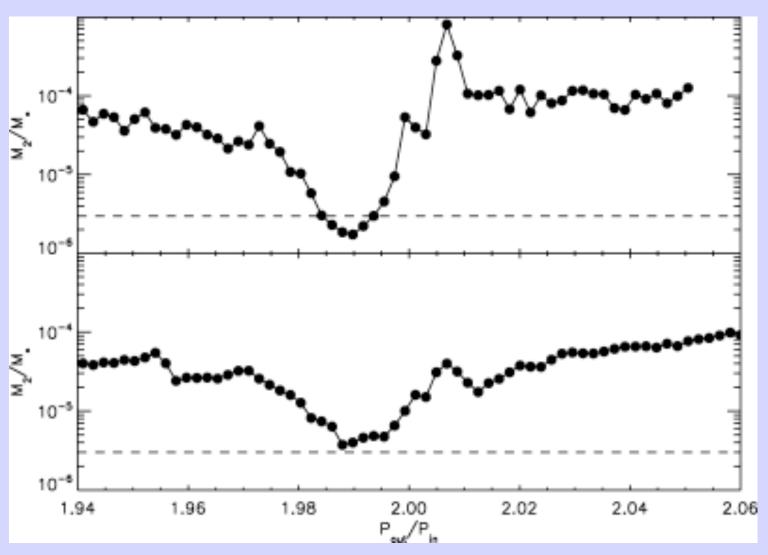
#### Agol & Steffen 2007

## TrES-1 vs HD 209458b



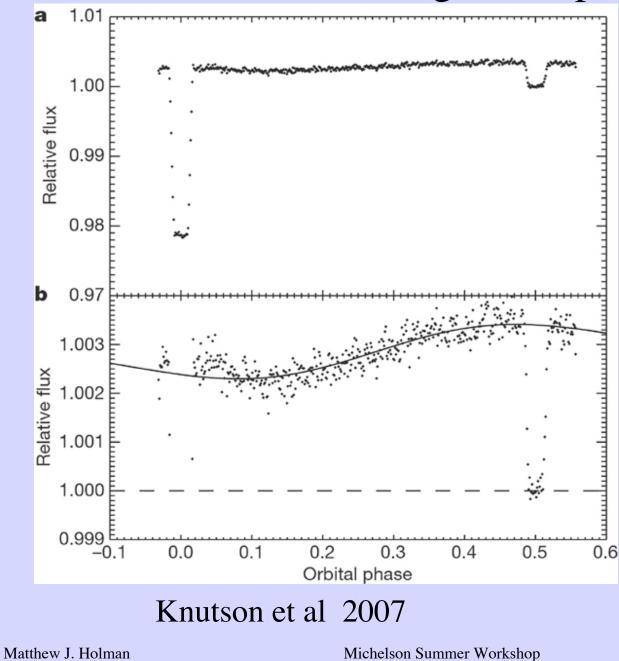
Agol & Steffen 2007





Agol & Steffen 2007

### Transit timing with Spitzer



HD 189733b

~6 sec timing precision for primary transit.

~24 sec timing precision for secondary eclipse.

Best achieved to date.

Eric Agol has a Spitzer program to observe 6 primaries and 6 secondaries of HD 189733b.

## We can collect more ground-based data: The Transit Light Curve Project

#### THE TRANSIT LIGHT CURVE (TLC) PROJECT

MATTHEW J. HOLMAN (CFA) JOSHUA N. WINN (MIT)

Dave Latham (CfA) Dave Charbonneau (CfA) Gaspar Bakos (CfA) Francis O'Donovan (Caltech) Dimitar Sasselov (CfA) Cesar Fuentes (CfA) Joel Hartman (CfA) Jose Fernandez (CfA) Kris Stanek (OSU) Scott Gaudi (OSU)

Tsevi Mazeh (Tel Aviv) Avi Shporer (Tel Aviv) Guillermo Torres (CfA) Gil Esquerdo (CfA, PSI) Mark Everett (PSI) Anna Roussanova (MIT) Andras Pal (Eotvos) Wesley Fraser (U. Vic) Lynne Jones (NRC Canada) Carl Hergenrother (LPL)

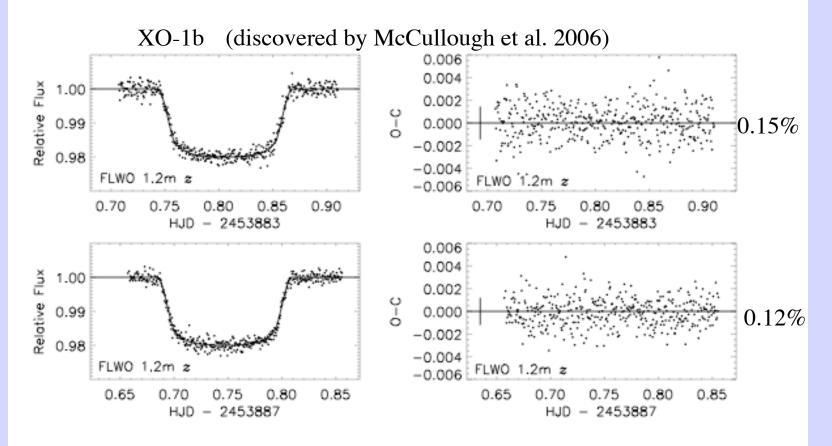
#### The TLC Project:

We have initiated a long-term campaign to build a library of high-precision transit photometry.

