

# Core Accretion Scenario of Exoplanet Formation

Douglas N.C.

Lin

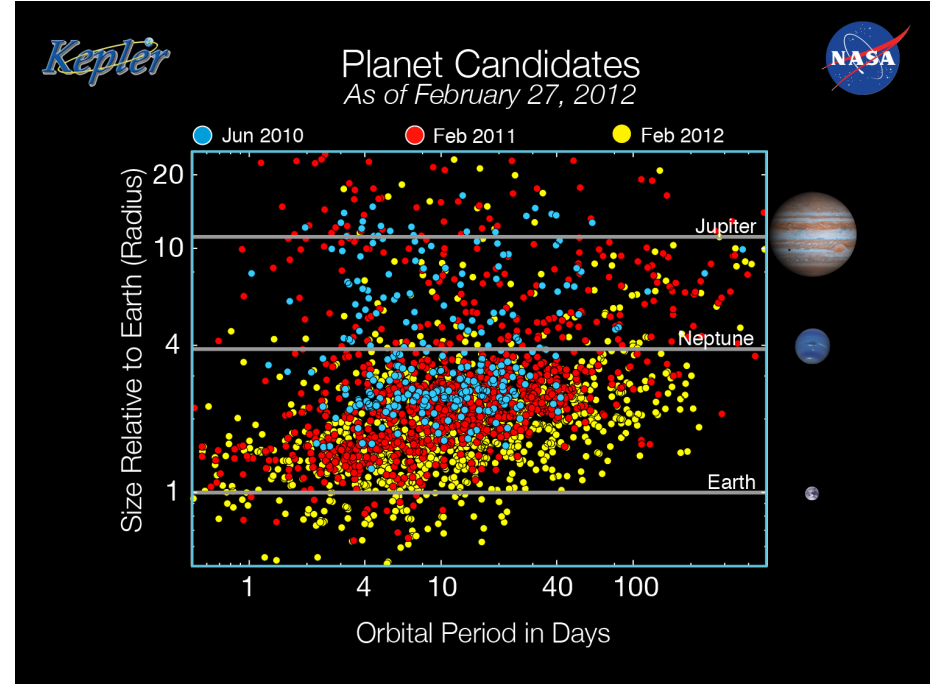
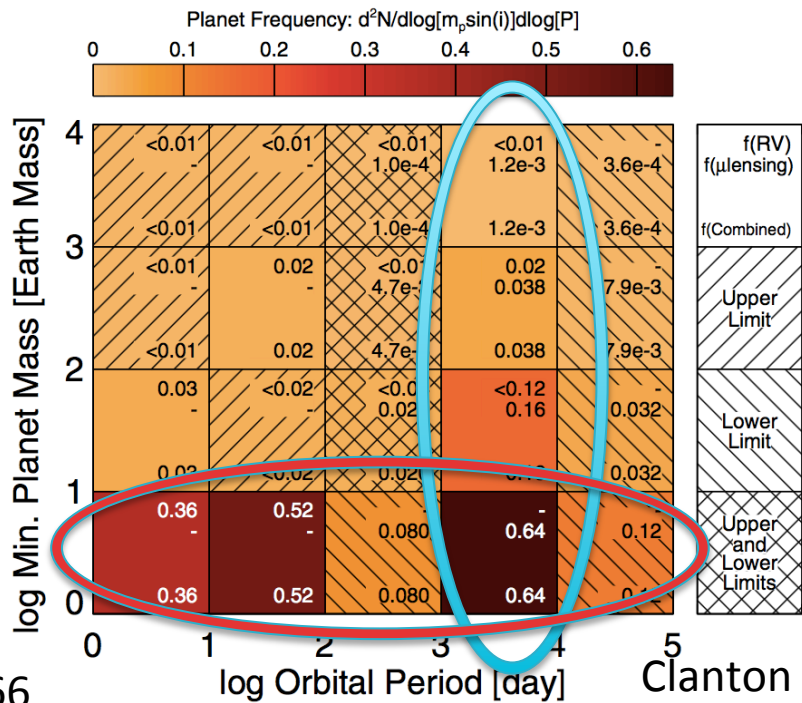
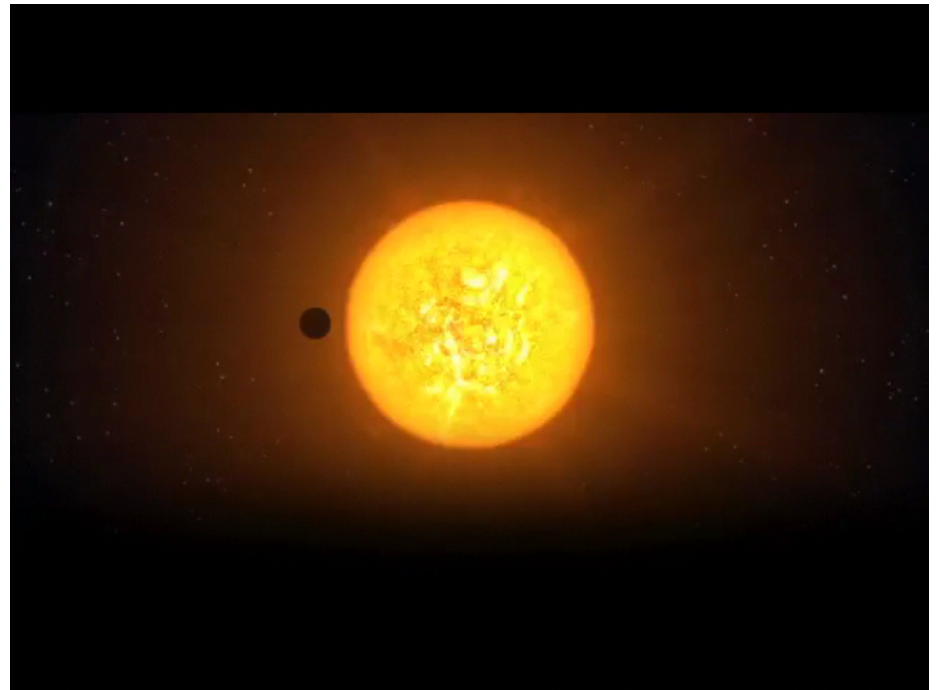
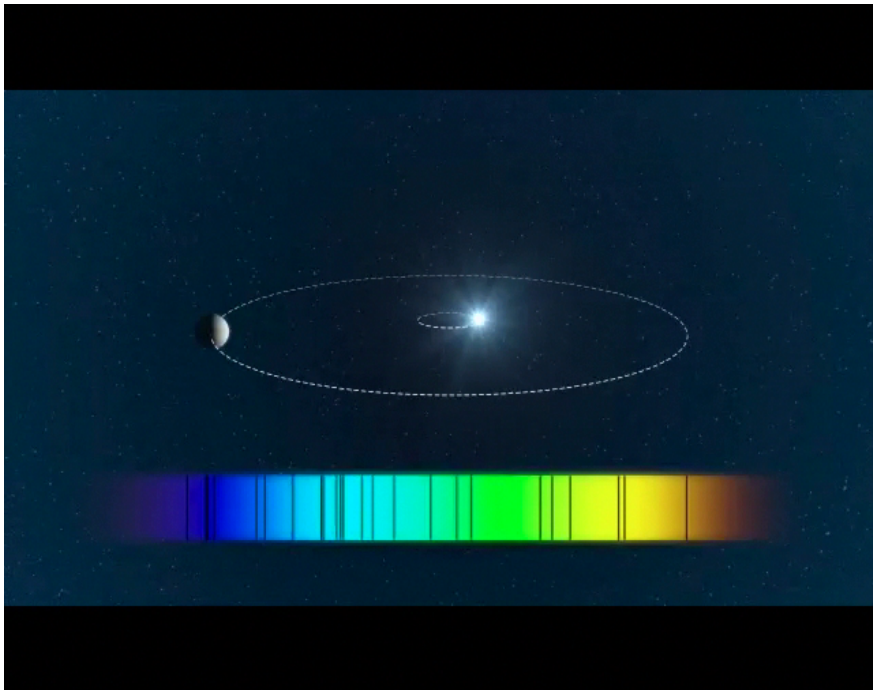
Astronomy (UCSC), KIAA (PKU), IAS (THU)

Beibei Liu, Xiaojia Zhang, Zhuoxiao Wang, Shangfei Liu, Xiaochen Zheng  
Rui Xu, Rixin Li, Yuan Zhang, Bili Dong, Wenhua Ju, Randy Laine, Yas

Hori ***Exoplanetary System Demographics: Theory and Observations***

Beckman Institute, Caltech, July 27-31, 2015

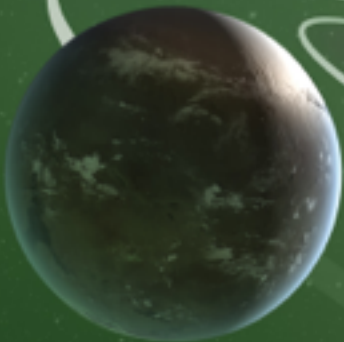




# Science

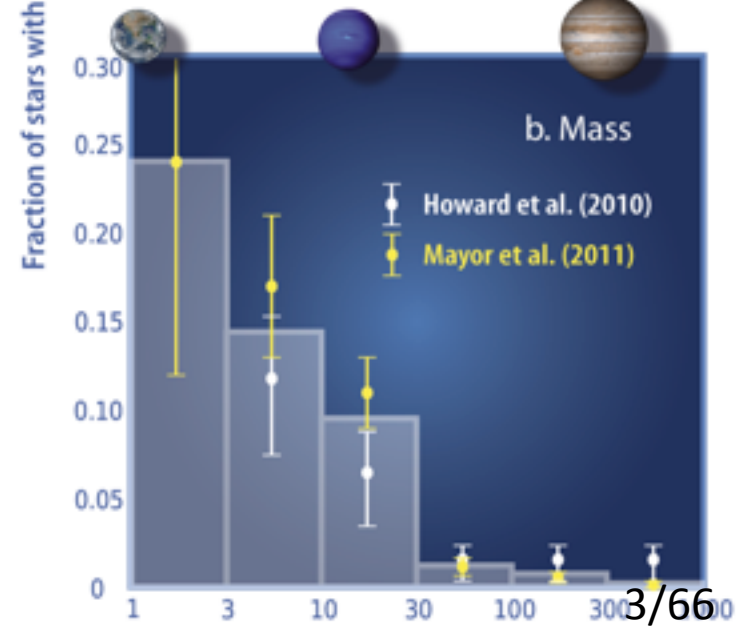
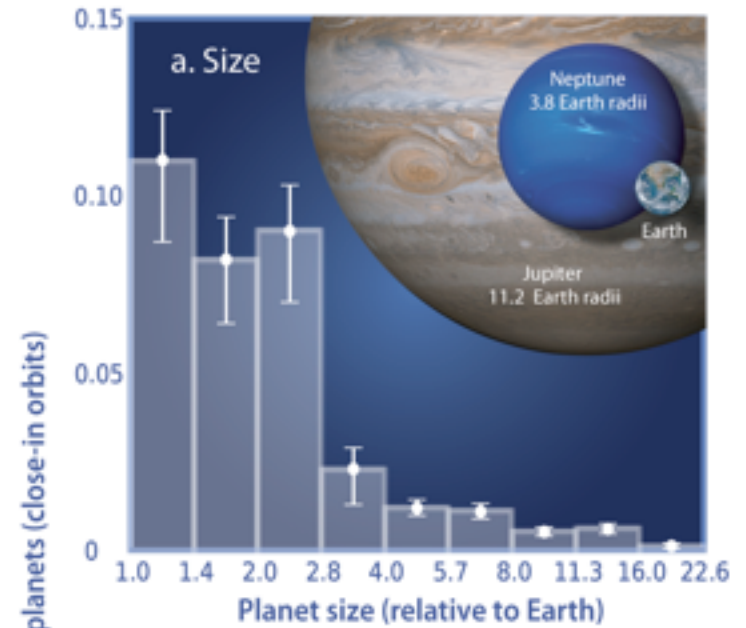
3 May 2013 | \$10

Exoplanets



AAAS

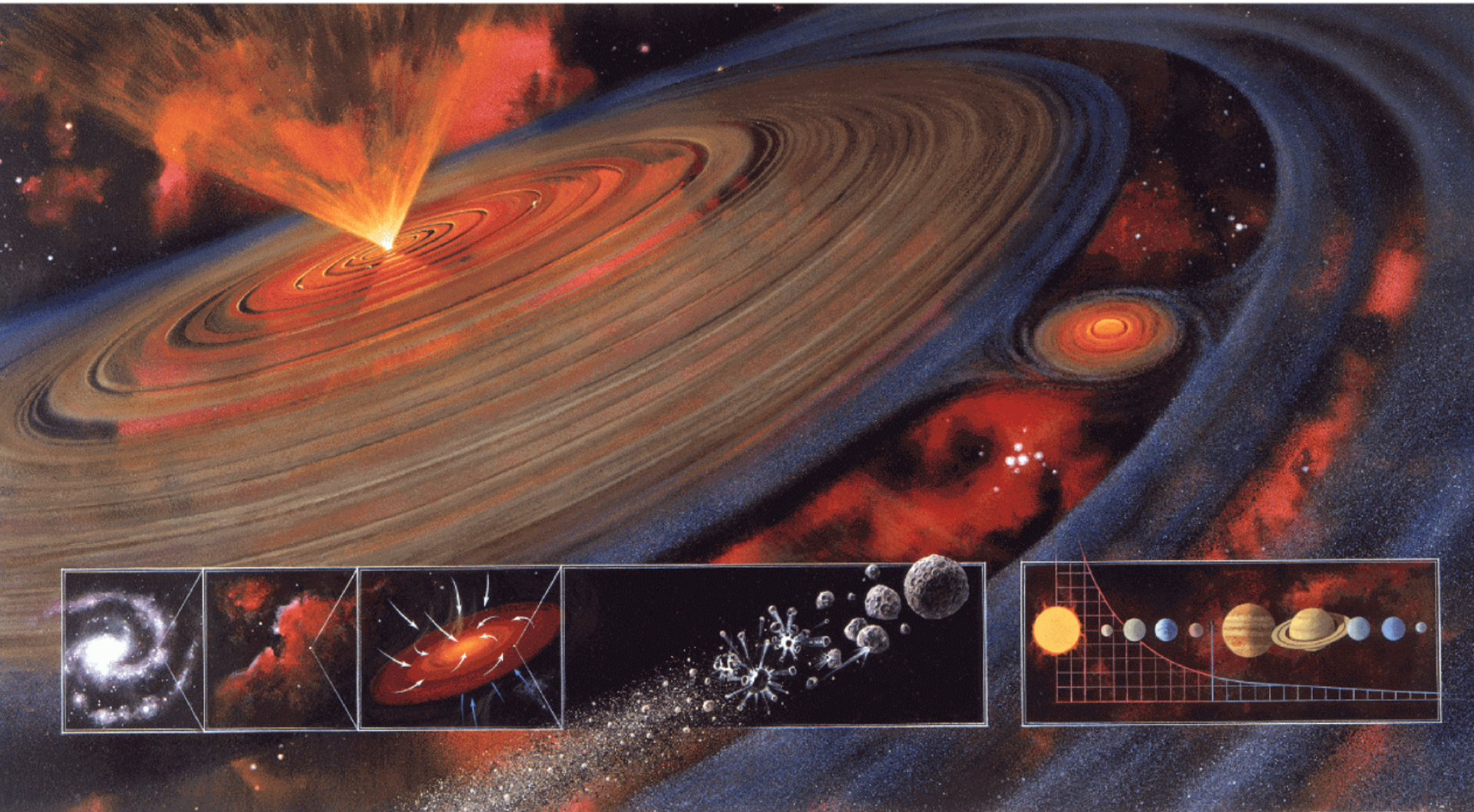
## Observed Properties of Extrasolar Planets Howard (2013)



# Big picture questions

- How did super Earth form so prolifically
- Why is the emergence of gas giant marginal?
- How did planets establish their structural diversity?
- How did planetary systems acquired the observed kinematic distribution?
- How did multiple systems attain meta-stability?

# Conventional core accretion scenario



# Minimum-mass nebula hypothesis

## in situ formation scenario

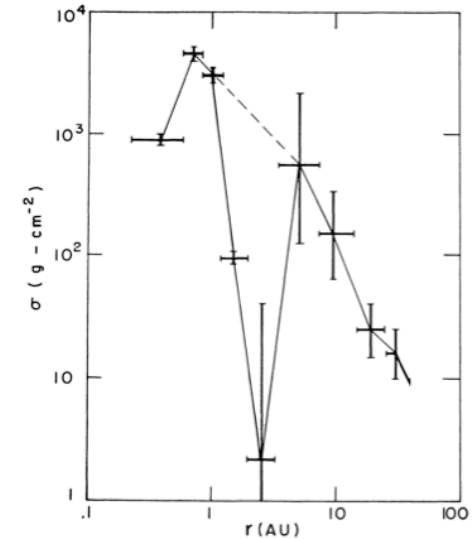
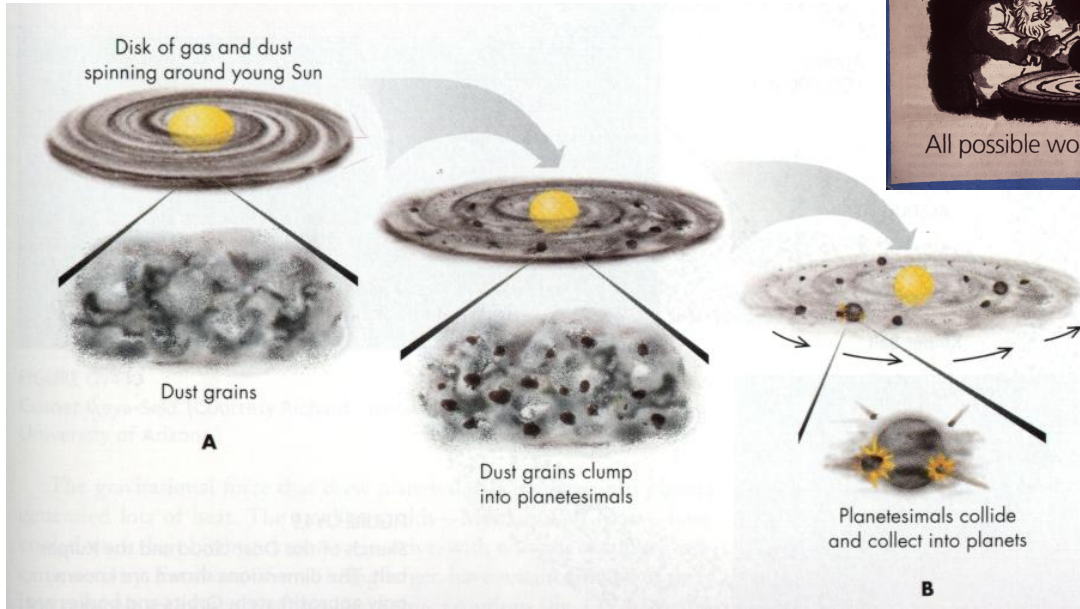
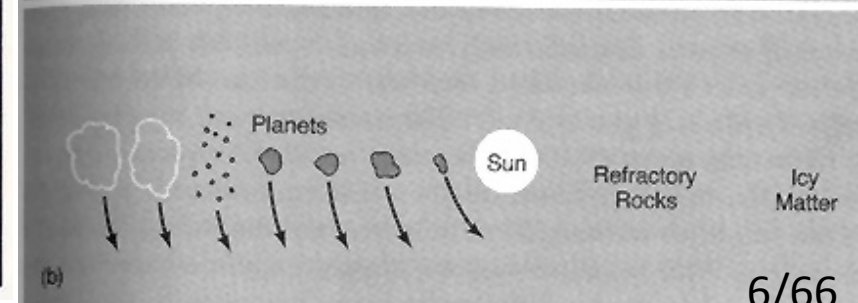
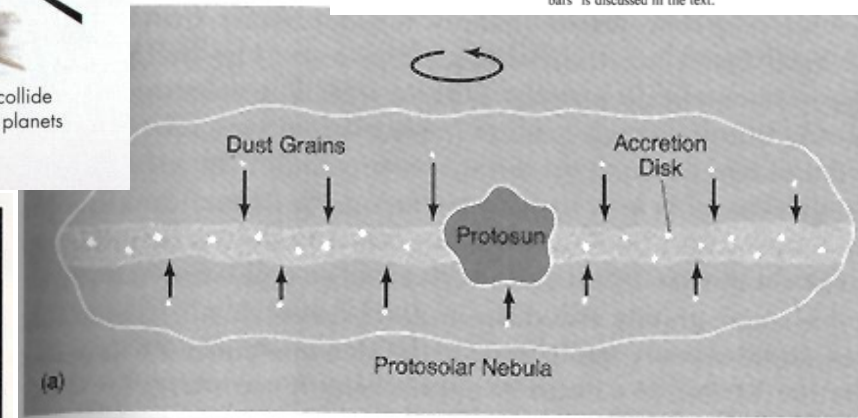
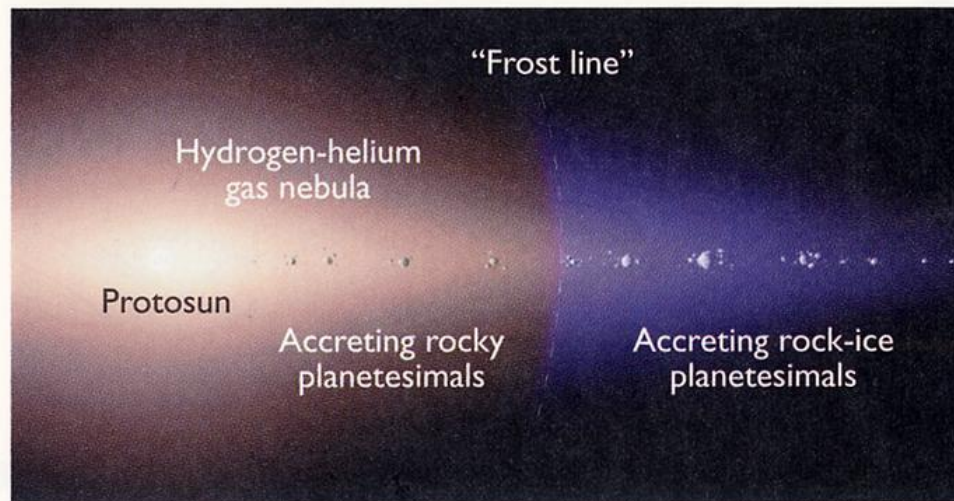


Fig. 1. Surface densities,  $\sigma$ , obtained by restoring the planets to solar composition and spreading the resulting masses through contiguous zones surrounding their orbits. The meaning of the 'error bars' is discussed in the text.



# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

# Meter-barrier: Hydrodynamic drag on dusts

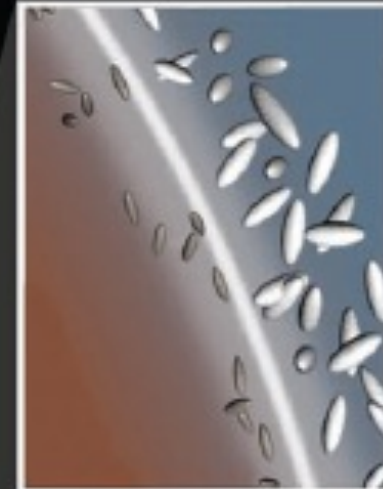
1 Grains collide, clump and grow.



2 Small grains are swept along by the gas, but those larger than a millimeter experience a drag force and spiral in.

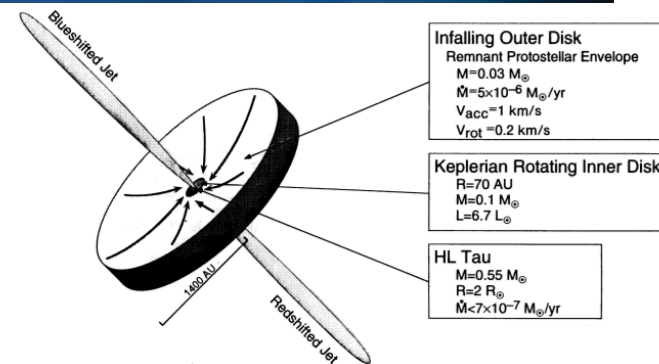


3 At the snow line, local conditions are such that the drag force reverses direction. Grains tend to accumulate and readily coagulate into larger bodies called planetesimals.

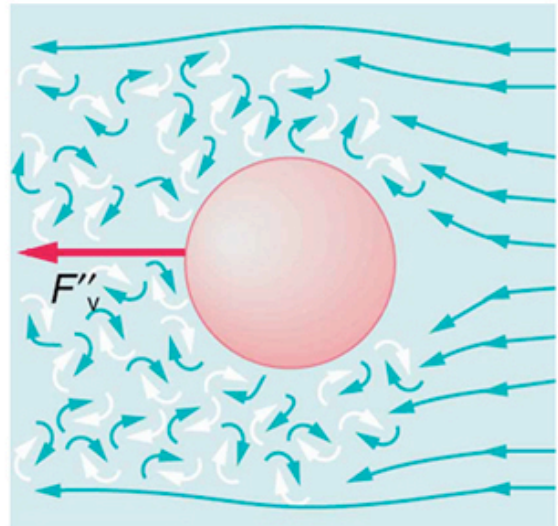
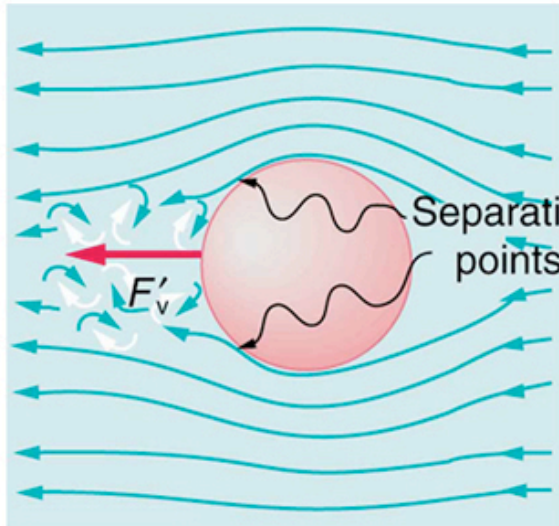
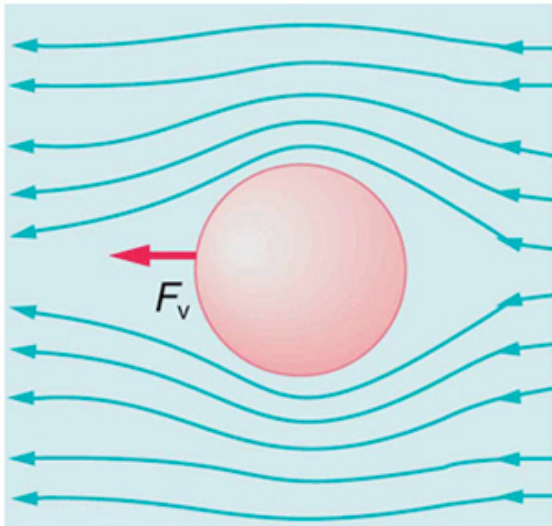
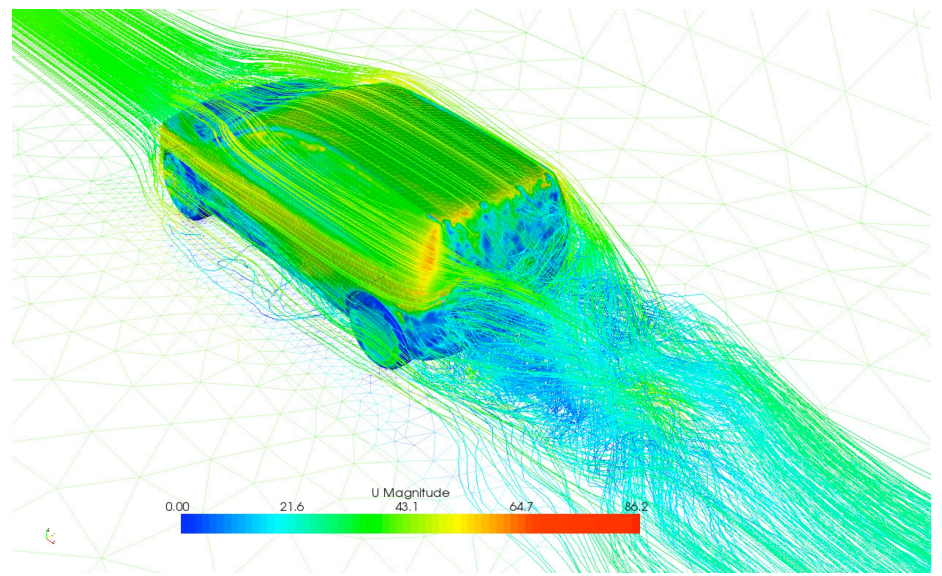
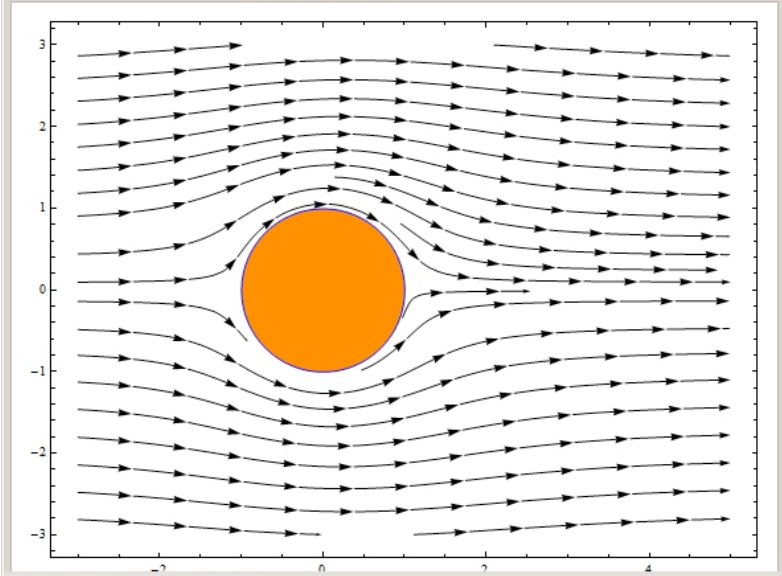


Dust spirals inward

Disk of gas and dust







(a)

$$F_d = m_p \frac{\rho}{\rho_s s} (\mathbf{r} - \mathbf{v}_g) \quad \text{when } s \ll \lambda,$$

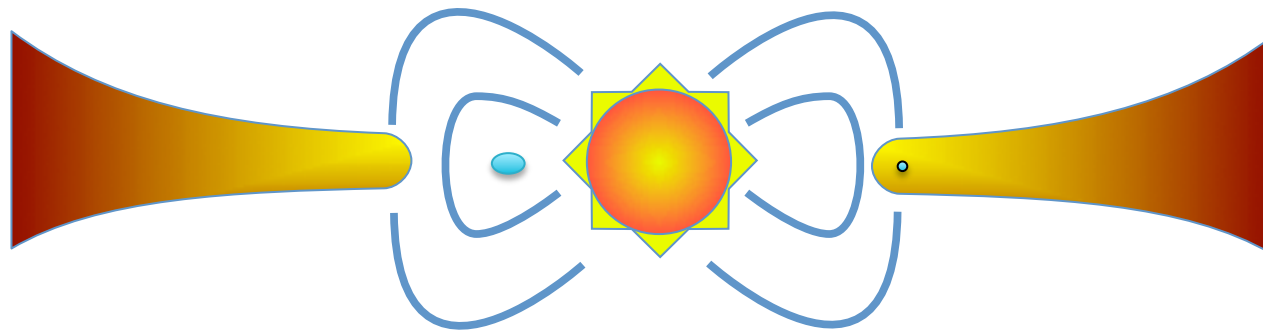
$$F_d = m_p \frac{\rho}{\rho_s} \frac{C(\text{Re})}{s} |\Delta \mathbf{v}| (\dot{\mathbf{r}} - \mathbf{v}_g) \quad \text{when } s \gg \lambda.$$

(b)

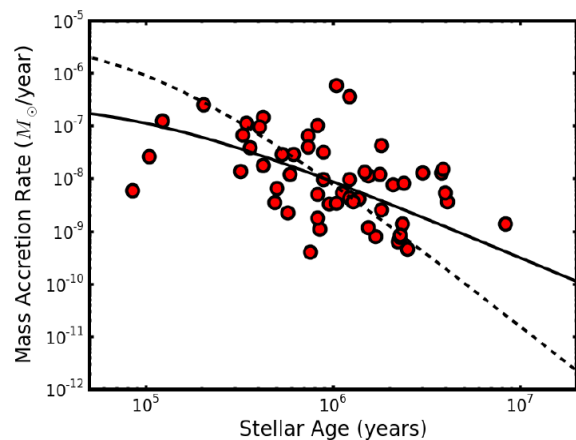
(c)

$$C = \begin{cases} 9\text{Re}^{-1} & \text{for } \text{Re} \leq 1, \\ 9\text{Re}^{-0.6} & \text{for } 1 \leq \text{Re} \leq 800, \\ 0.165 & \text{for } 800 \leq \text{Re}. \end{cases}$$

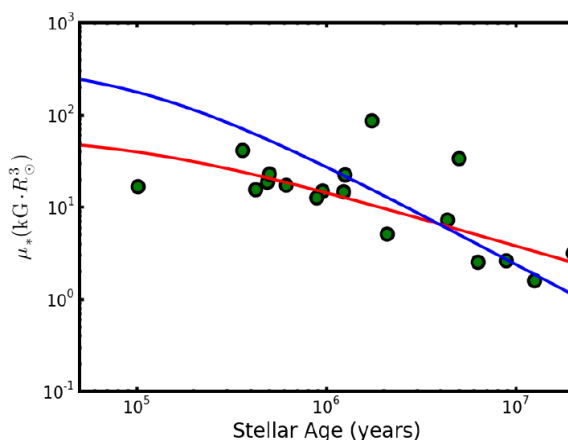
# Stalling of planets inside & at the magnetospheric truncation radius



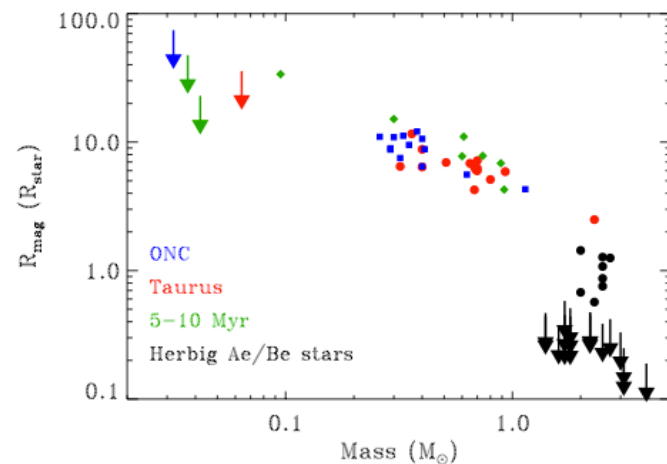
$$r_{\text{mag}} \propto \mu_*^{4/7} \dot{M}^{-2/7}$$



Mass Accretion Rate

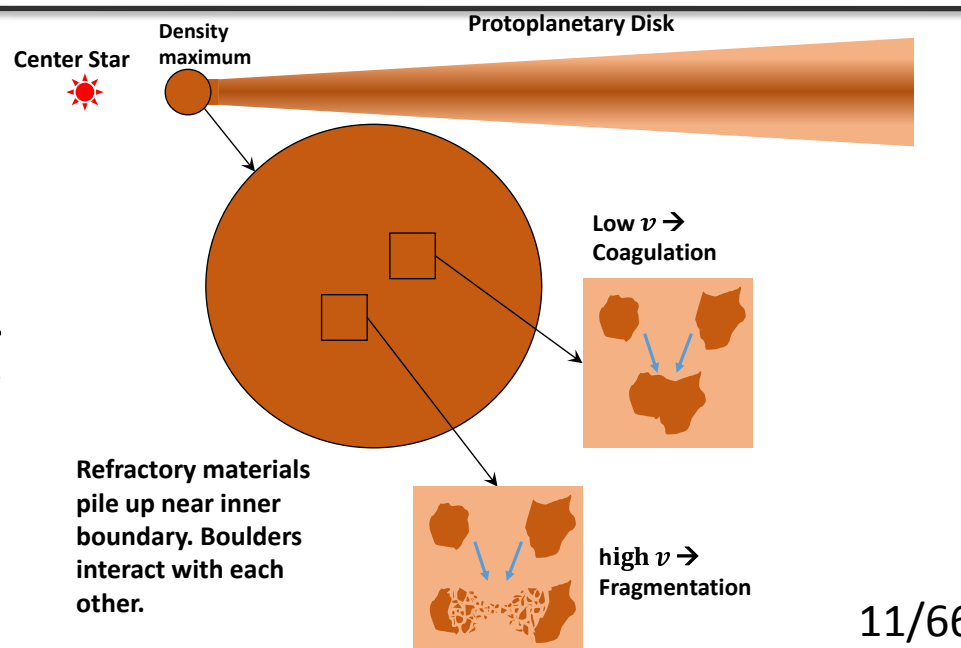
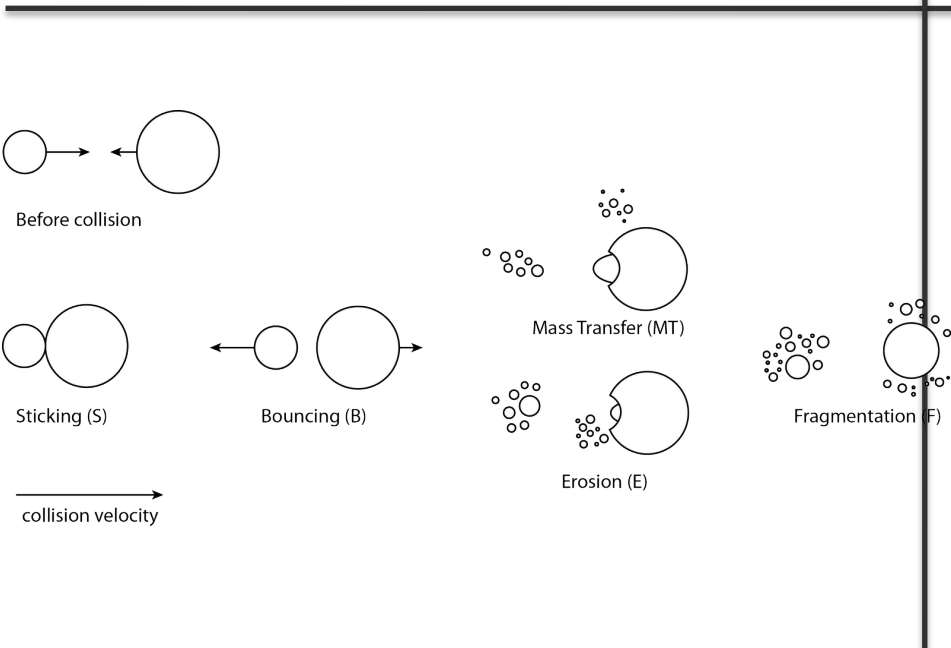
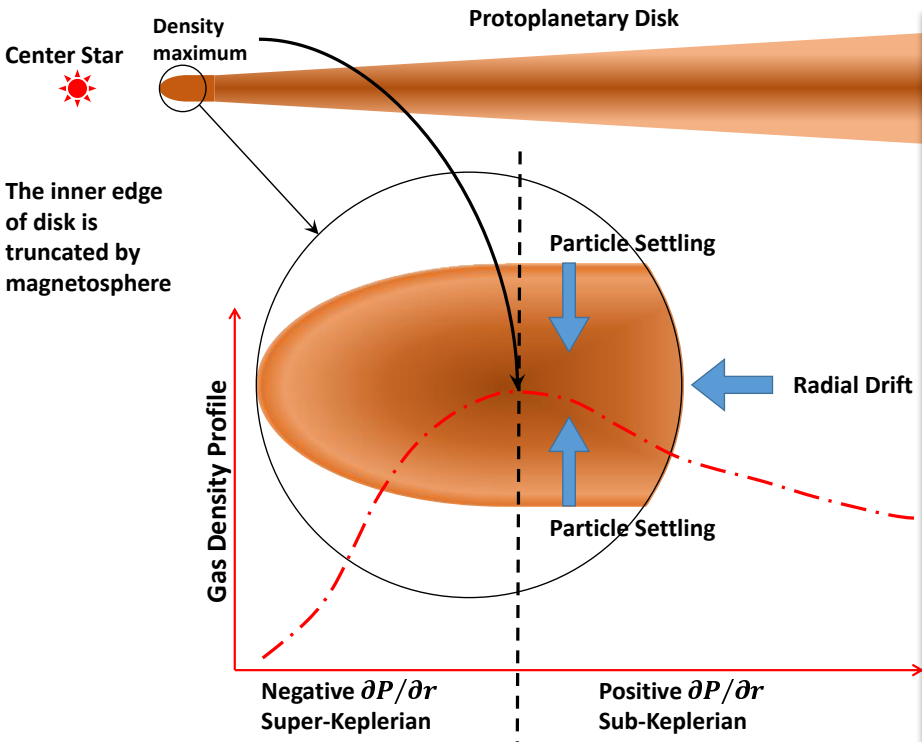


Stellar Dipole Moment



Magnetosphere radius

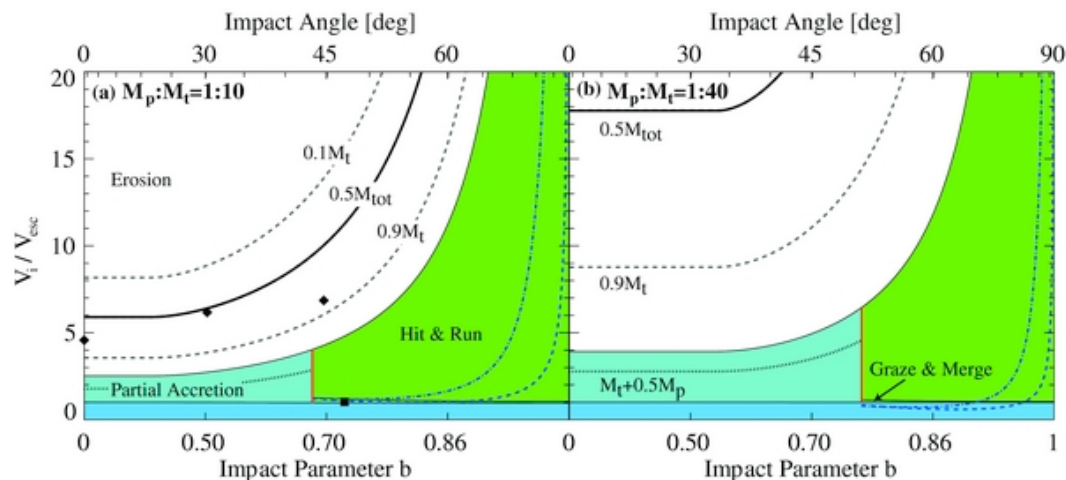
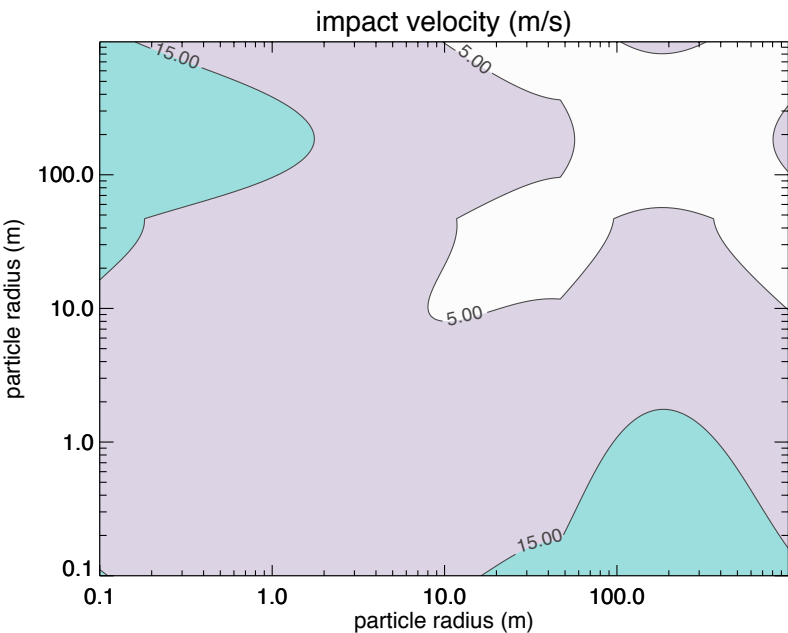
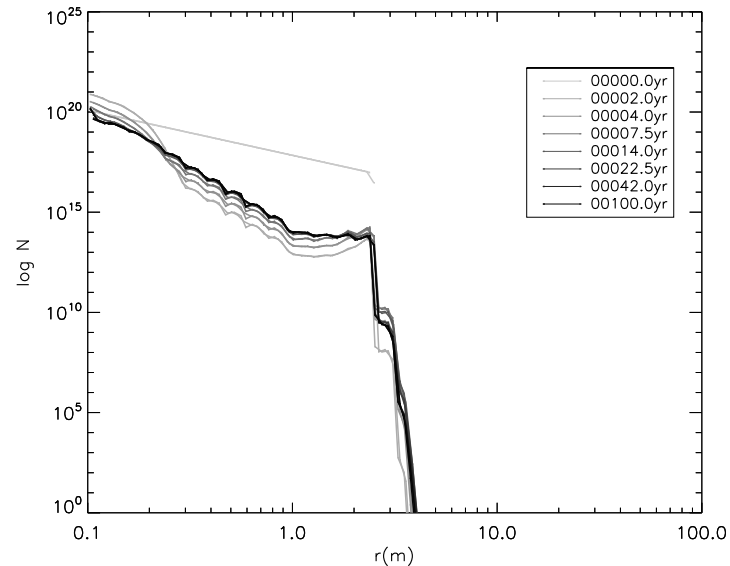
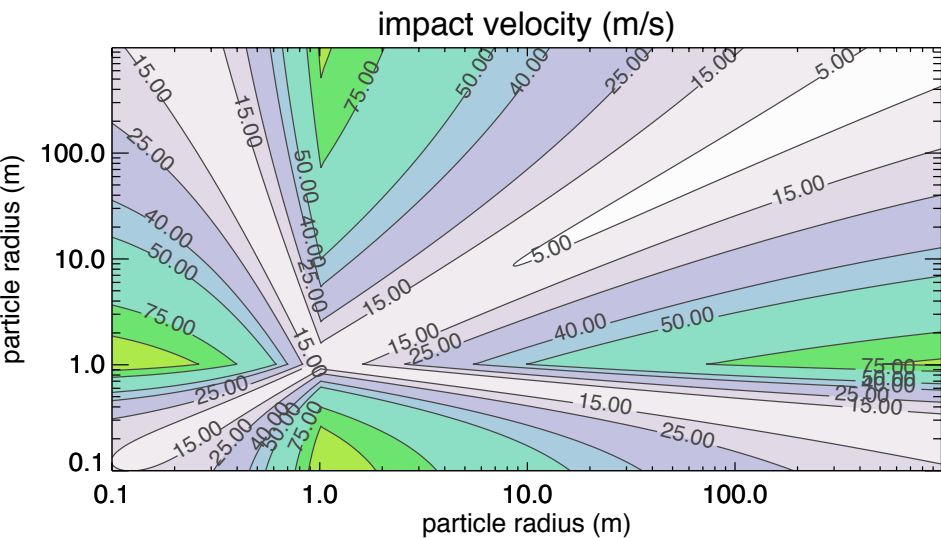
Heczeg