The goals of the project are:

- 1. To refine the physical and orbital parameters of all suitable known transiting extrasolar planets.
- 2. To search for transit time variations that may result from the perturbation of other planets, precession, tidal dissipation, etc.
- 3. To search for stellar flux reflected from extrasolar planets near times of secondary eclipses to constrain the atmospheric properties of such planets.

#### TLC I: XO-1b (Holman et al. 2006)

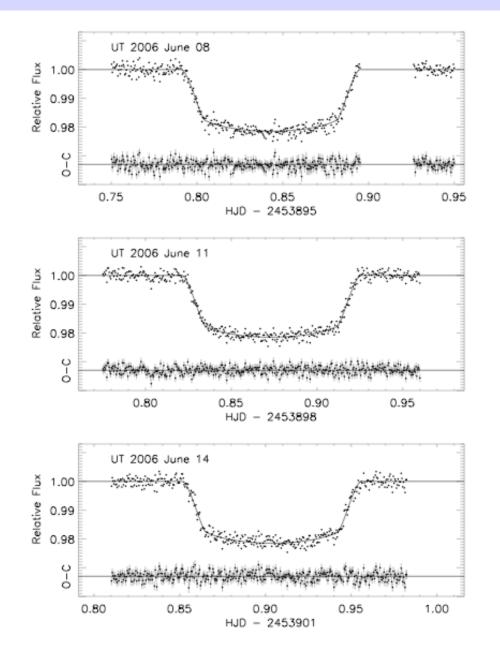


FLWO 1.2m, Keplercam z-band observations: 30 sec exposures, auto-guiding, 11.5 sec read/reset time Aperture photometry with 4 nearby comparison stars of similar magnitude and color, differential extinction correction.

 $M_{S} = 1.00 + -0.03 M_{sun}$  assumed. Uncertainties dominated by stellar mass.  $R_{\rm P} = 1.184 + 0.025 / -0.018 R_{\rm jup}$  $R_{\rm S} = 0.928 + 0.018 / -0.013 R_{\rm jup}$ 

Uncertainties in  $T_C$  unc. ~ 15-20 sec, comparable or better than with HST.Matthew J. HolmanMichelson Summer Workshop

#### TLC III: TrES-1 (Winn, Holman, Roussanova 2007)



Keplercam z-band observations: 30 sec exposures, auto-guiding, 10 sec read/reset time Aperture photometry with nearby comparison stars of similar magnitude and color, differential extinction correction.

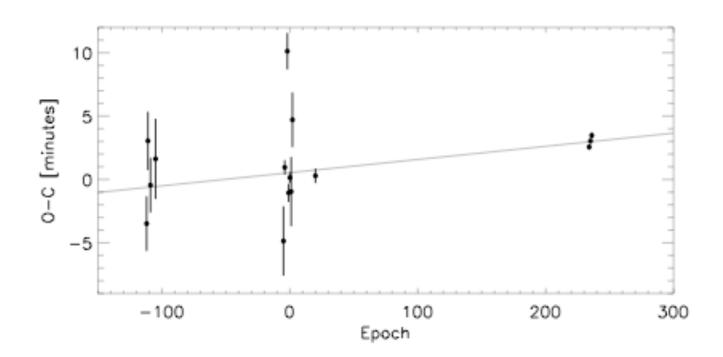
Mild a priori constraint on limb darkening coefficients.

 $T_{C}$  uncertainties ~ 15 sec.

 $R_{\rm P} = 1.085 \text{ +/- } 0.029 \text{ R}_{\rm jup}$   $R_{\rm S} = 0.812 \text{ +/-} 0.020 \text{ R}_{\rm jup}$  $M_{\rm S} = 0.89 \text{ +/- } 0.05 \text{ M}_{\rm sun} \text{ assumed.}$ 

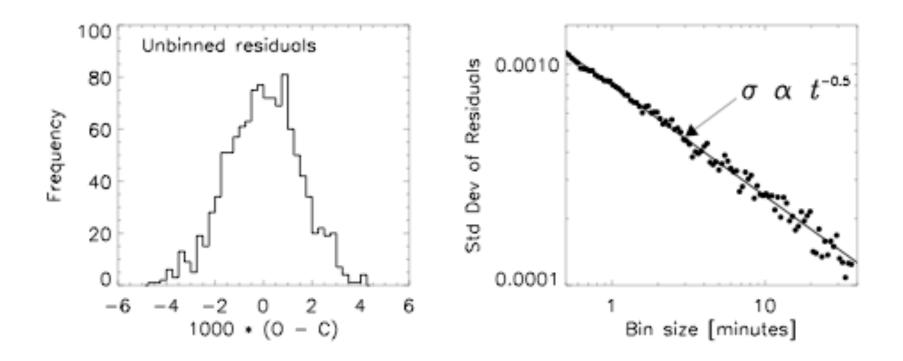
Uncertainties dominated by stellar mass.