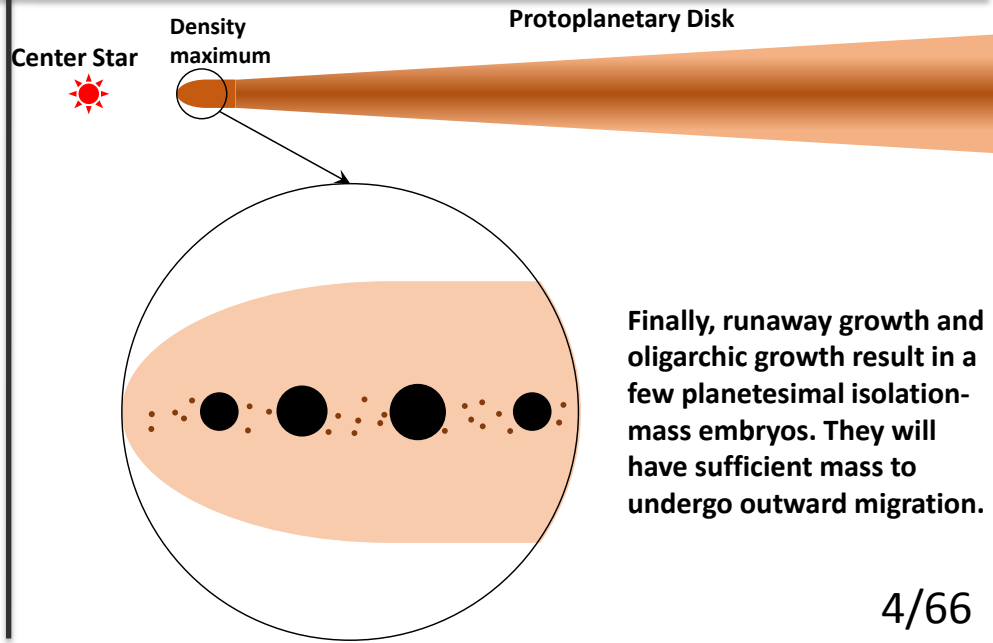
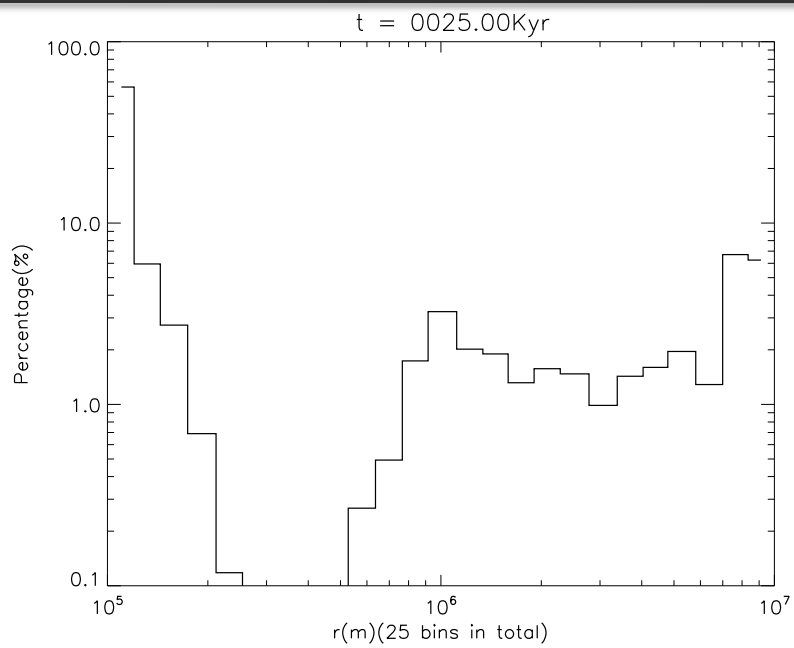
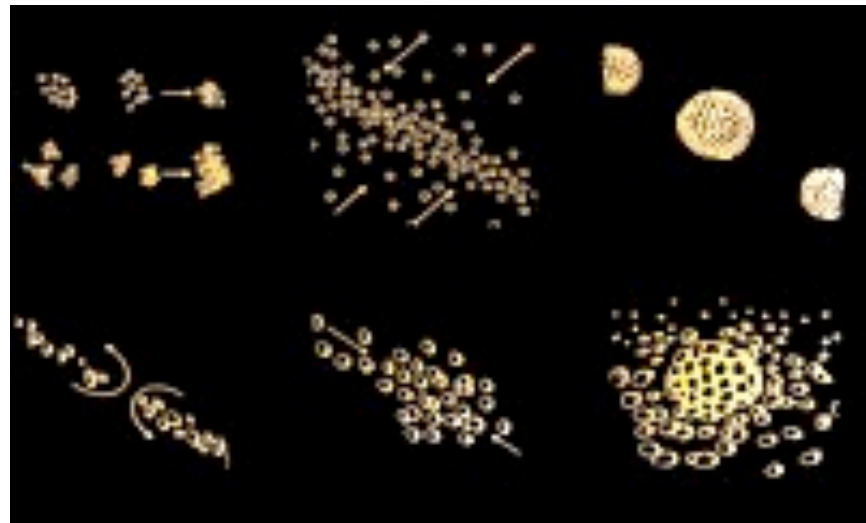
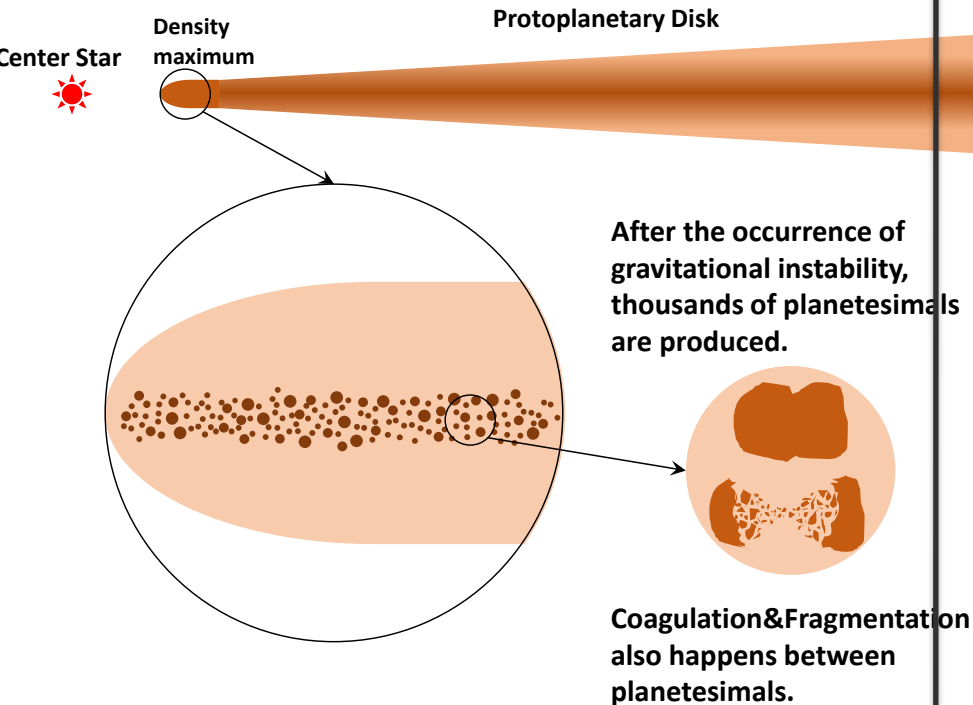
# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- **Fragmentation: km-size barrier (Benz)**
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

# Collisional energy & spectrum



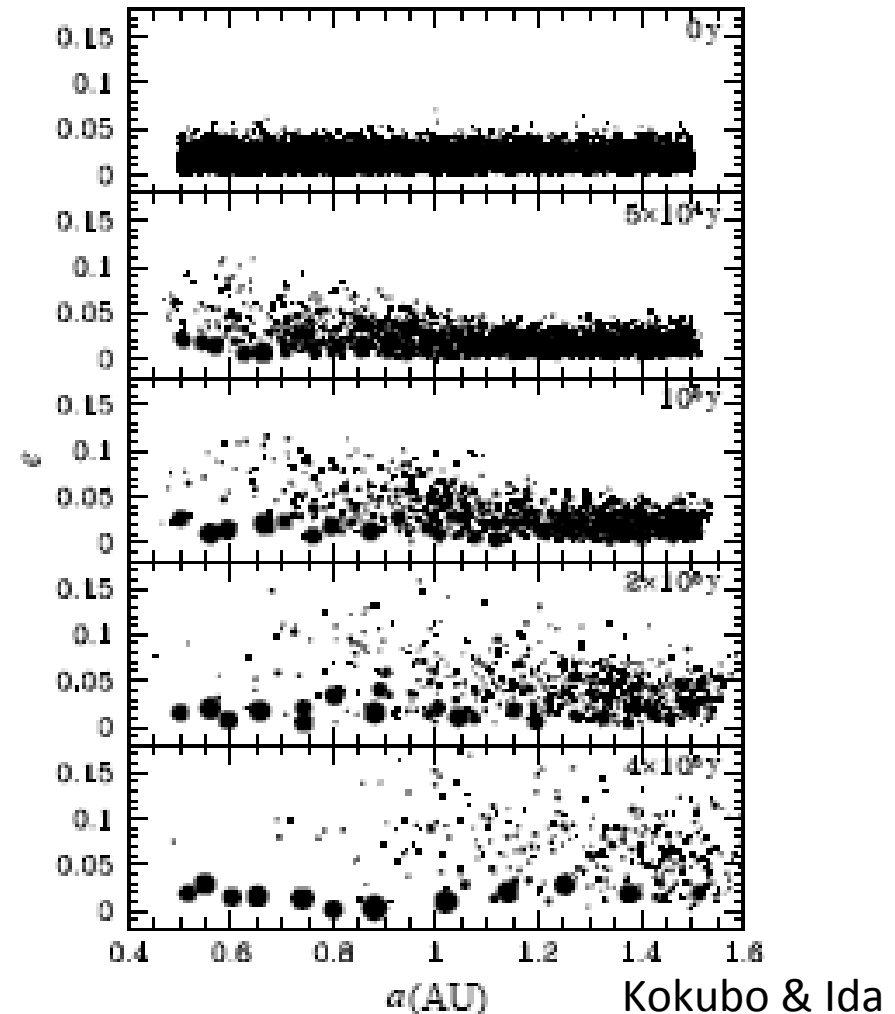
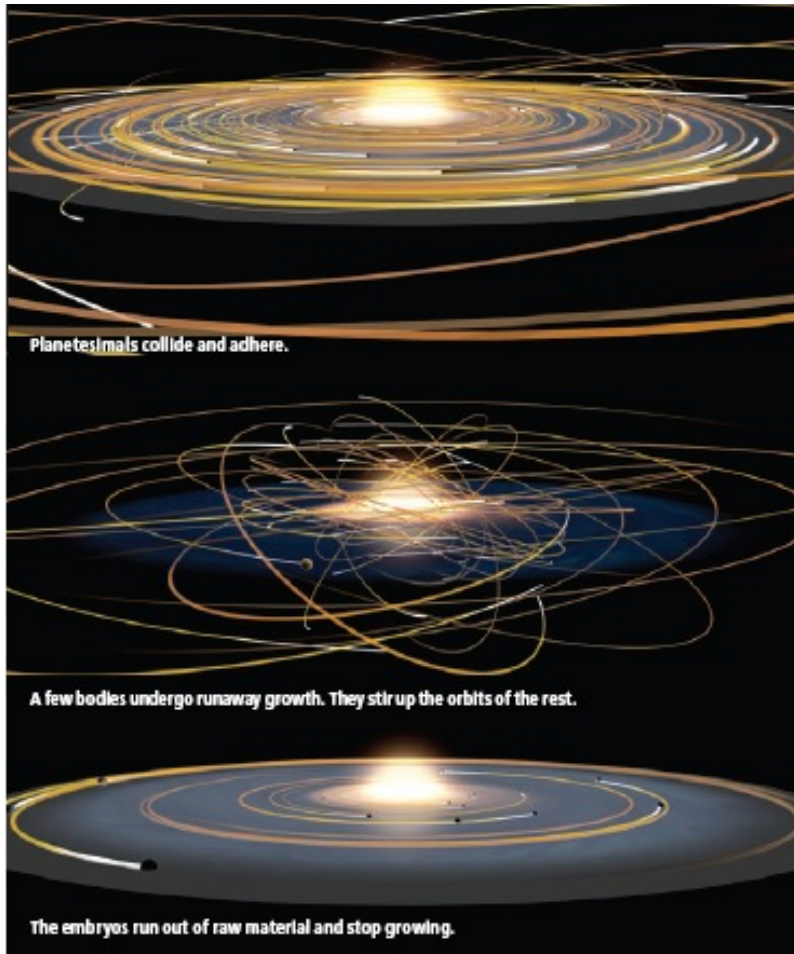
# fragmentation vs gravitational instabilities



# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

# Step III, oligarchic barrier: Isolation mass



Feeding zones:

$$\Delta \sim 10 r_{\text{Hill}}$$

**Isolation mass:**

$$M_{\text{isolation}} \sim \Sigma^{1.5} a^3 M_*^{-1/2}$$



# Equi-potential surface and Roche lobe

Energy & angular momentum are not conserved.

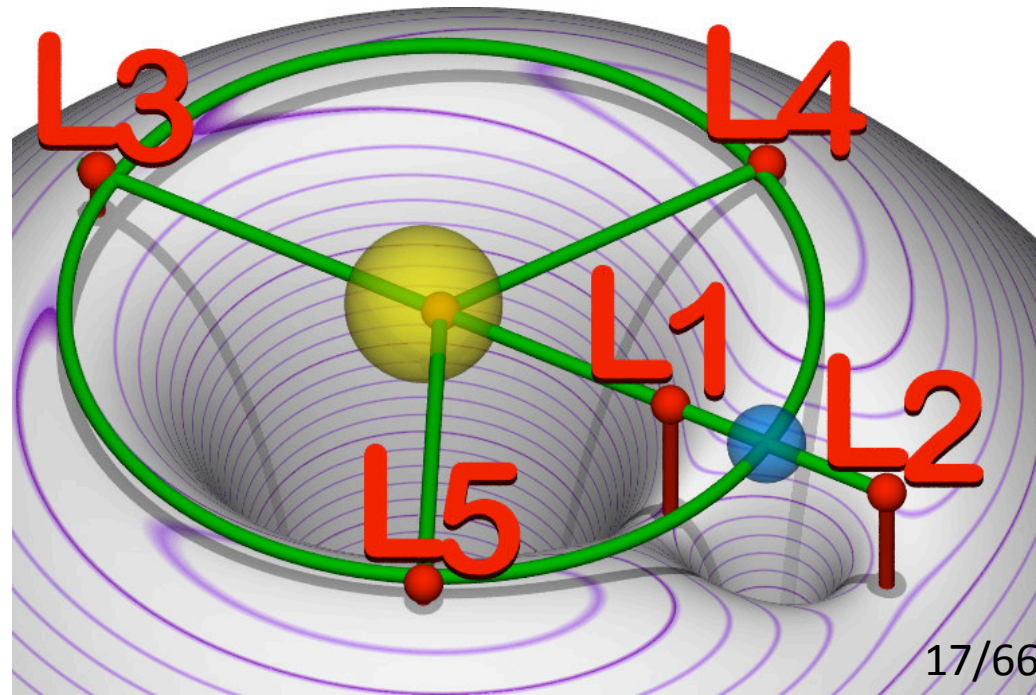
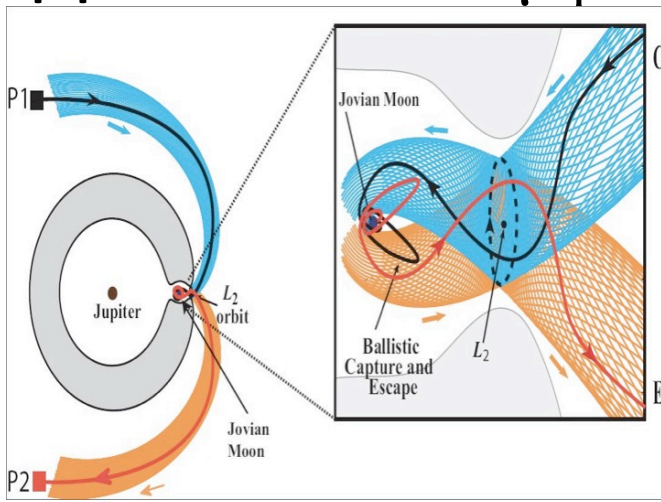
Conserved quantity: Jacobi "energy" Integral

$$C_J = n^2(x^2 + y^2) + 2(\mu_1/r_1 + \mu_2/r_2) - (x^2 + y^2 + z^2)$$

Roche radius: distance between the planet and  $L_1$

$$r_R = (\mu_2/3\mu_1)^{1/3} a_{12} \text{ (to first order in } \mu_2/\mu_1)$$

Hill's equation is an approximation  $\mu_1 = 1$

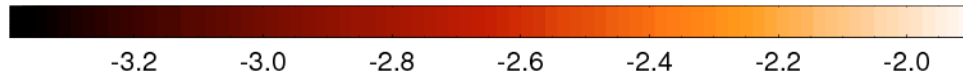


# Some major Challenges:

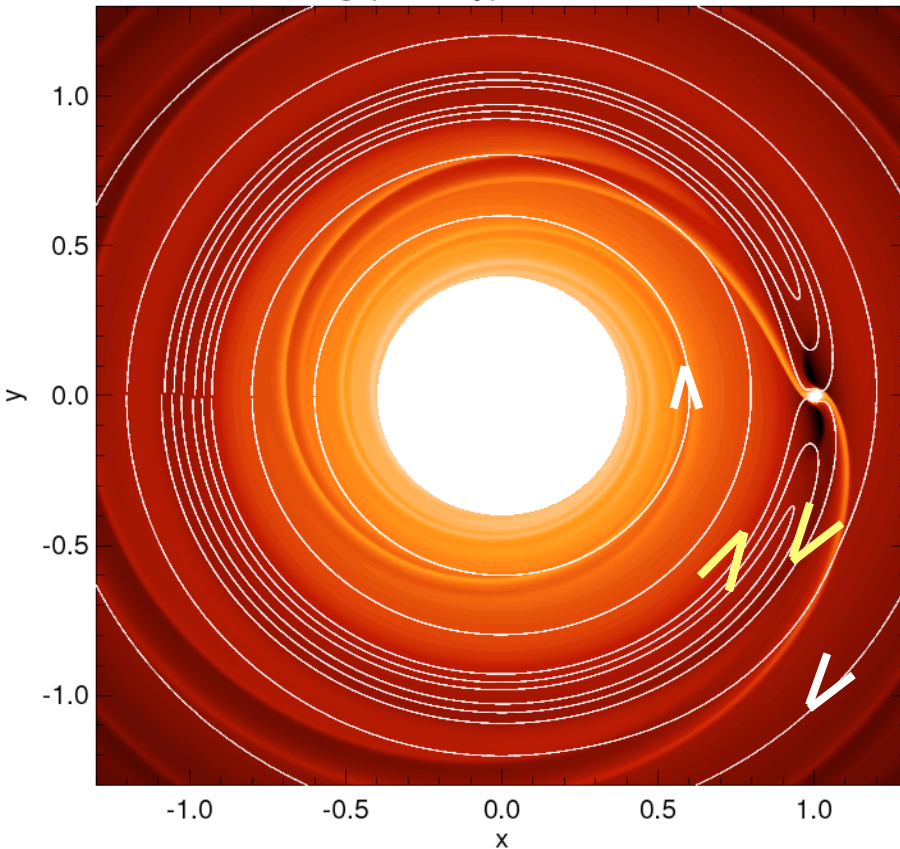
- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- **Retention of embryos: type I migration (Goldreich, Tremaine, Ward)**
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

# Embryos barrier: planetary migration

## Type I migration of super-Earth in isothermal disks

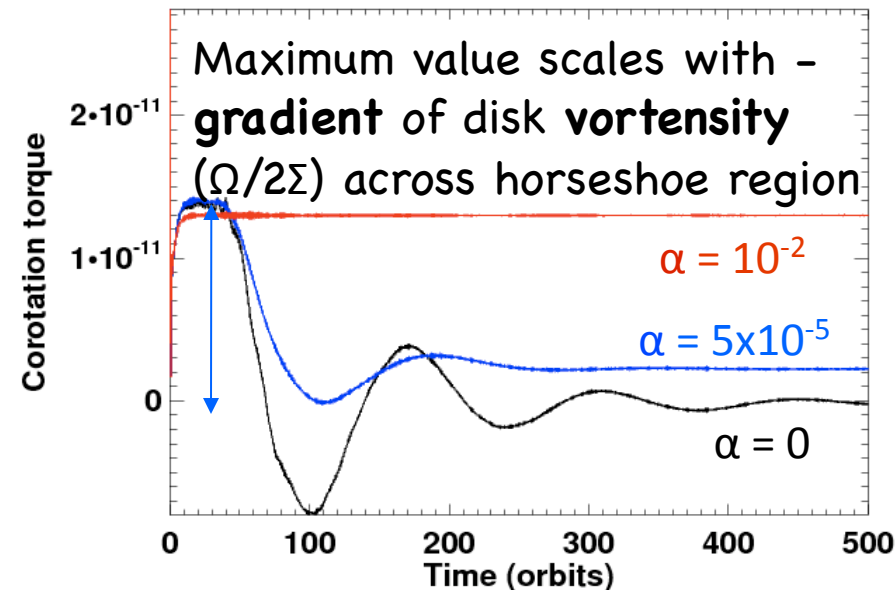


Log (Density) at  $t = 20T_{\text{orb}}$



The planet exchanges angular momentum with:

- **circulating** fluid elements:  
→ differential Lindblad torque
- **librating** fluid elements:  
→ **corotation torque**



e.g. Goldreich & Tremaine (1980), Ward (1992)  
Masset (2001), Paardekooper, Baruteau, Kley

Long-term evolution of the corotation torque is related to the disk viscosity  
Paardekooper, Baruteau.

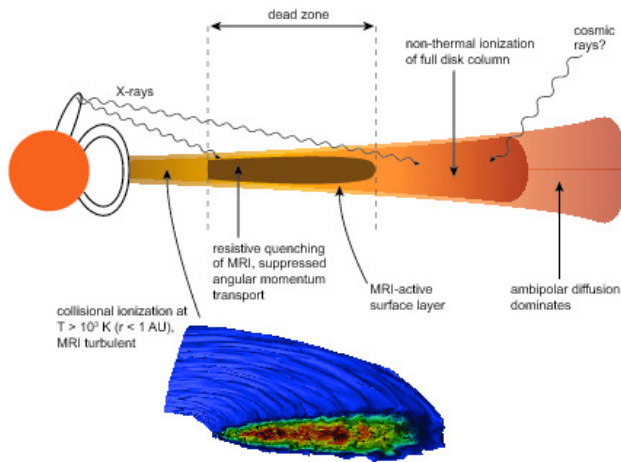
# Planet-disk tidal interaction

Total tidal torque:

$$\Gamma = \Gamma_L + \Gamma_c = f(p, q, p_v, q_v, p_K, q_K) \Gamma_0$$

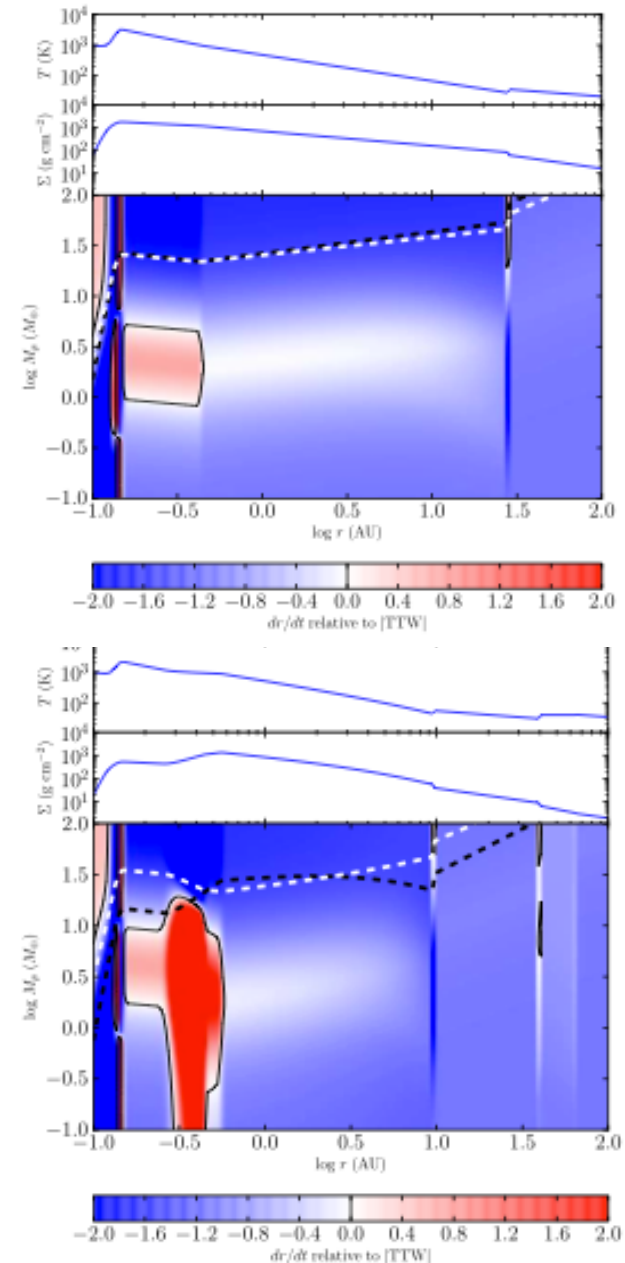
$$\Gamma_0 = (q/h)^2 \Sigma_p r_p^4 \Omega_p^2$$

$p$  and  $q$  depend on disk structure &  $p_v, q_v, p_K,$  and  $q_K$  also depend on  $m_p$



$$\frac{dr}{dt} = f(p, q, p_v, p_K) \frac{M_p}{M_*} \frac{\Sigma r^2}{M_*} \left( \frac{r \Omega_K}{c_s} \right)^2 r \Omega_K$$

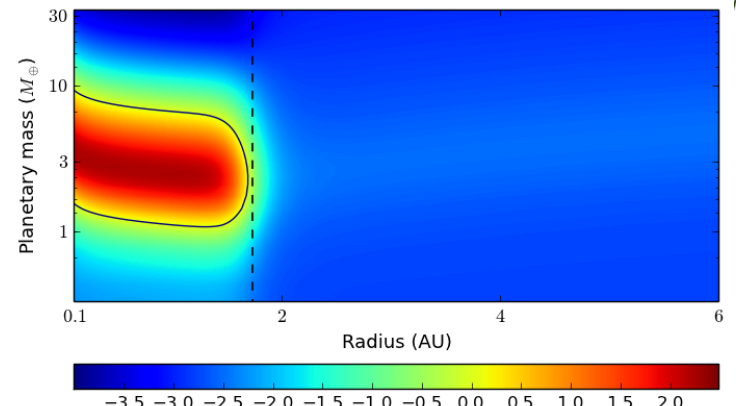
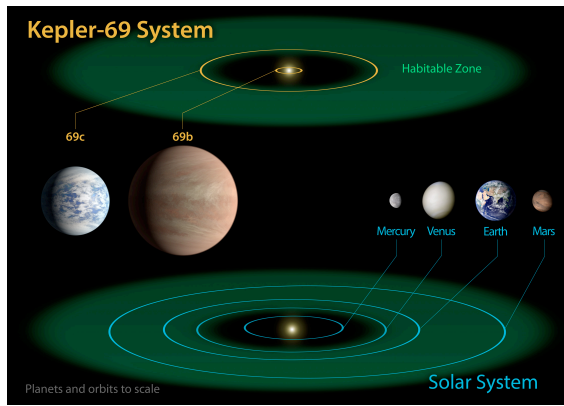
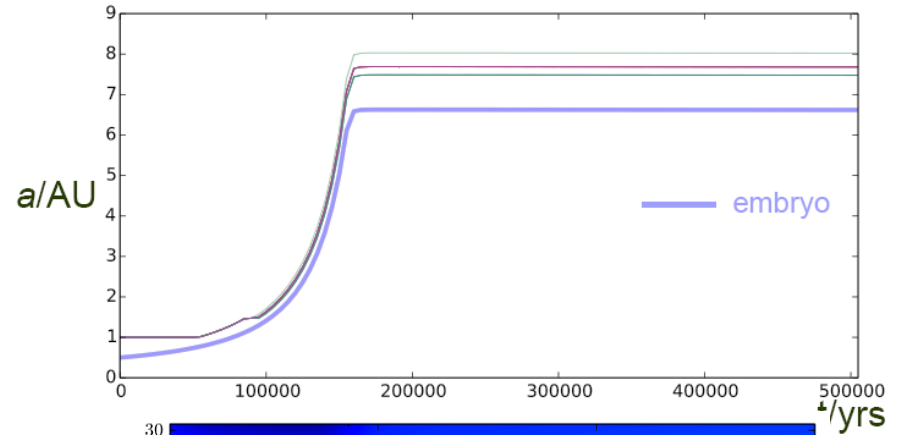
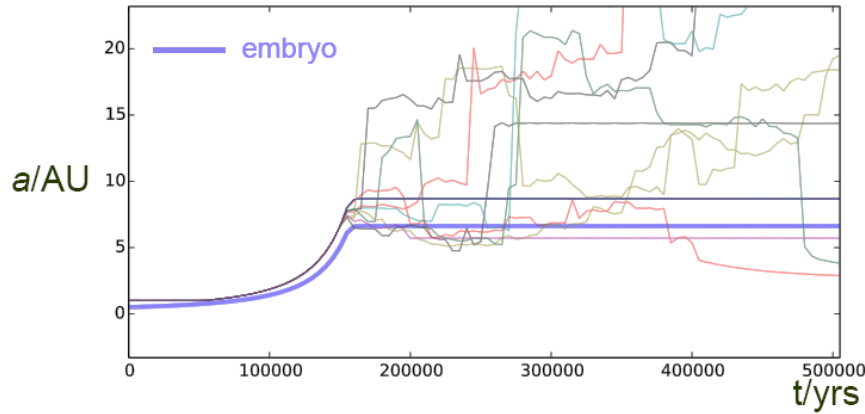
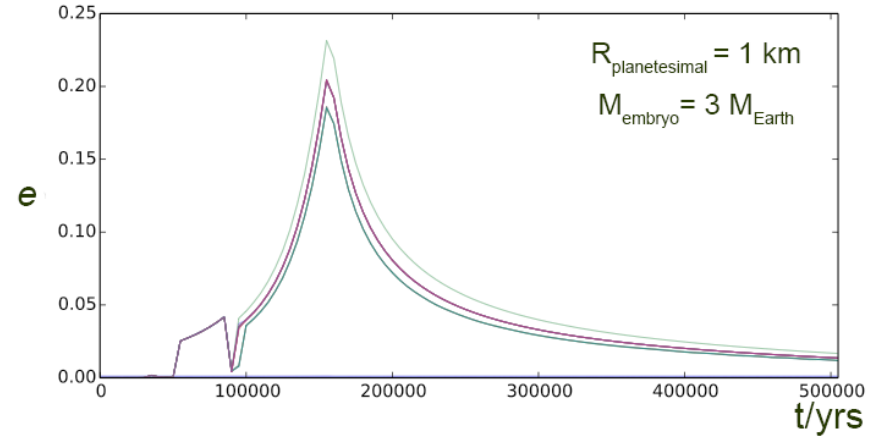
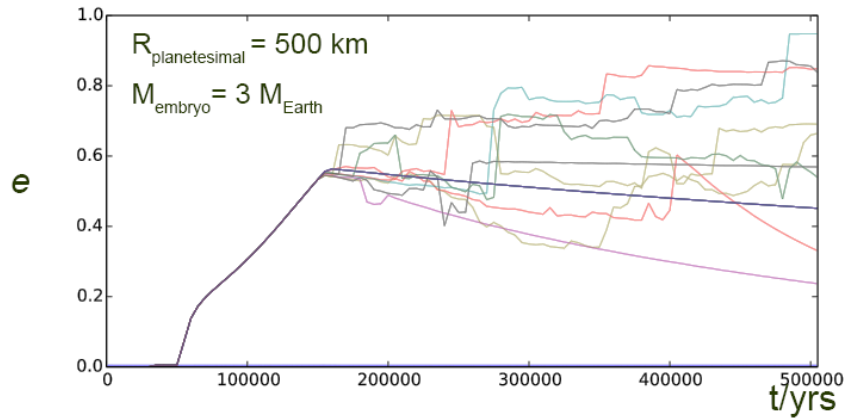
$$(1/e) de/dt = (a/H)^4 (M_p \Sigma a^2 / M_*^2) \Omega$$



# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- **Proliferation of multiple, widely spread embryos**
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

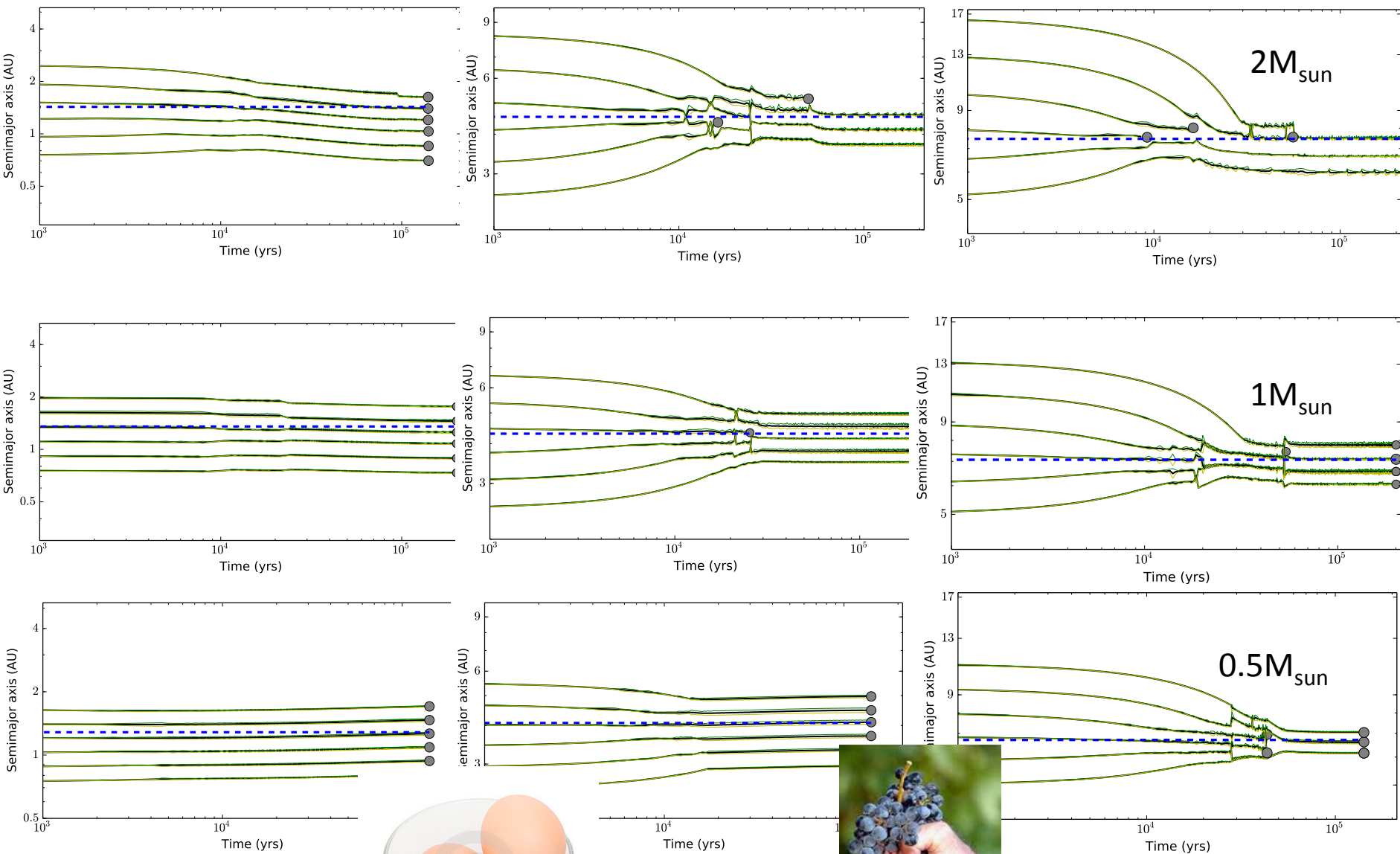
# Resonant sweeping of planetesimals



# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- **Diversity of planetary architecture**
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

# Dependence on the disks' accretion rate



$\dot{M} = 10^{-8}$

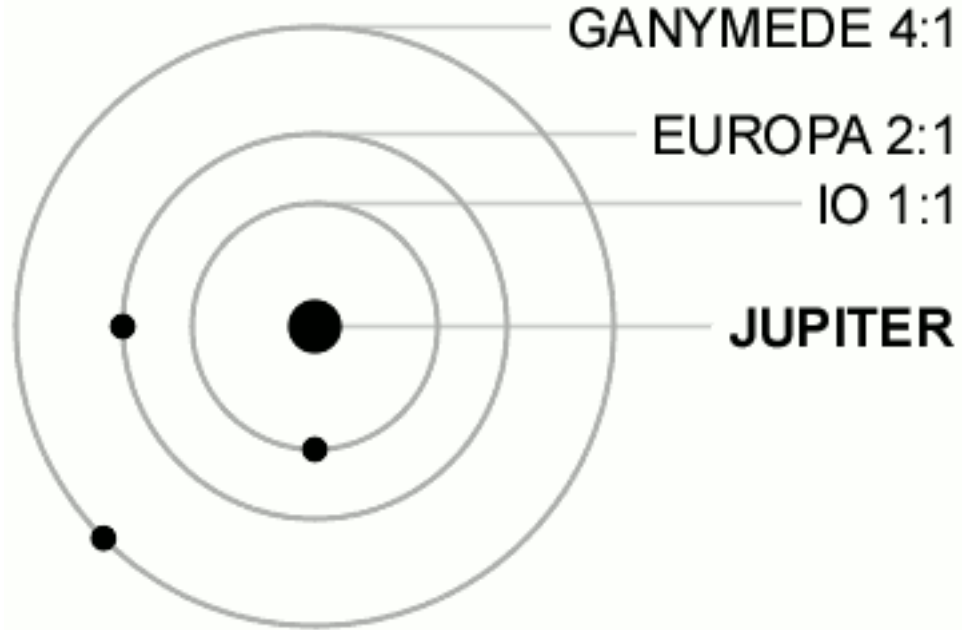
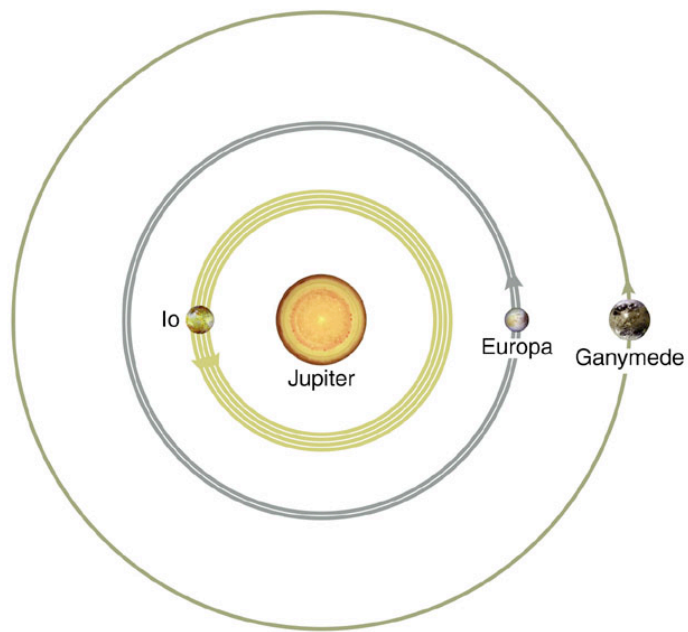


$5 \times 10^{-8}$

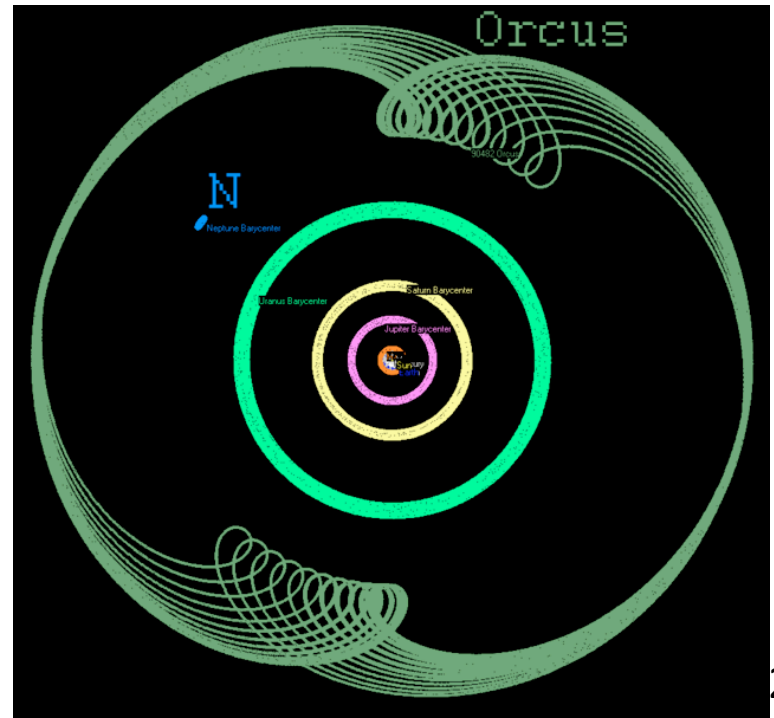
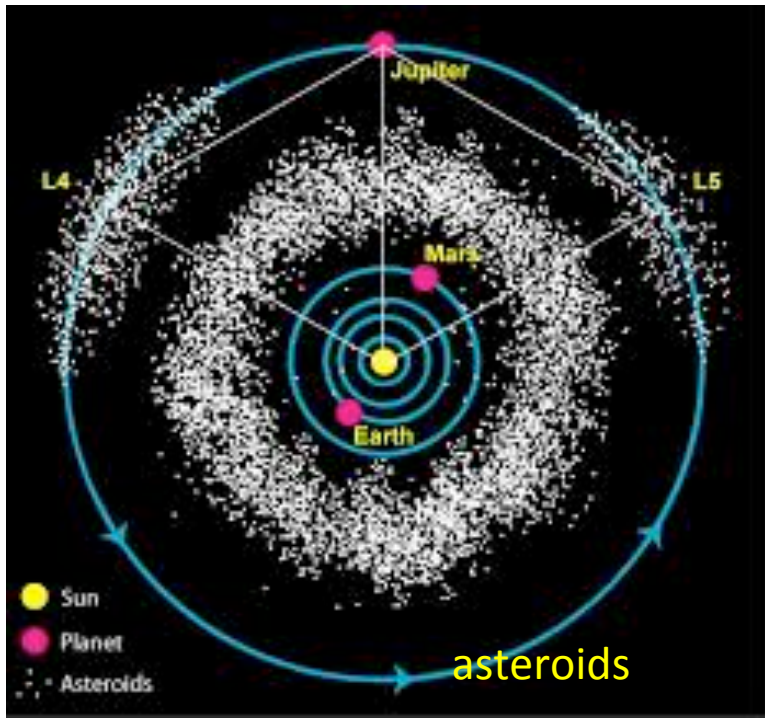


$10^{-7}$



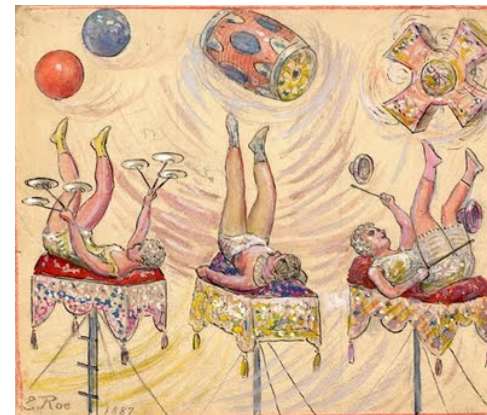
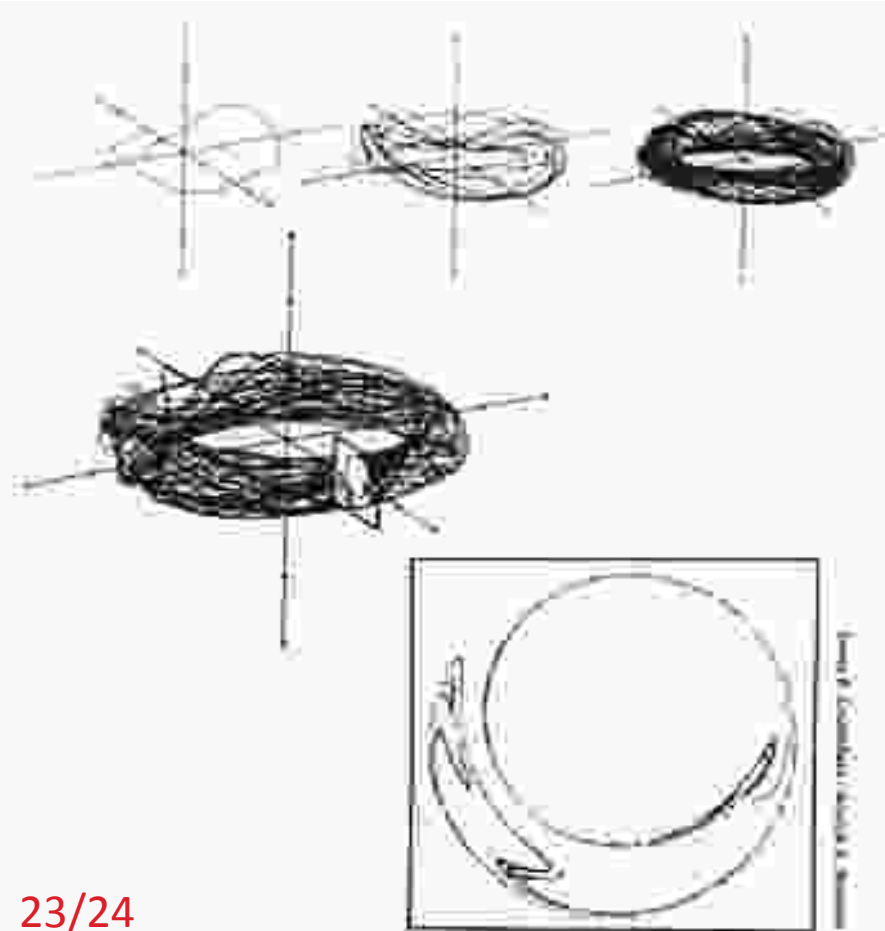
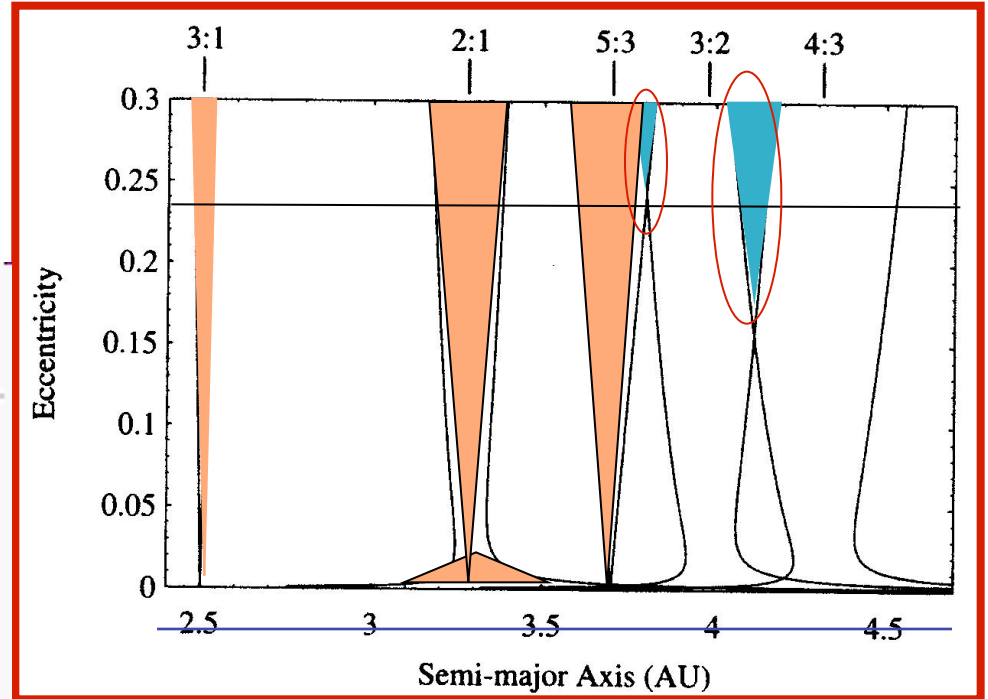


Copyright © 2004 Pearson Education, publishing as Addison Wesley.