## TrES-1

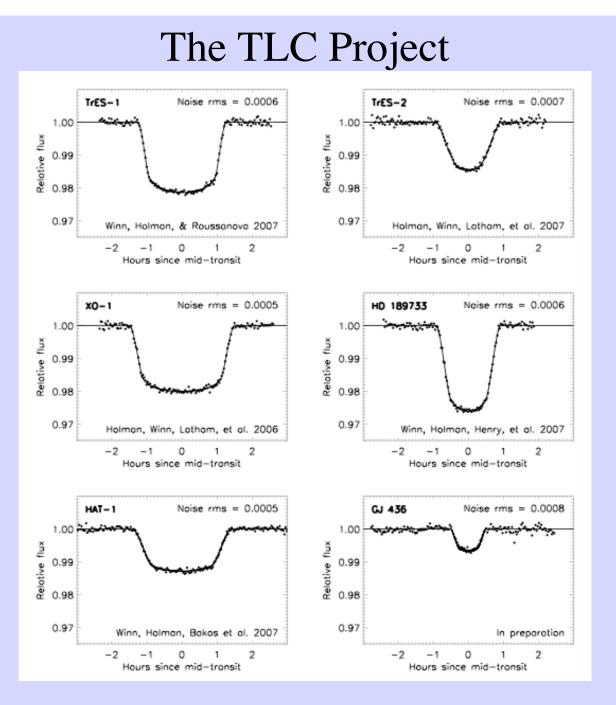


 $T_C$  uncertainties ~ 10-15 sec

## TrES-1



The KeplerCam data are remarkably free of systematic errors!



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#### What is the TLC Project doing right?

KeplerCam has rapid readout and excellent cosmetic properties.

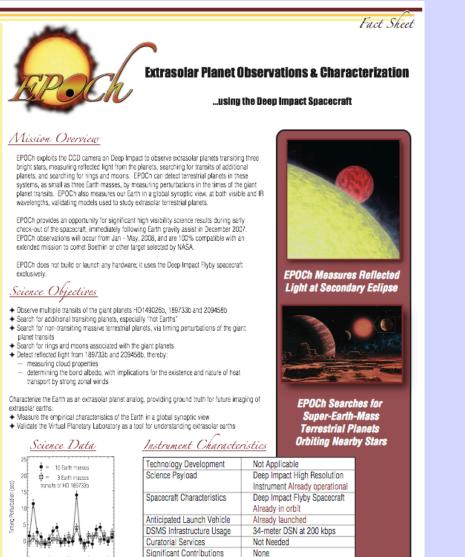
For moderately bright (V~10-12) northern hemisphere targets we have

- Plenty of signal and little scintillation in 30 sec exposures with 1.2-m.
- Numerous nearby comparison stars of similar magnitude and color.
- Good sampling of the PSF.
- Good resolution of the 4 points of contact in z band.
- Apparent lack of significant systematic errors (for many targets).

We are able to obtain and schedule, through the formal TAC process and informal trading and collaboration, multiple nights of observation near the time of announcement.

High-precision, high cadence photometry allows us to fit for the radius of the star and planet, assuming only the stellar mass.

#### We can re-use spacecraft to observe transiting planets



**EPOXI** selected!

A'Hearn (DIXI PI) Deming (EPOCH PI)

Charbonneau (CfA) Holman (CfA) Kuchner (GSFC) Lisse (JHU) Livengood (GSFC) Pedelty (NASA) Richardson (GSFC) Schutz (NASA) Seager (DTM) Veverka (Cornell) Wellnitz (U. MD)

Drake Deming's talk today

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Transit Numbe

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## We propose new space missions: There is an Announcement of Opportunity for NASA Small Explorer Missions

## Summary of Transit Timing

- The presence of one or more additional planets in transiting systems can lead to variations in the times, durations, and light curve shapes of transits.
- Many of these variations will be detectable with Kepler, CoRoT, EPOXI/EPOCh, or ground-based telescopes, allowing one to detect the presence of additional planets in transiting systems.
- More theoretical work is needed:
  - The non-co-planar case, including transit durations and depths.
  - <sup>-</sup> The inverse problem of determining the the perturbing planet's orbit and mass.
  - More detailed work on the observational limits.
- There is an opportunity to propose new Small Explorer Missions.

Matthew J. Holman