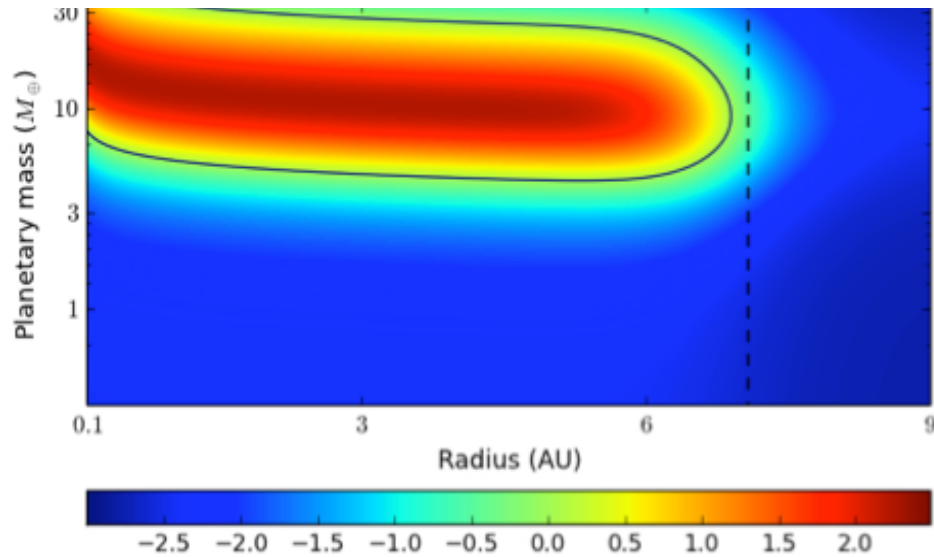
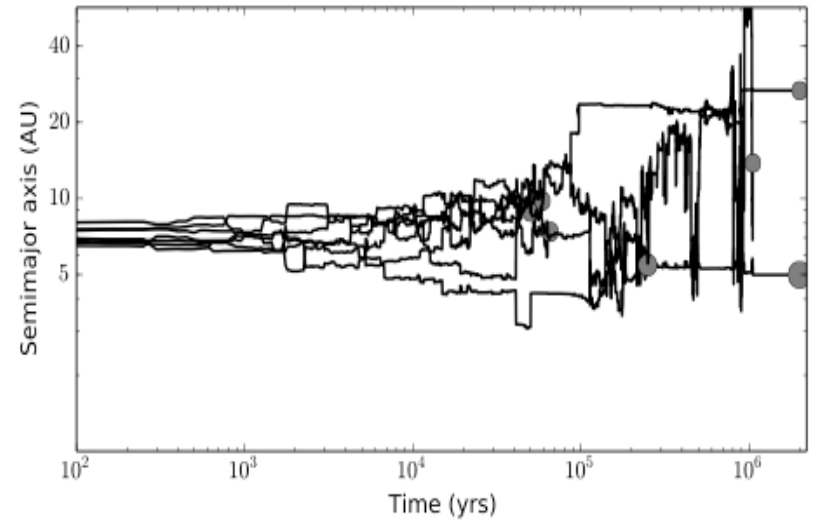
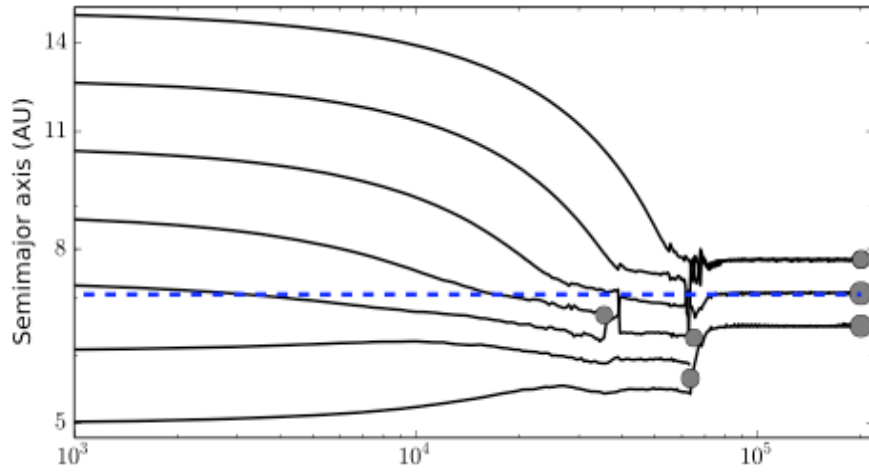


# Overlapping resonances & dynamical instability

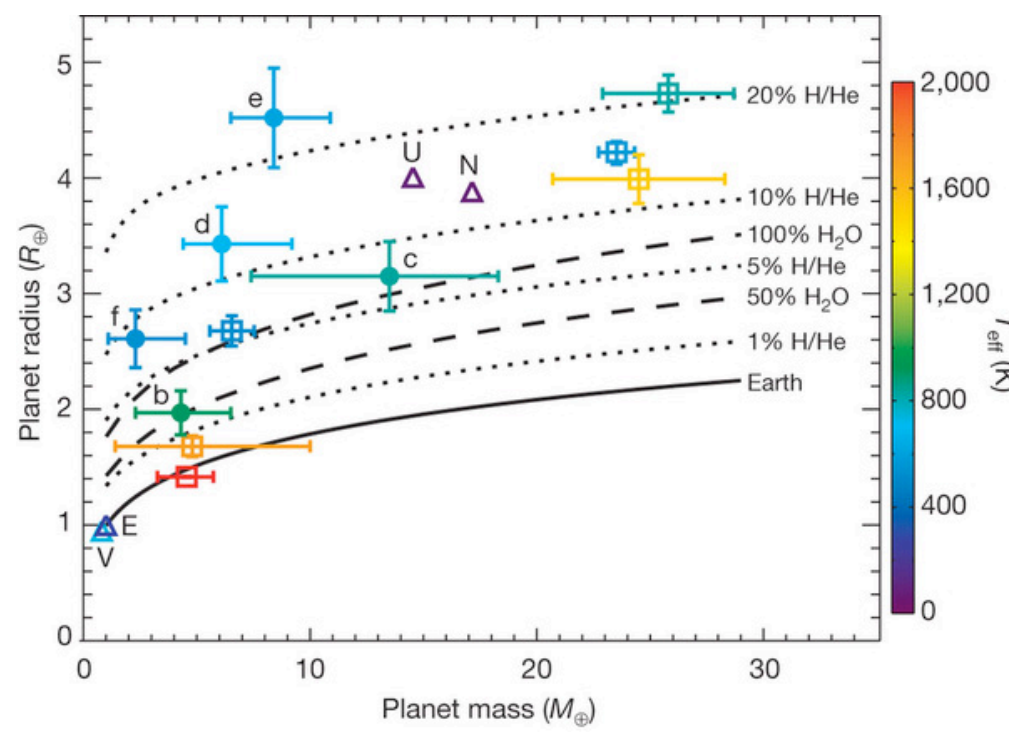
Dynamical filling factor & gas damping



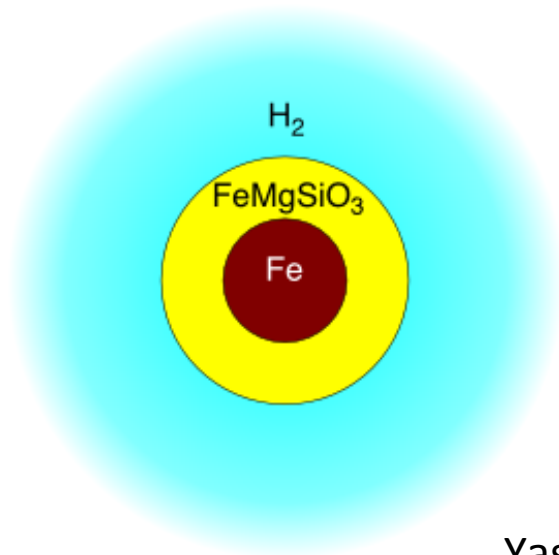
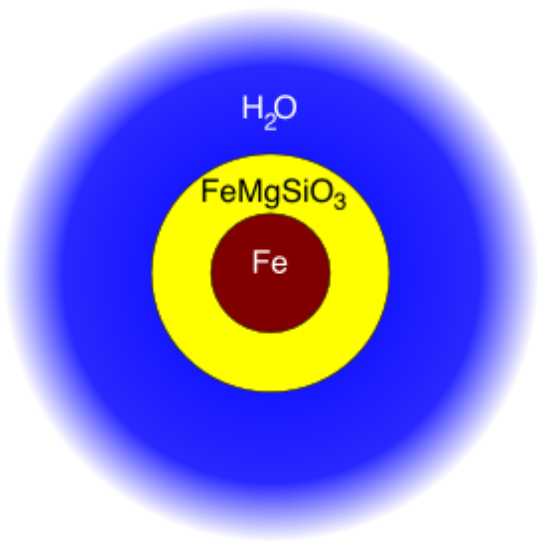
# Bypass the resonance barrier

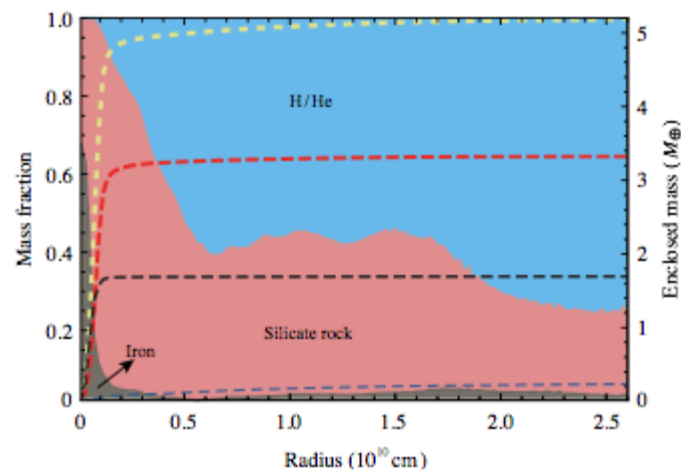
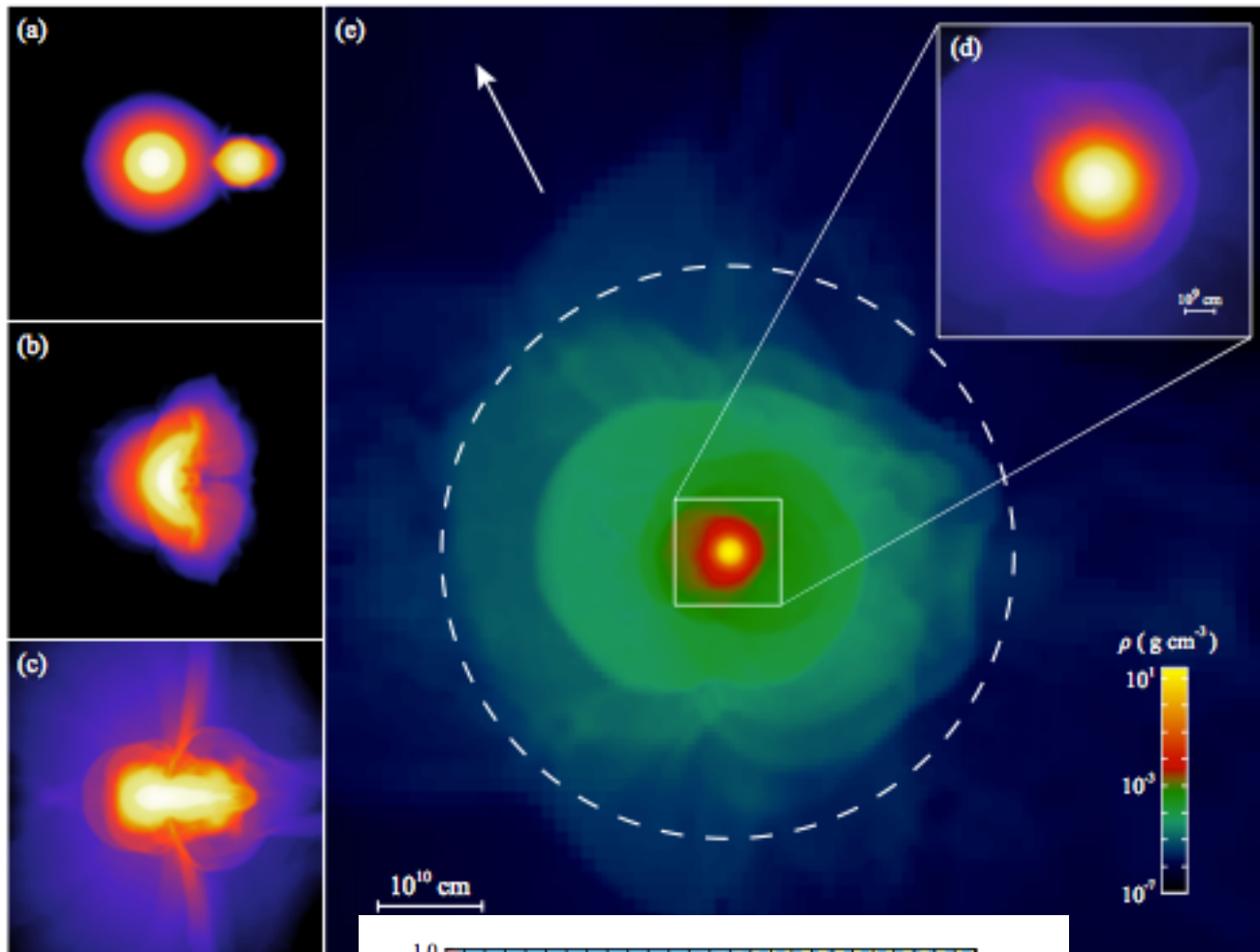


27/66  
Orbit crossing, close encounters, home coming & collisions



Eric Lopez, Angie Wolfgang





# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- **Onset of efficient gas accretion (Pollack, Bodenheimer)**
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

# Gas accretion barrier:

- Is there a threshold mass for gas accretion?

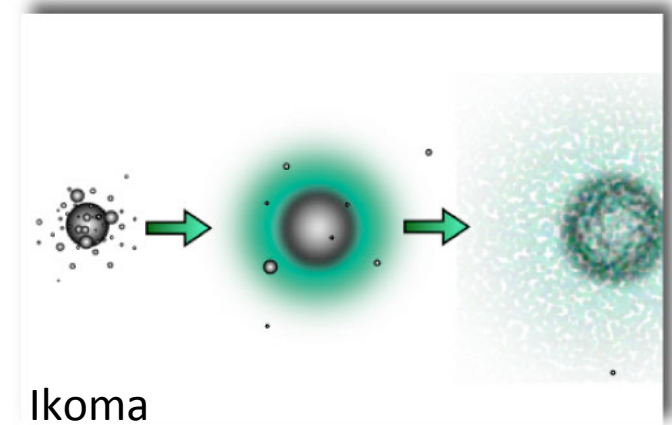
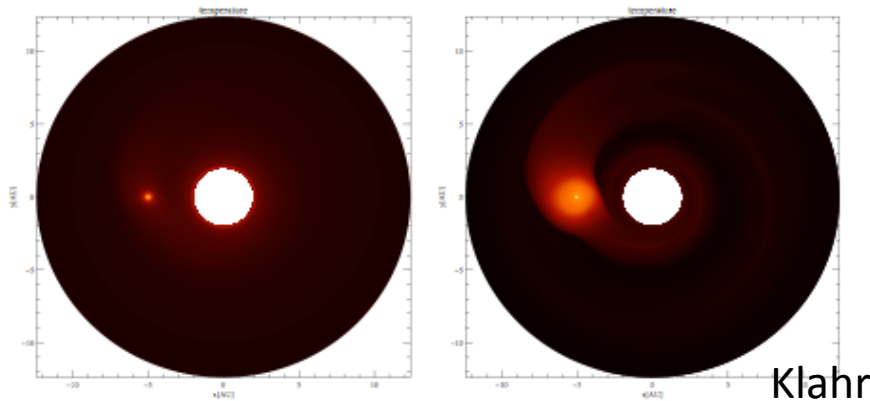
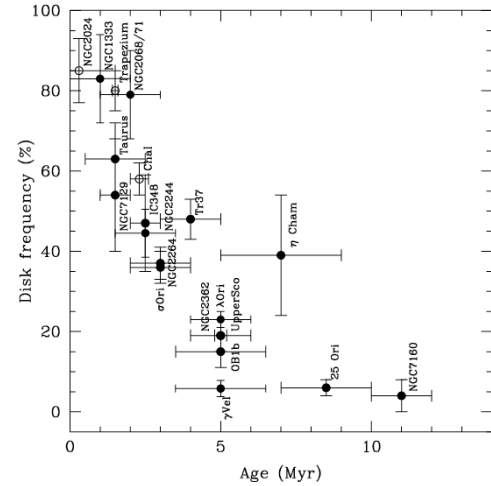
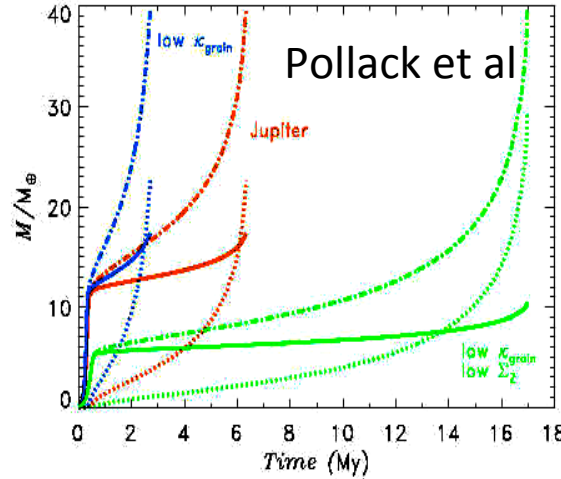
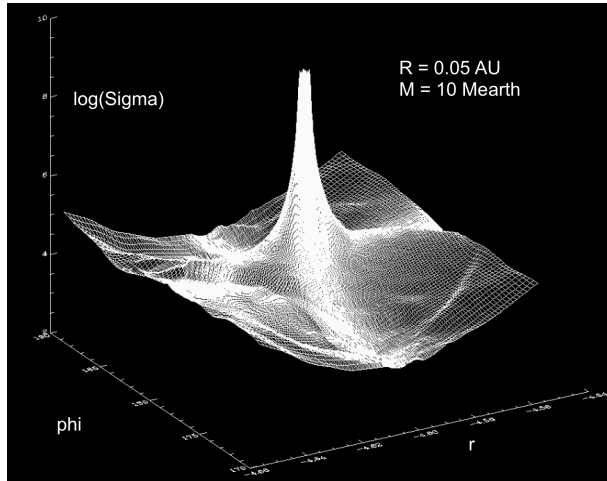
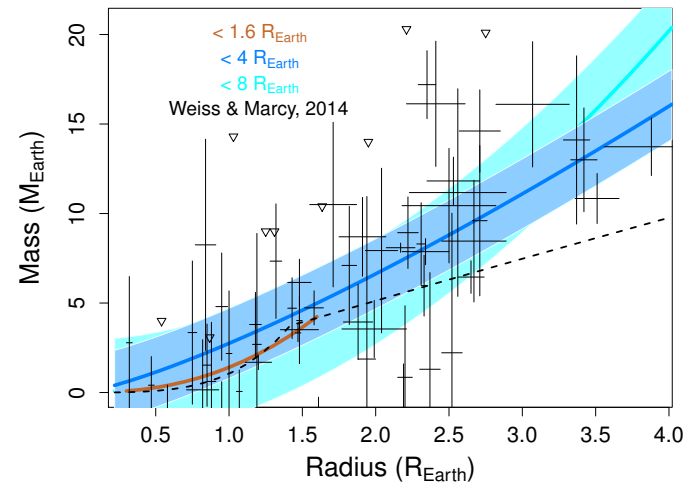
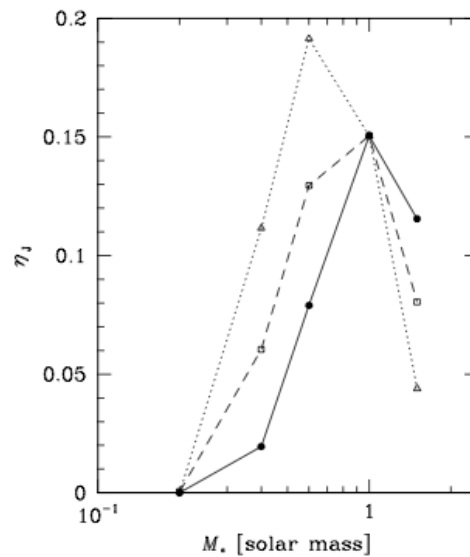
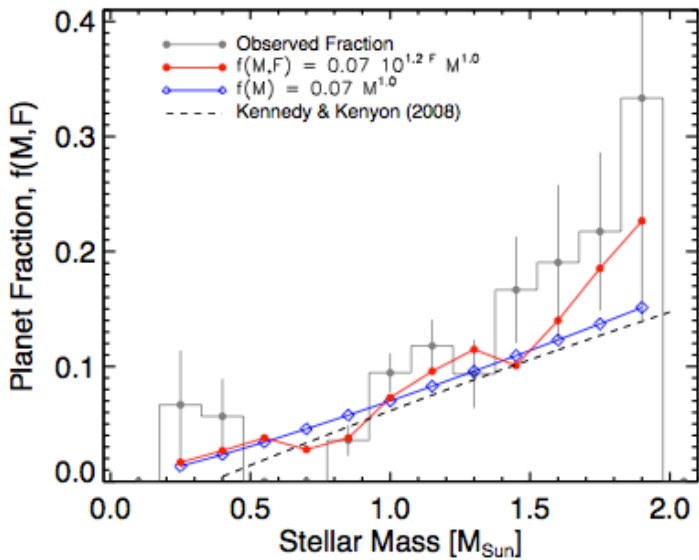


Fig. 4.— Temperature distribution - left:  $30M_{\odot}$  and  $\kappa = 0.01\kappa_0$ ; right:  $30M_{\odot}$  and  $\kappa = 1\kappa_0$

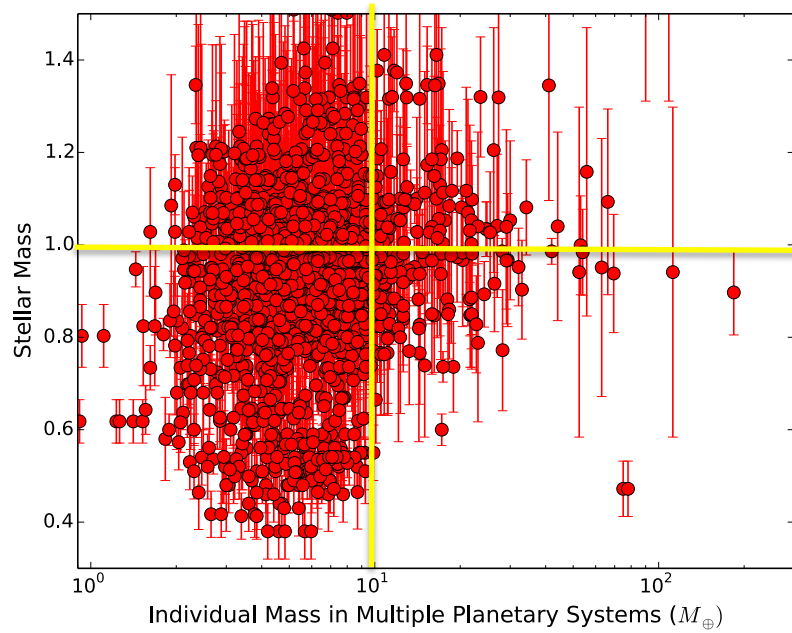
# Radiation transfer & gas accretion

# Dependence on stellar mass



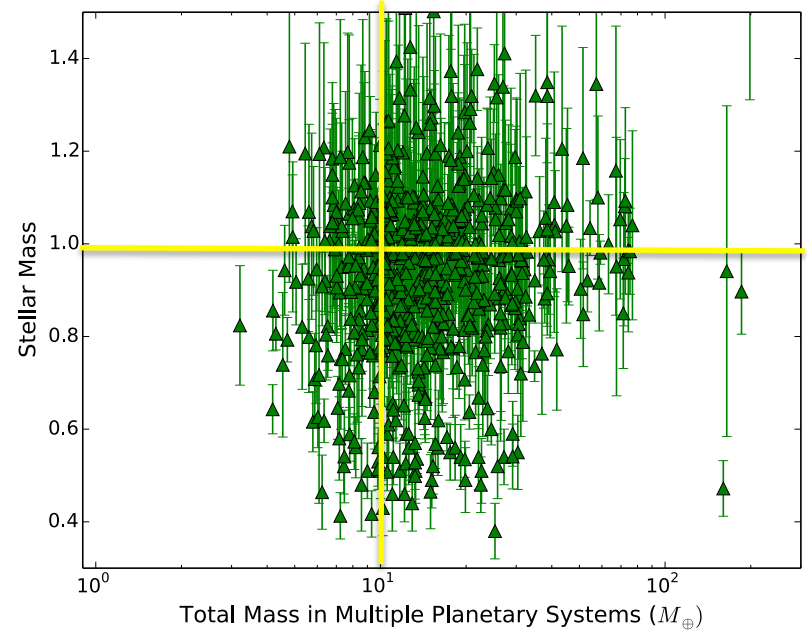
Ida

Wolfgang



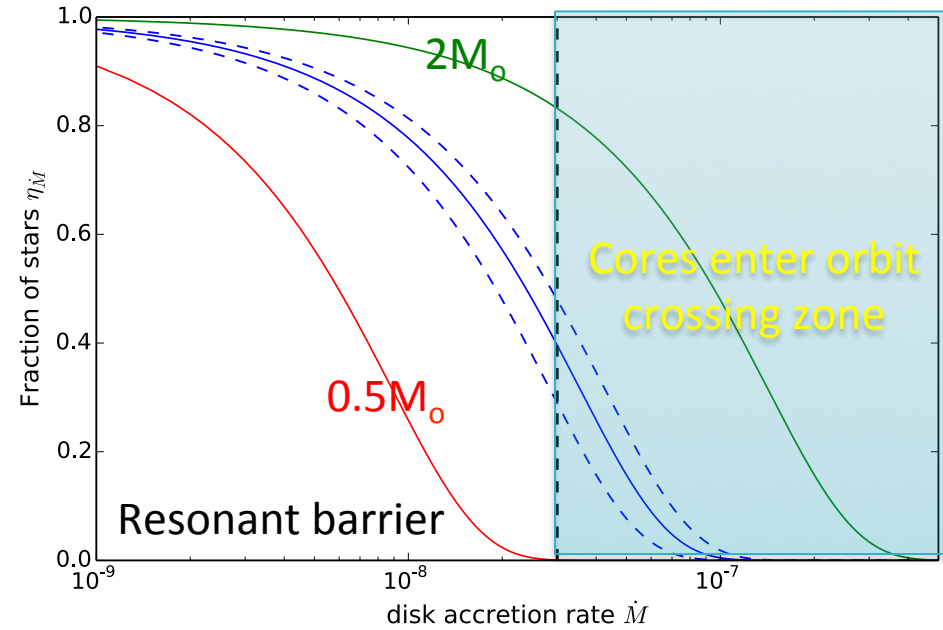
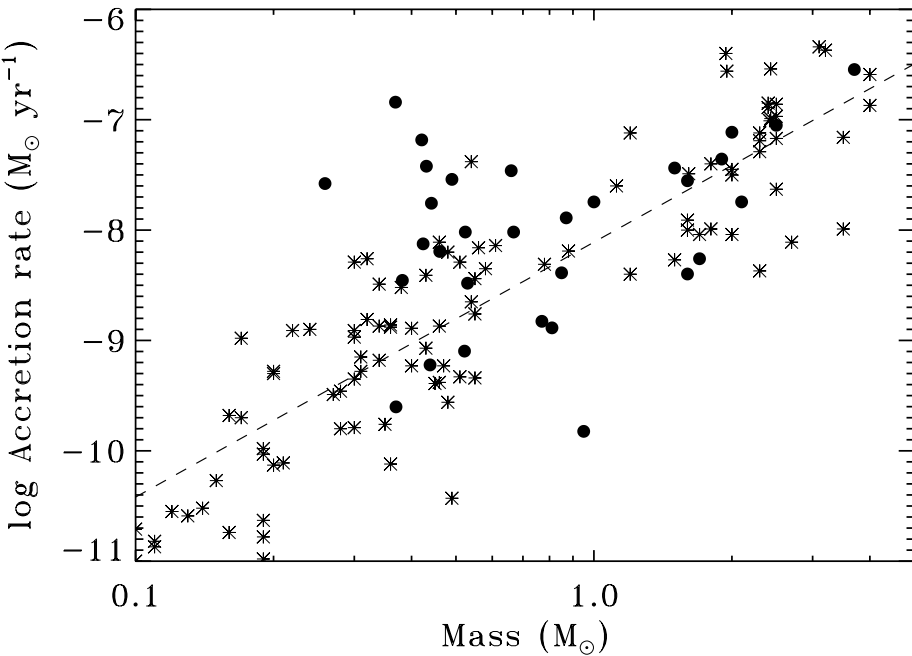
Beibei Liu

32/66

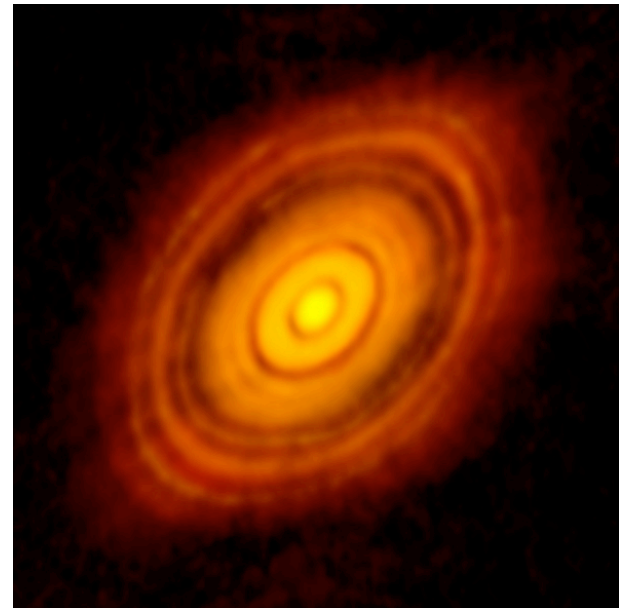




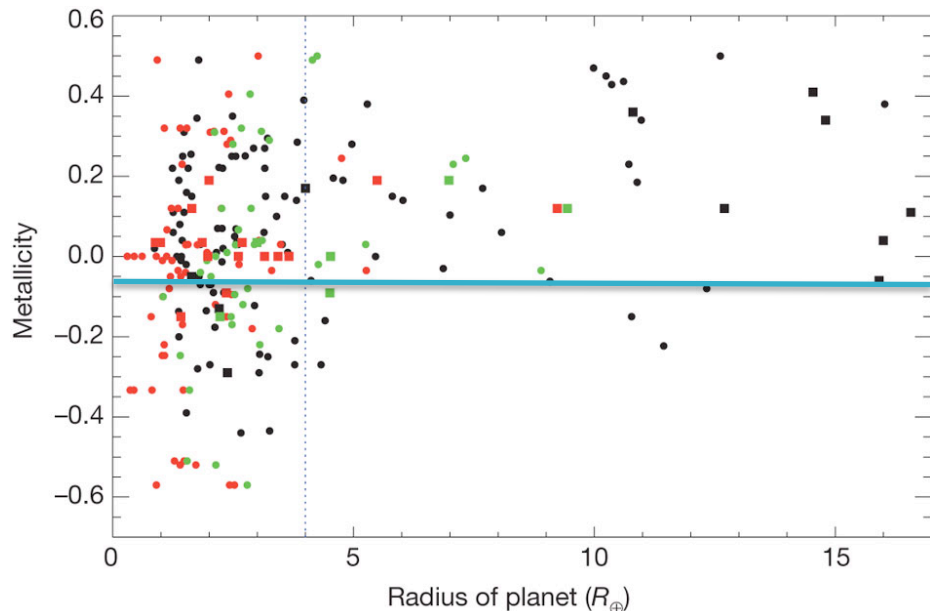
# Dependence on the disks' accretion rate



- 1) Cores' migration speed is determined by the surface density of the disk gas.
- 2) Surface density of the disk gas is proportional to the gas accretion rate
- 3) Gas accretion is observed to increase with the host stars' mass.
- 4) Gas giants' frequency correlation with the host stars' mass is through  $\dot{m}$ .

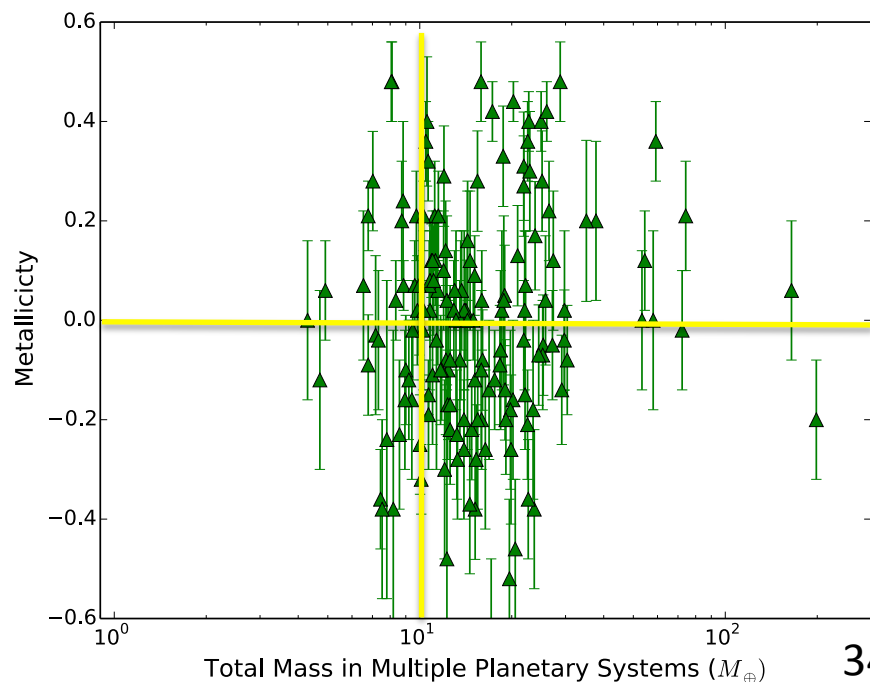
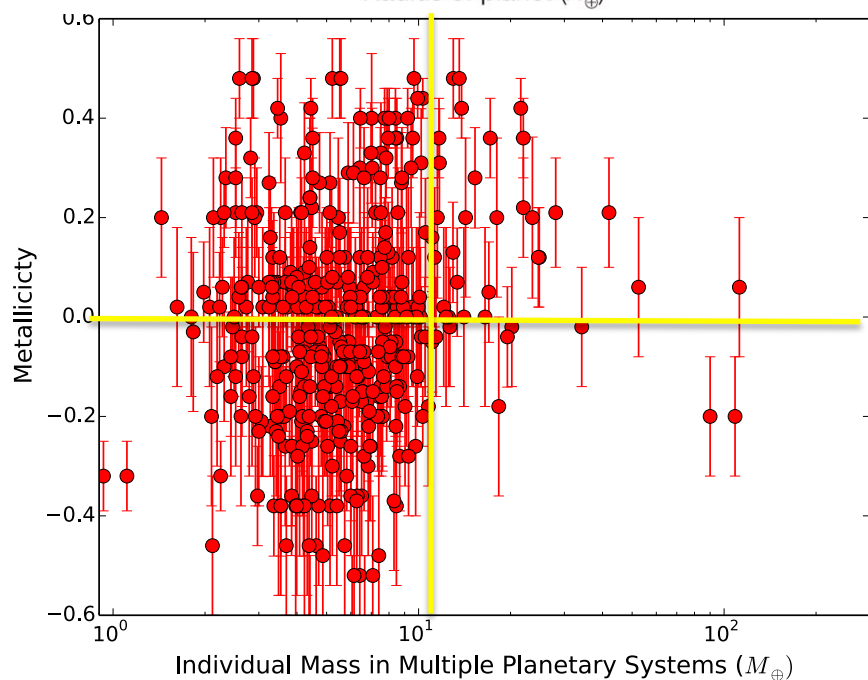


# Abundance of super Earths

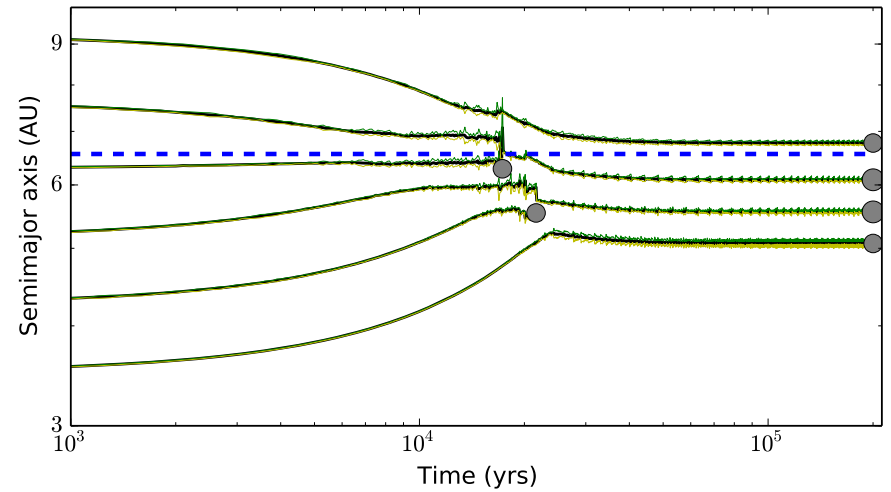
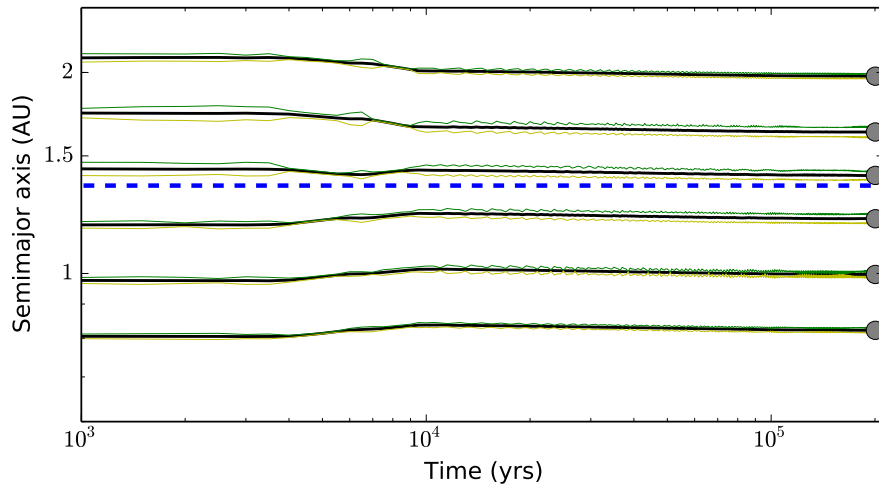
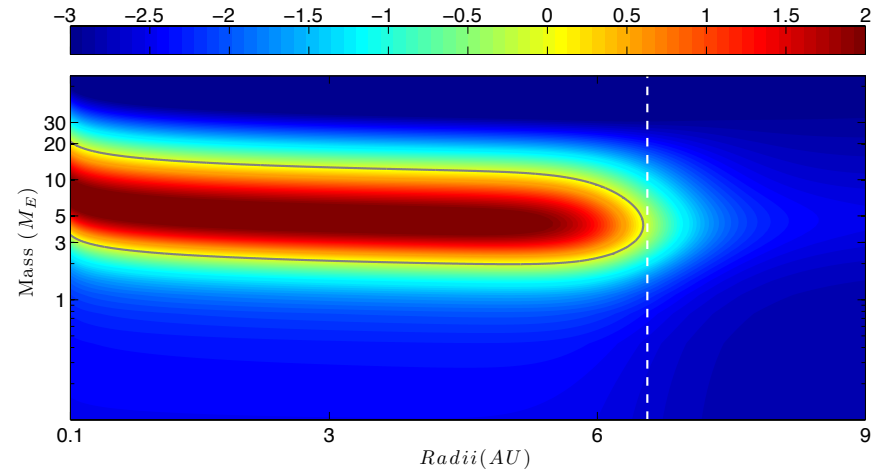
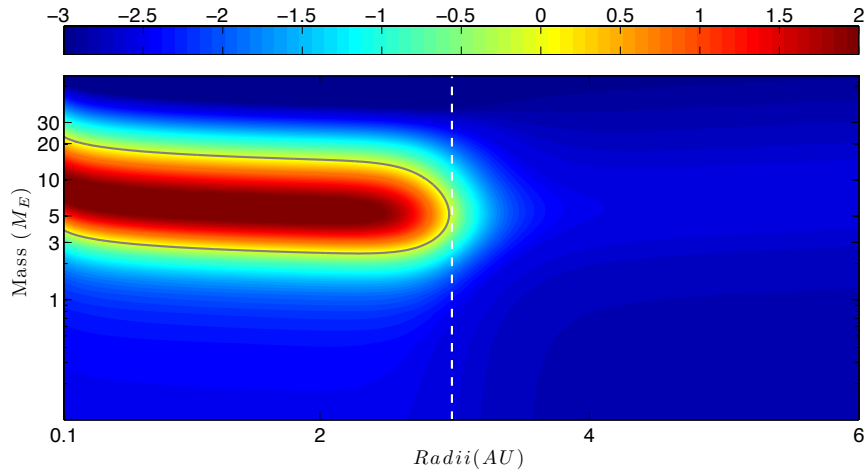


There is **no** shortage of super Earths around metal-poor stars

Formation of super Earths  
Does **not** depend on  $Z_*$  or  $M_*$



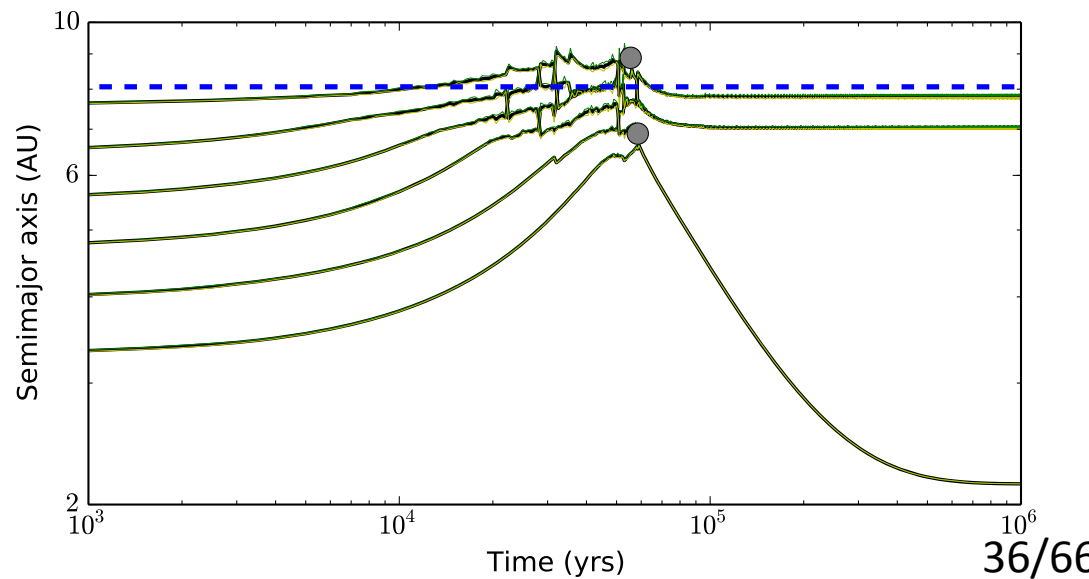
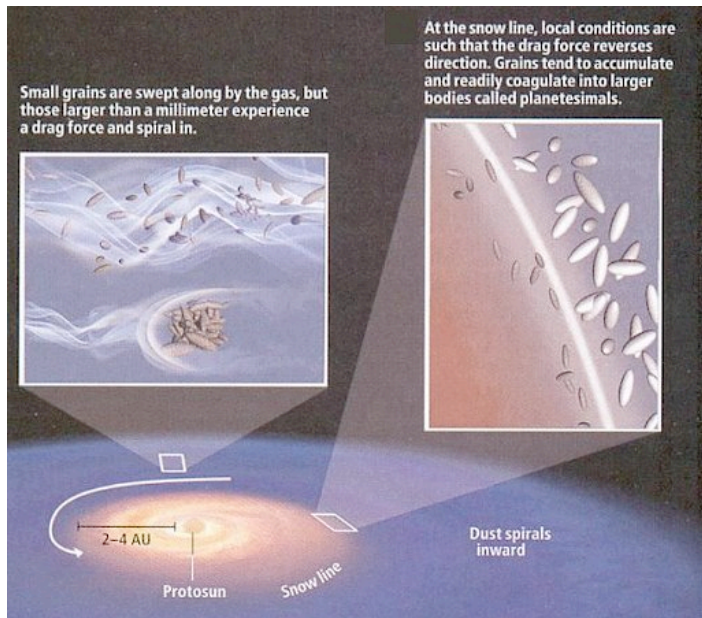
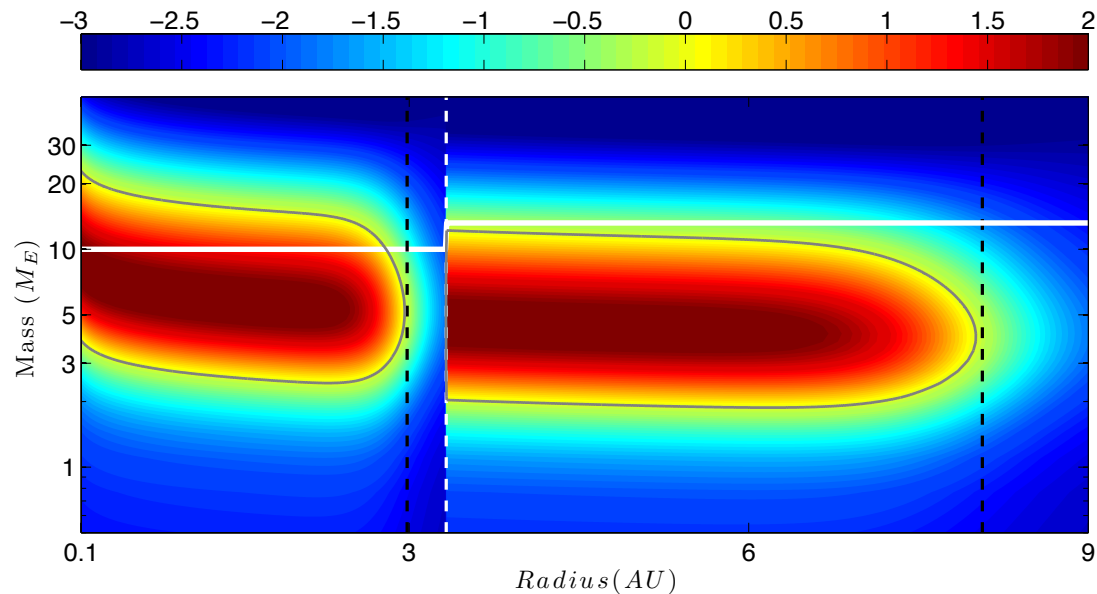
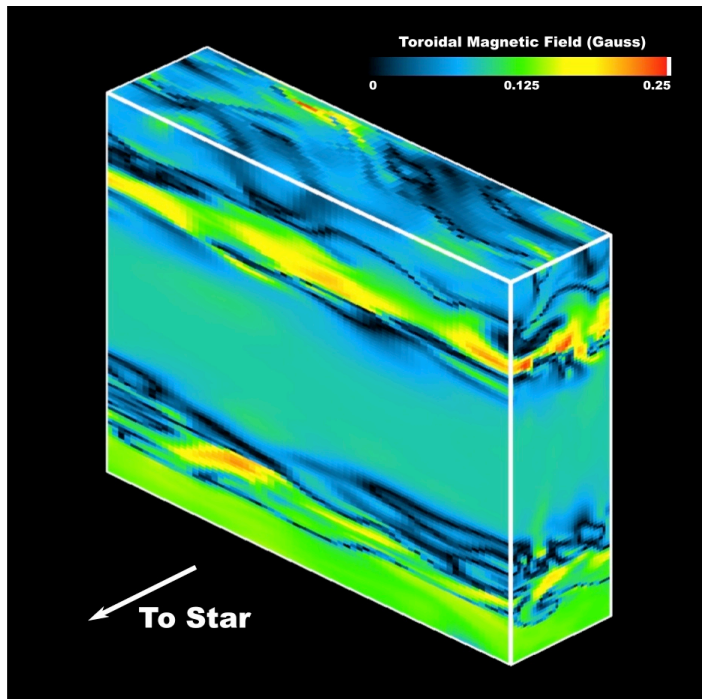
# Dependence on metallicity



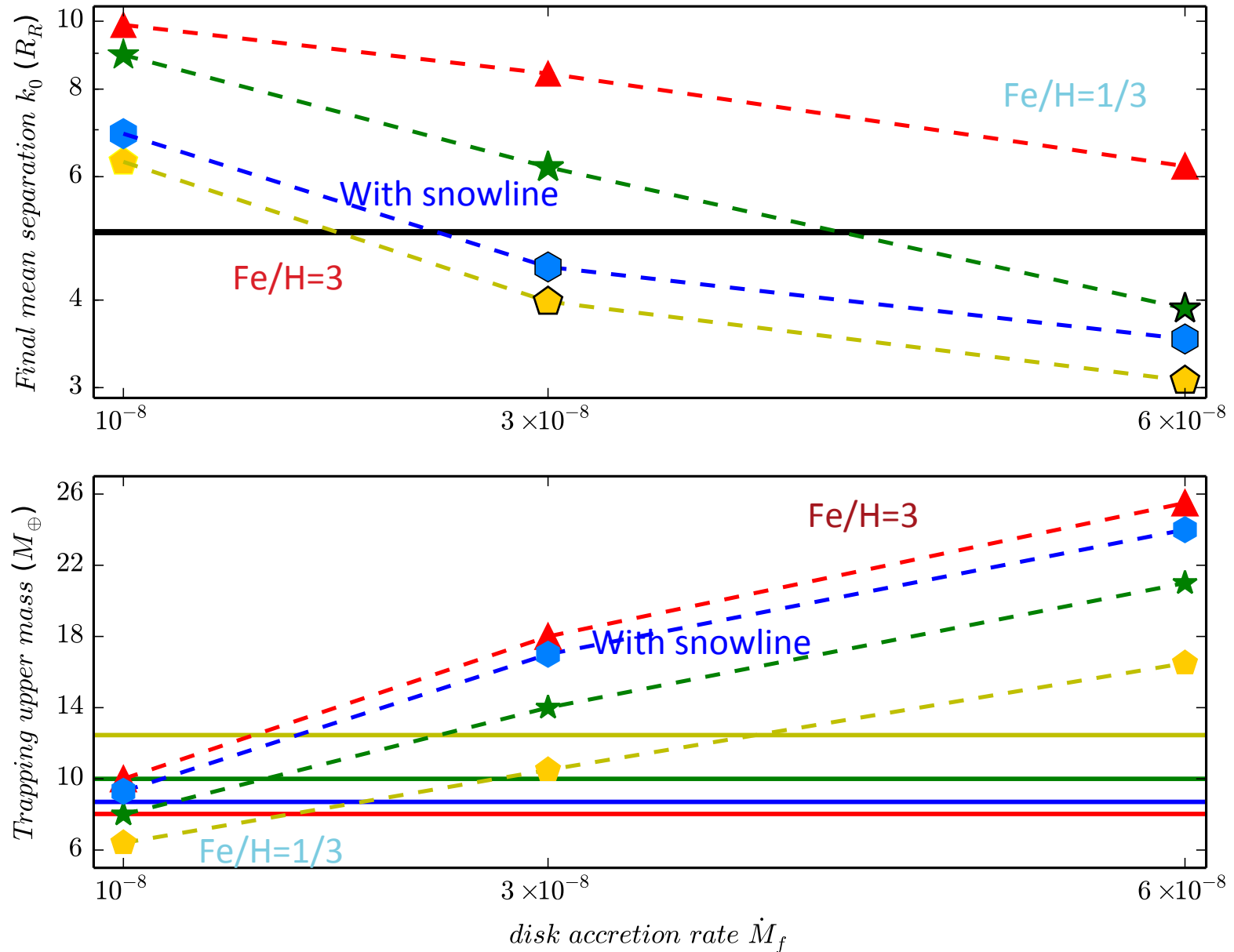
Fe/H=1

$3 \times 10^{-8} M_{\text{sun}}/\text{yr}$

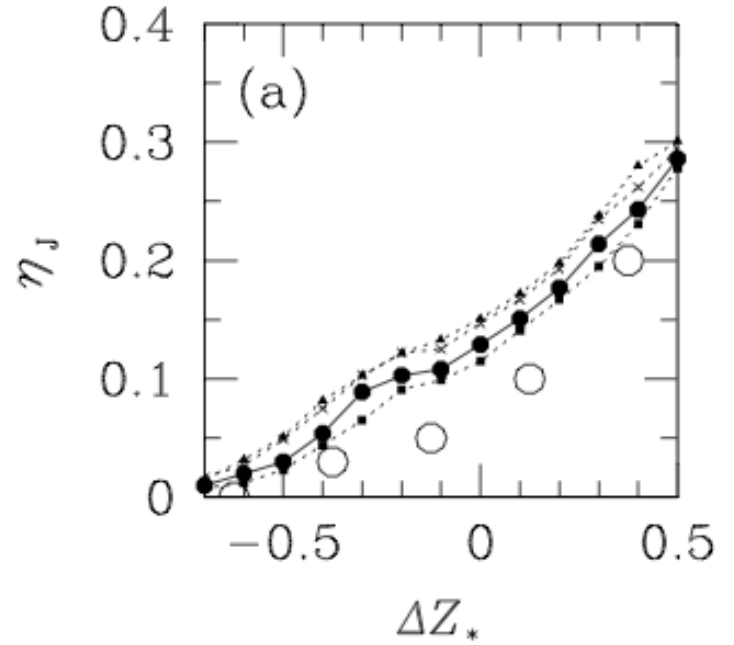
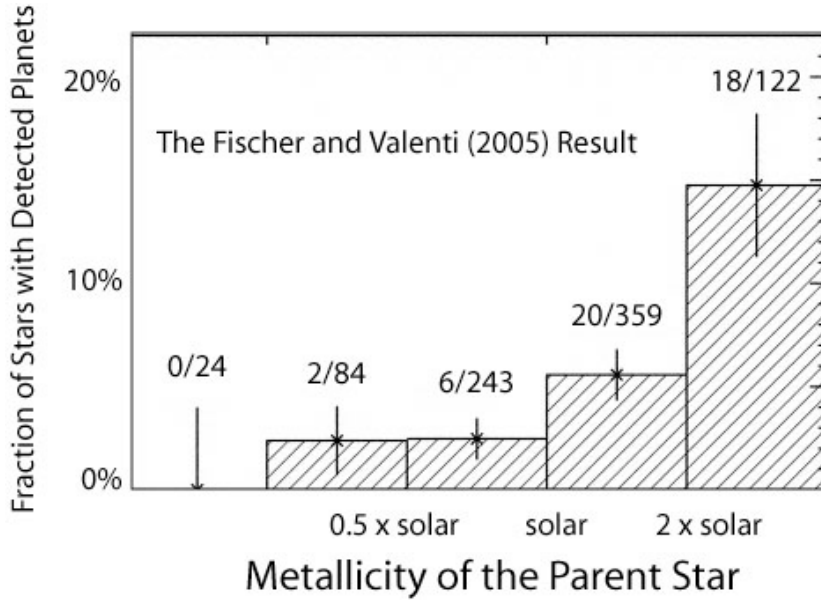
Fe/H=3



# Migration in metal-rich disks



# Planetary mass & size vs stellar metallicity



**BUT,  $Z_d$  is not  $Z_*$**

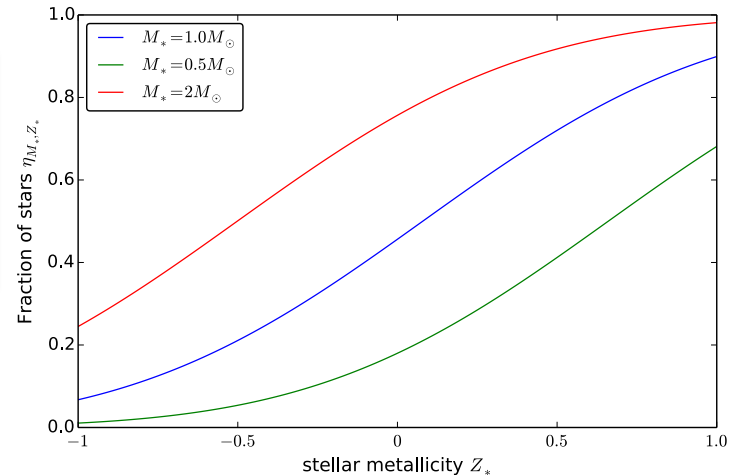
$$\frac{d^2N}{d\dot{M}_g dZ_d} = A_0 \exp - [(\log(\dot{M}_g/\dot{M}_a)/\Delta_{\dot{M}})]^2 \exp - [(Z_d - Z_*)/\Delta_Z]^2$$

$$\eta_Z(\dot{M}_f, M_*, Z_*) = \frac{1}{2} \int \text{erfc} \left( \frac{\log[\dot{M}_f(M_*, Z_d)/\dot{M}_a(M_*)]}{\Delta_{\dot{M}}} \right) \exp - [(Z_d - Z_*)/\Delta_Z]^2 dZ_d.$$

$$r_{\text{trans}} \simeq 1.36 \dot{m}_{a8}^{0.72} m_*^{-0.08} \alpha^{-0.36} \kappa_0^{0.36} \text{AU}$$

$$M_{\text{opt}}(r_{\text{trans}}) \simeq 3.6 \dot{m}_{a8}^{0.48} m_*^{1.24} \alpha_3^{0.43} \kappa_0^{0.24} M_{\oplus}$$

$$\dot{m}_{g \text{ res}} \simeq 6 f_{\text{res}}^{0.95} m_*^{0.07} \alpha_3^{0.97} \kappa_0^{-0.026}$$

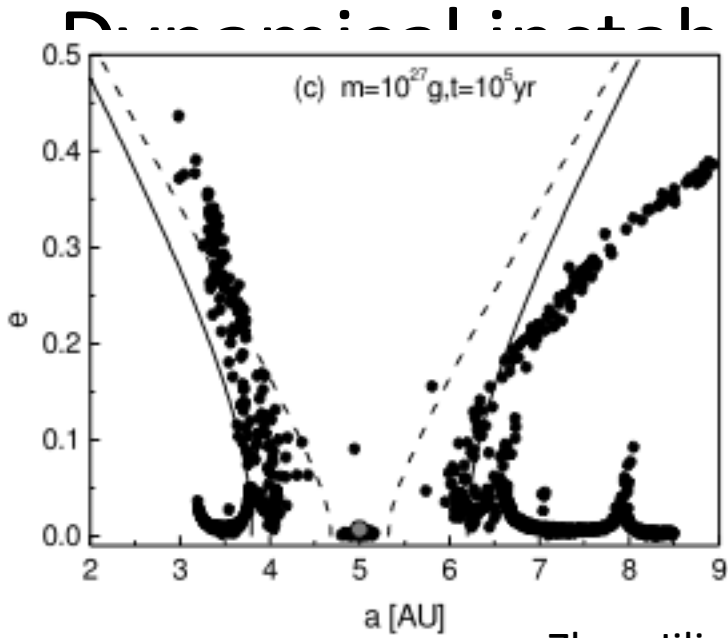


# Some major Challenges:

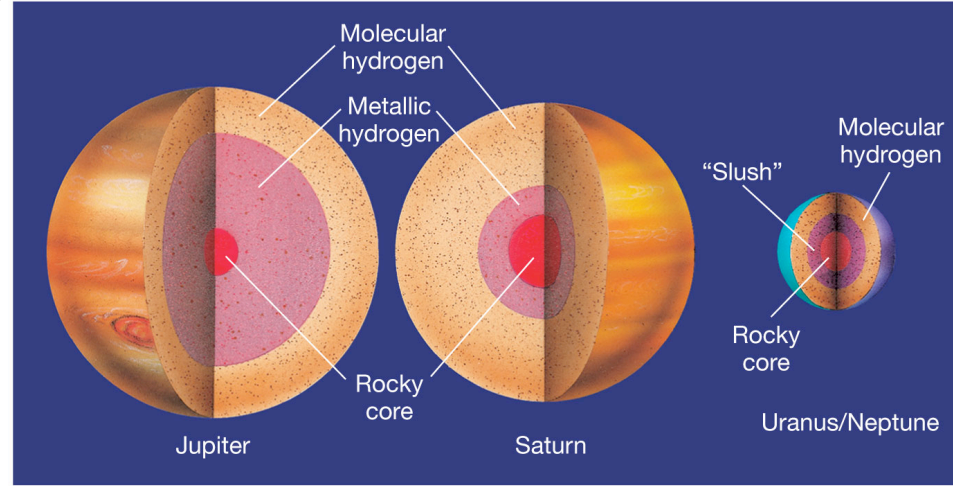
- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- **Multiple gas giants and eccentricity excitation**
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple planets: rapid & slow depletion of disk gas
- Competing physics on multiple length & time scales

# Rapid growth of proto gas giant planets:

Dimensional instability impacts & mergers

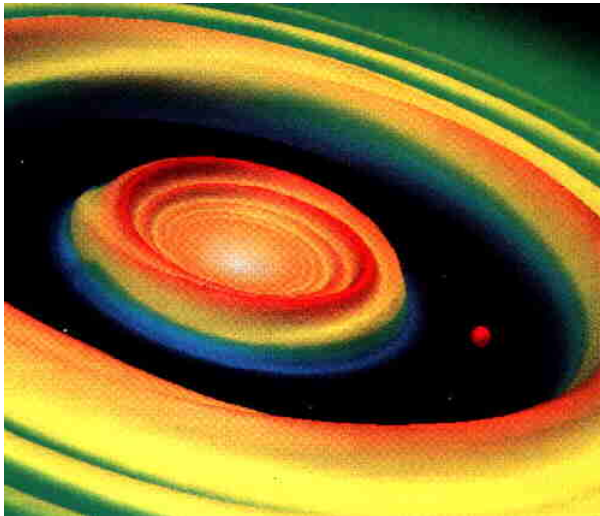
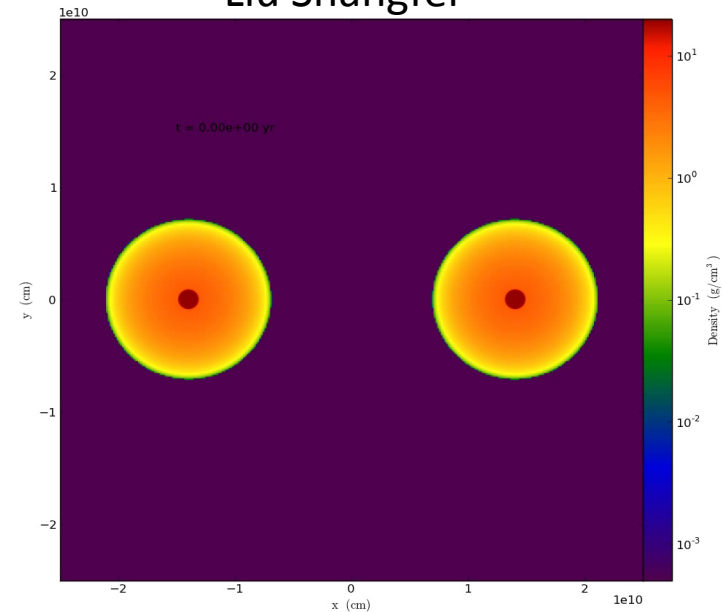


Zhou Jilin



(a)  
© 2011 Pearson Education, Inc.

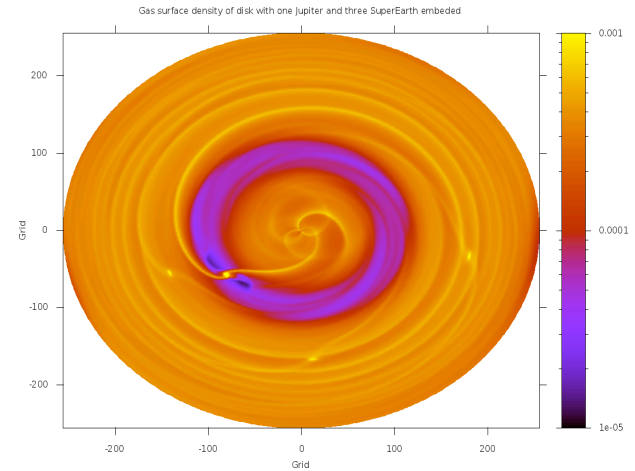
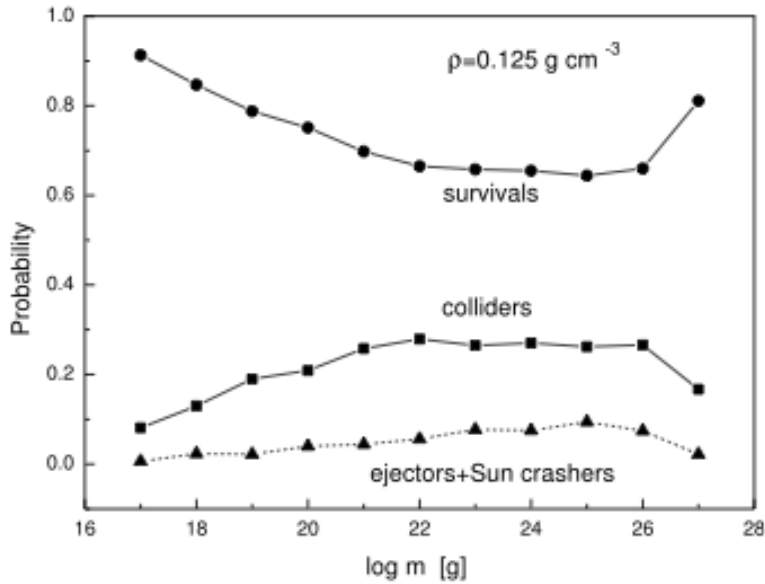
LIU Shanglei



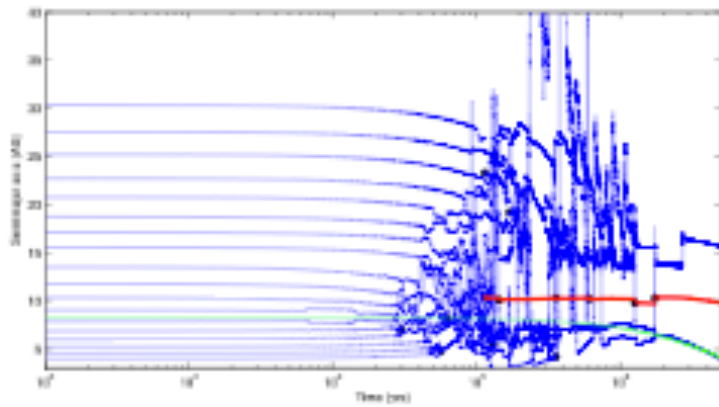
Bryden



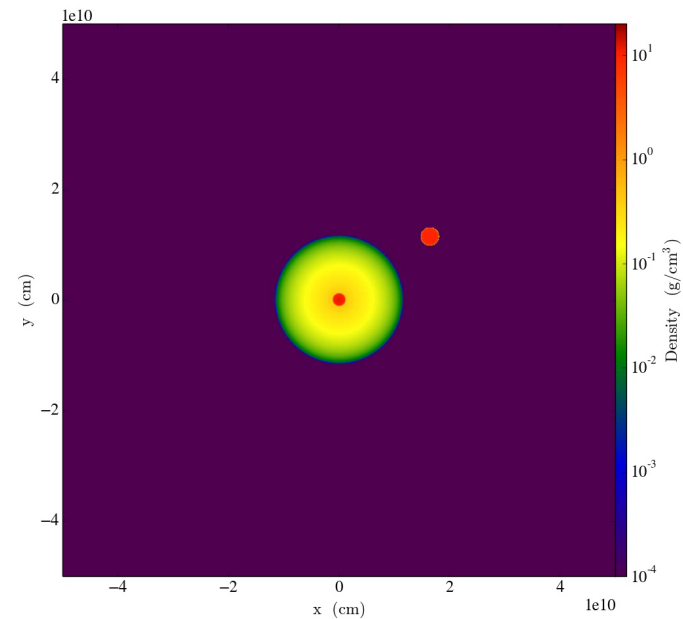
# Enhanced formation of multiple planets



XiaoJia Zhang

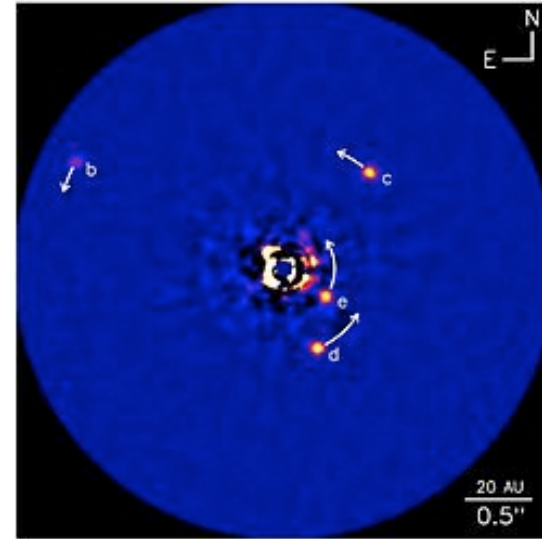
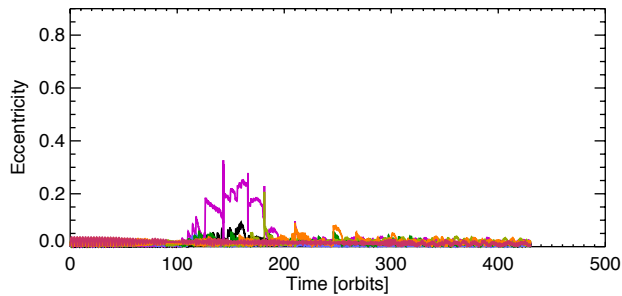
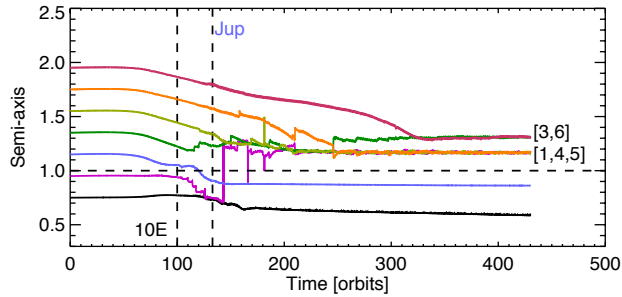


BeiBei Liu

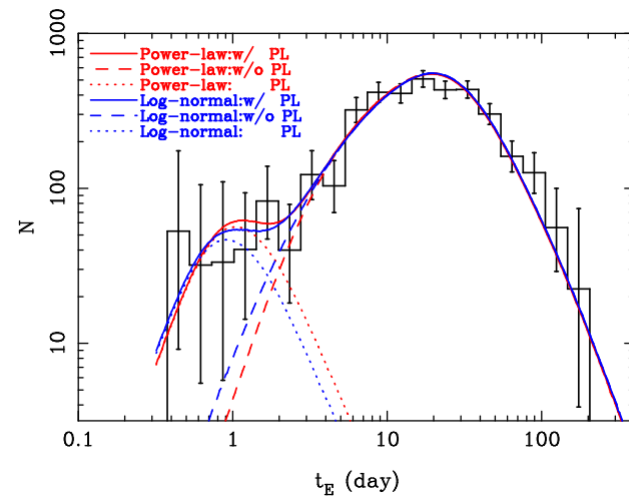
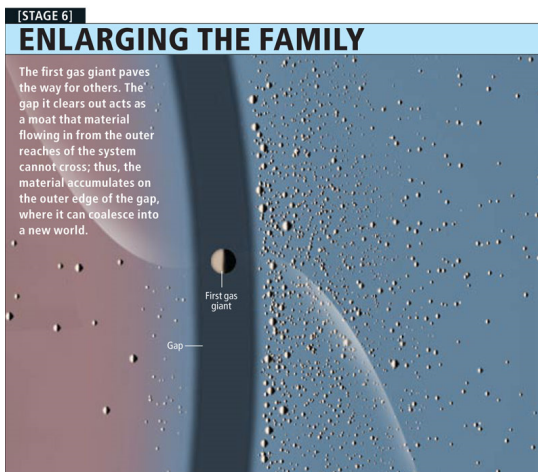


Shangfei Liu

# Enhanced formation of multiple planets

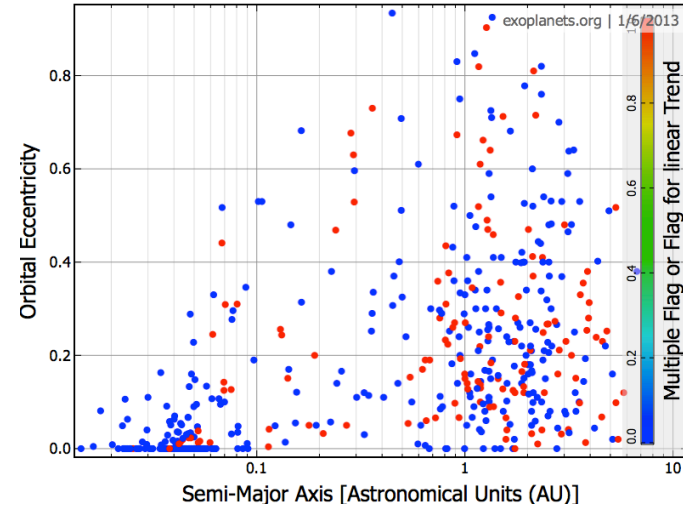
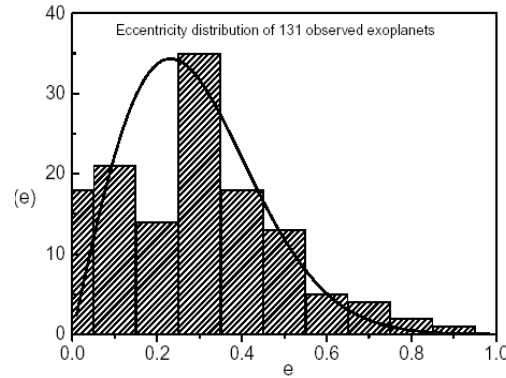
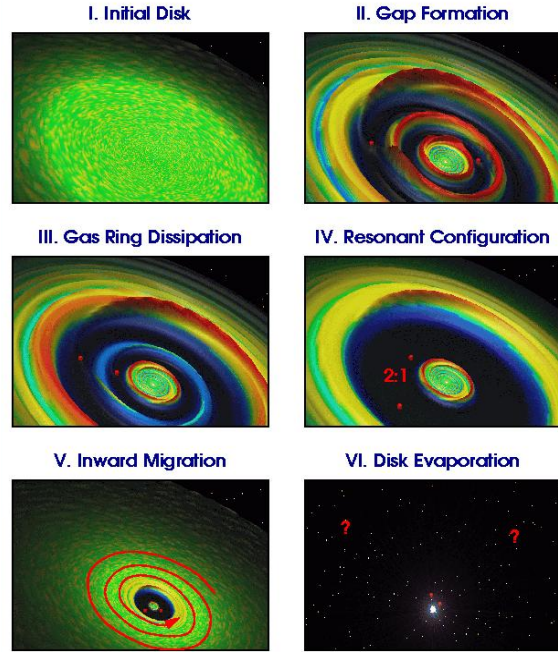


XiaoJia Zhang

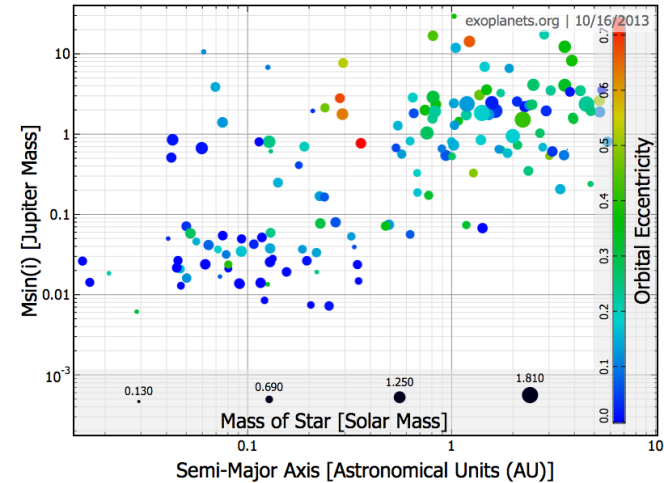
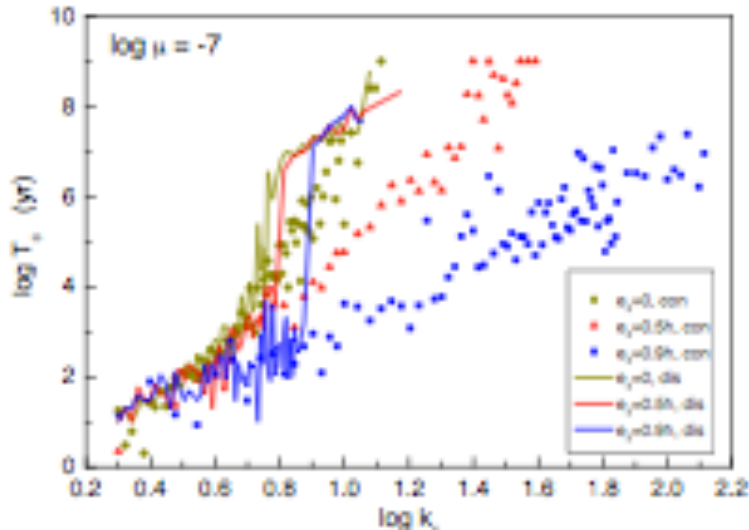


# Grand design barrier: dynamical instability

- How did gas giants acquire their eccentricity?

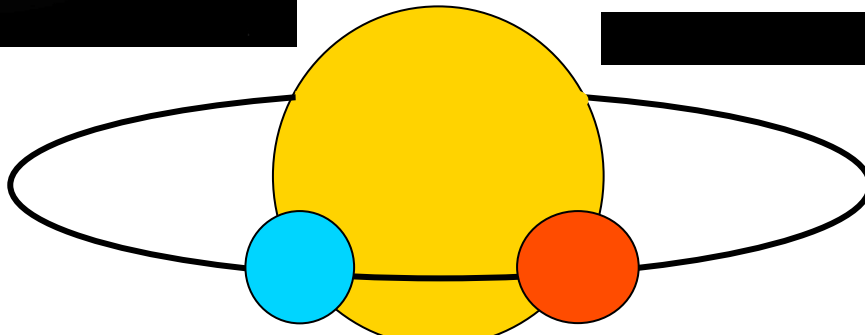
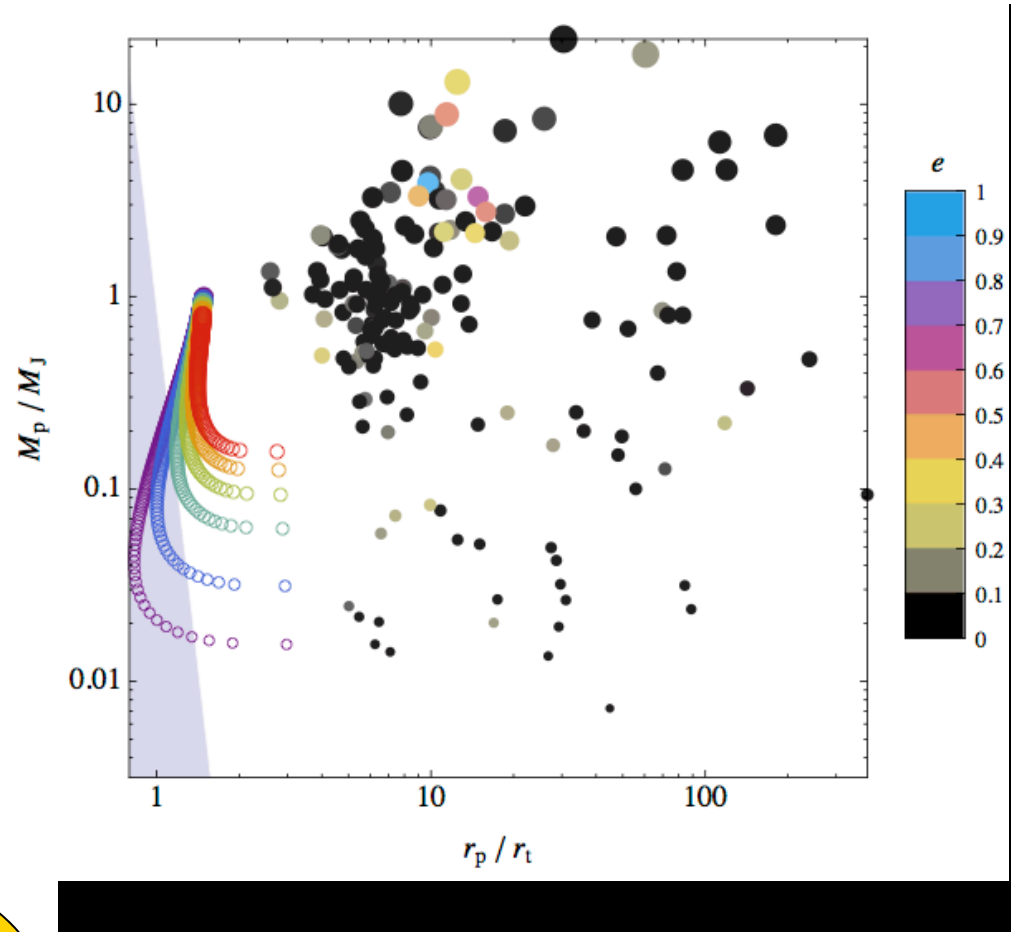
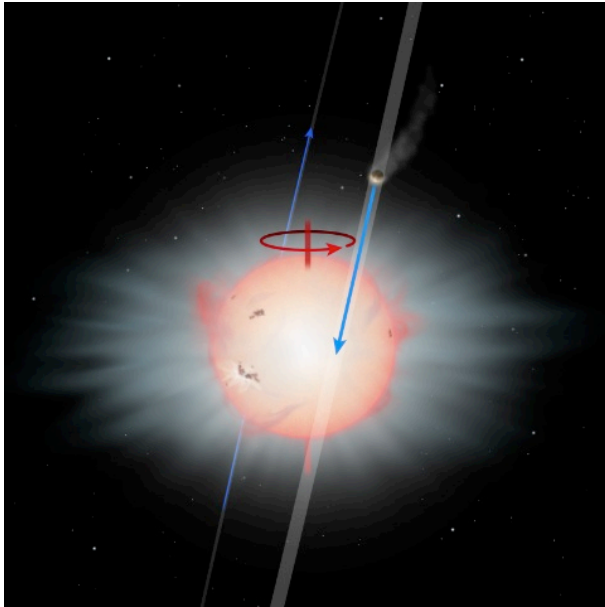
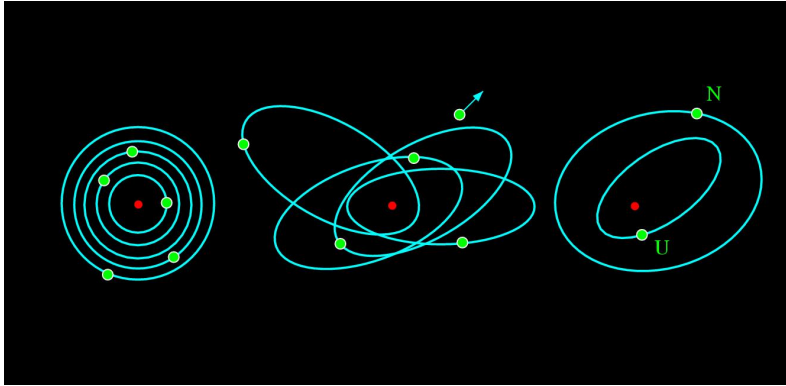


Bryden



Jilin Zhou

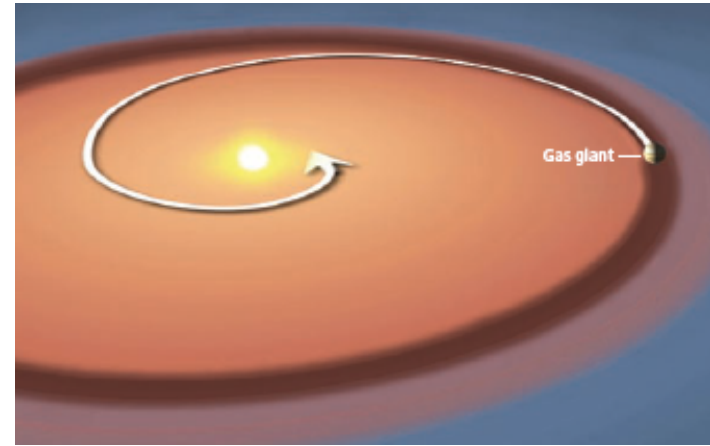
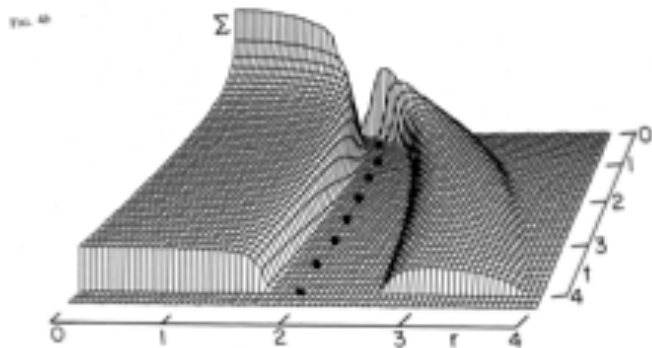
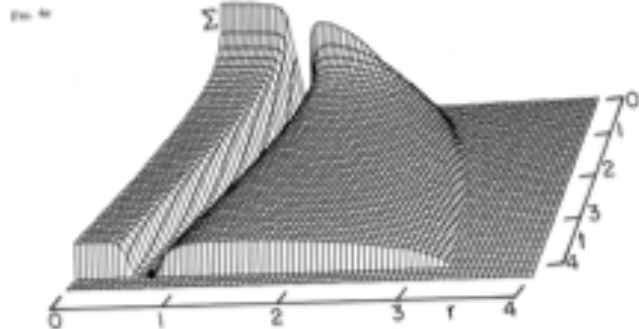
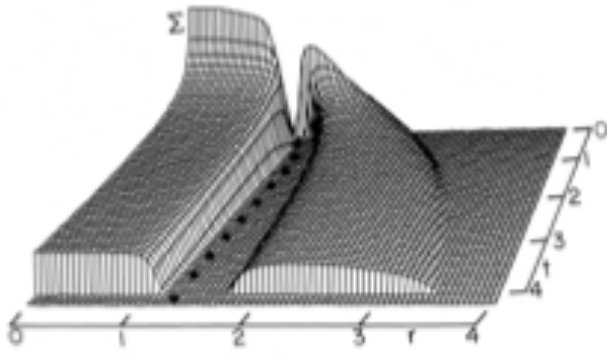
# RM effect and challenge to migration



# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Multiple gas giants and eccentricity excitation
- **Retention of gas giants: type II migration (Lin & Papaloizou)**
- Multiple gas giants: rapid depletion of disk gas
- Competing physics on multiple length & time scales

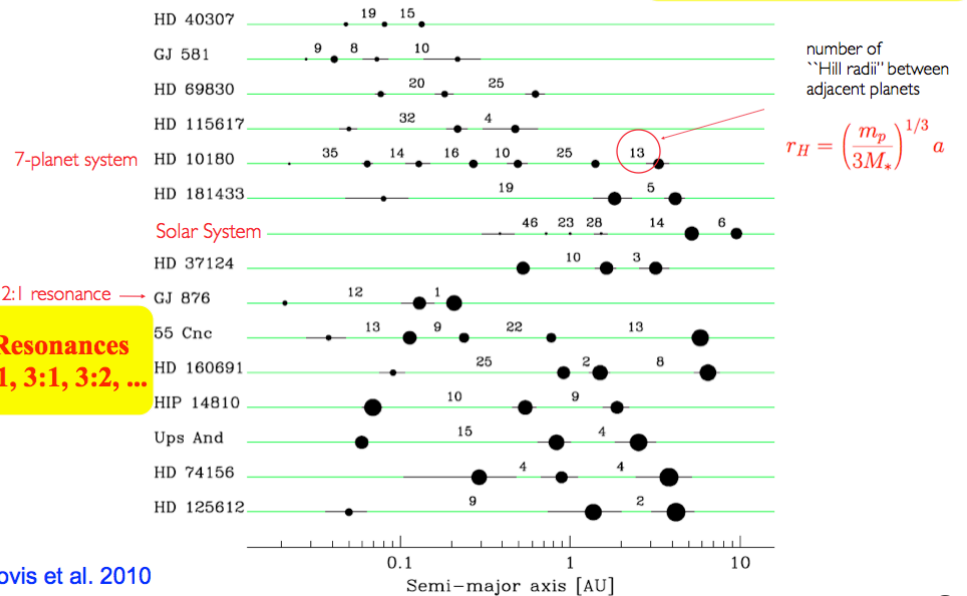
# Gas giants' type II migration



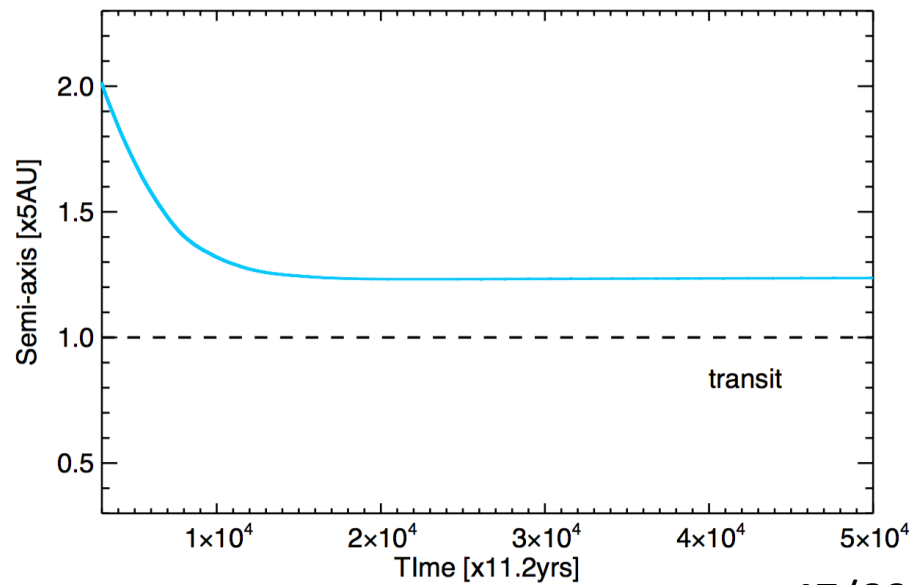
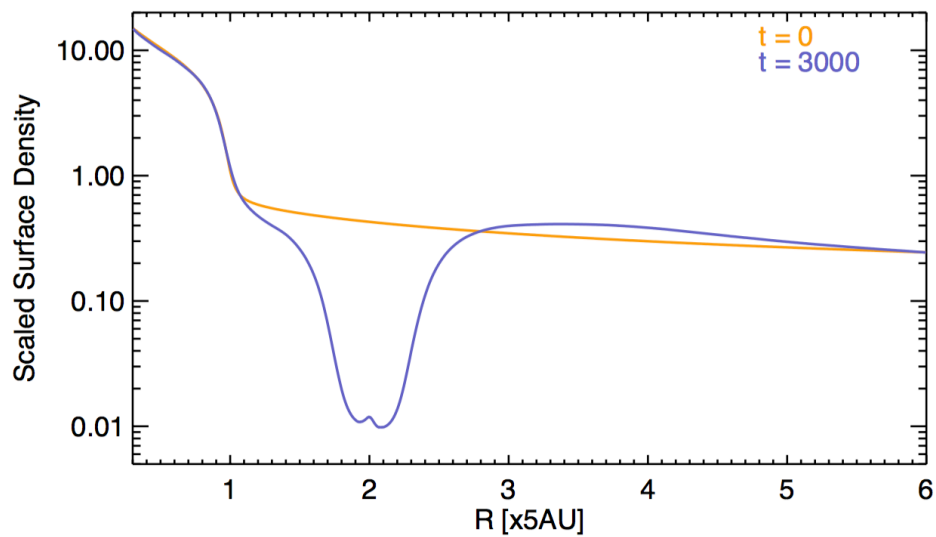
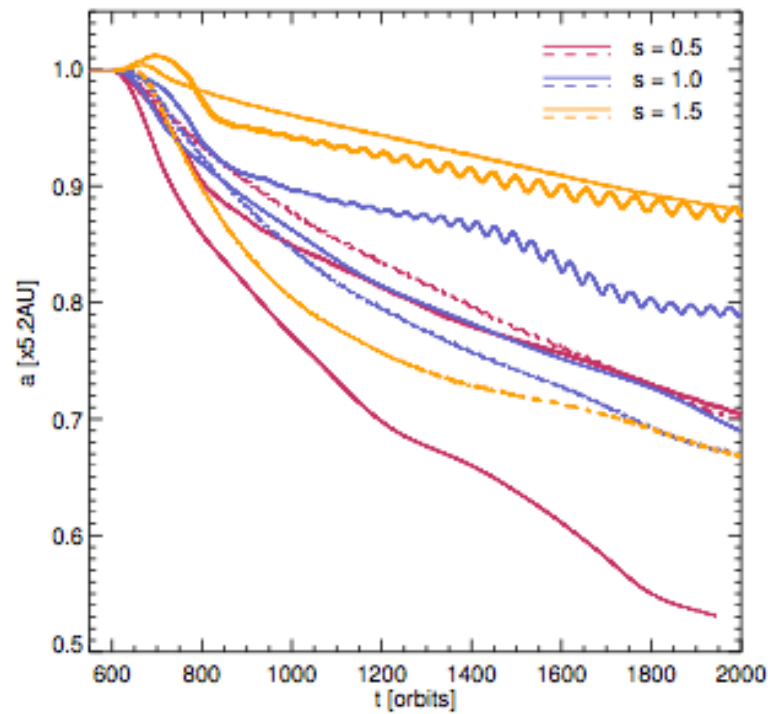
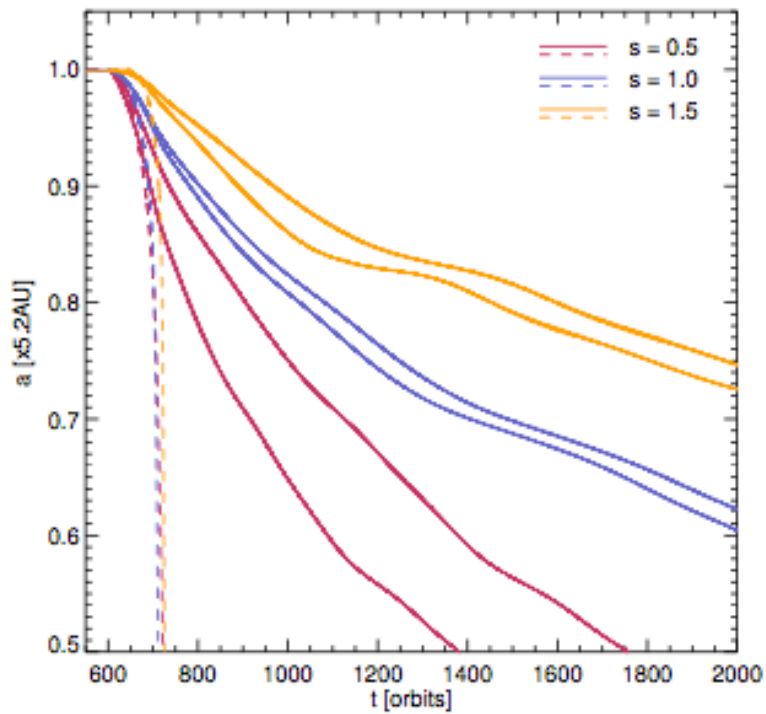
## Systems with n>2 planets

multi-planet systems: many are almost optimally "packed"

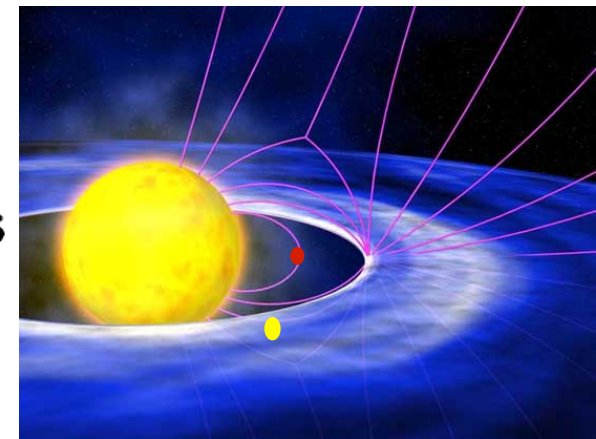
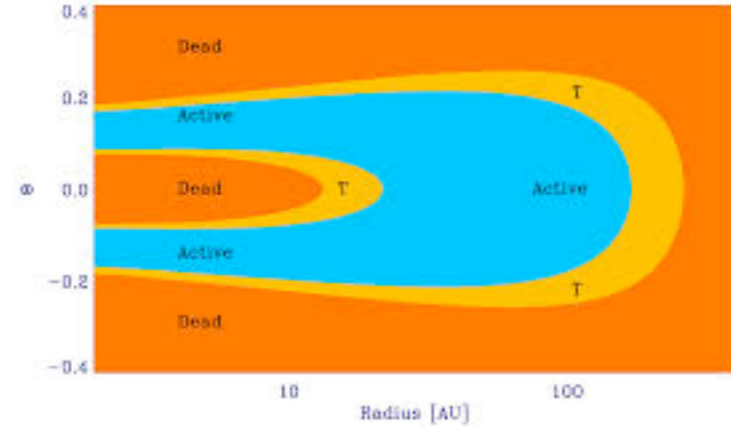
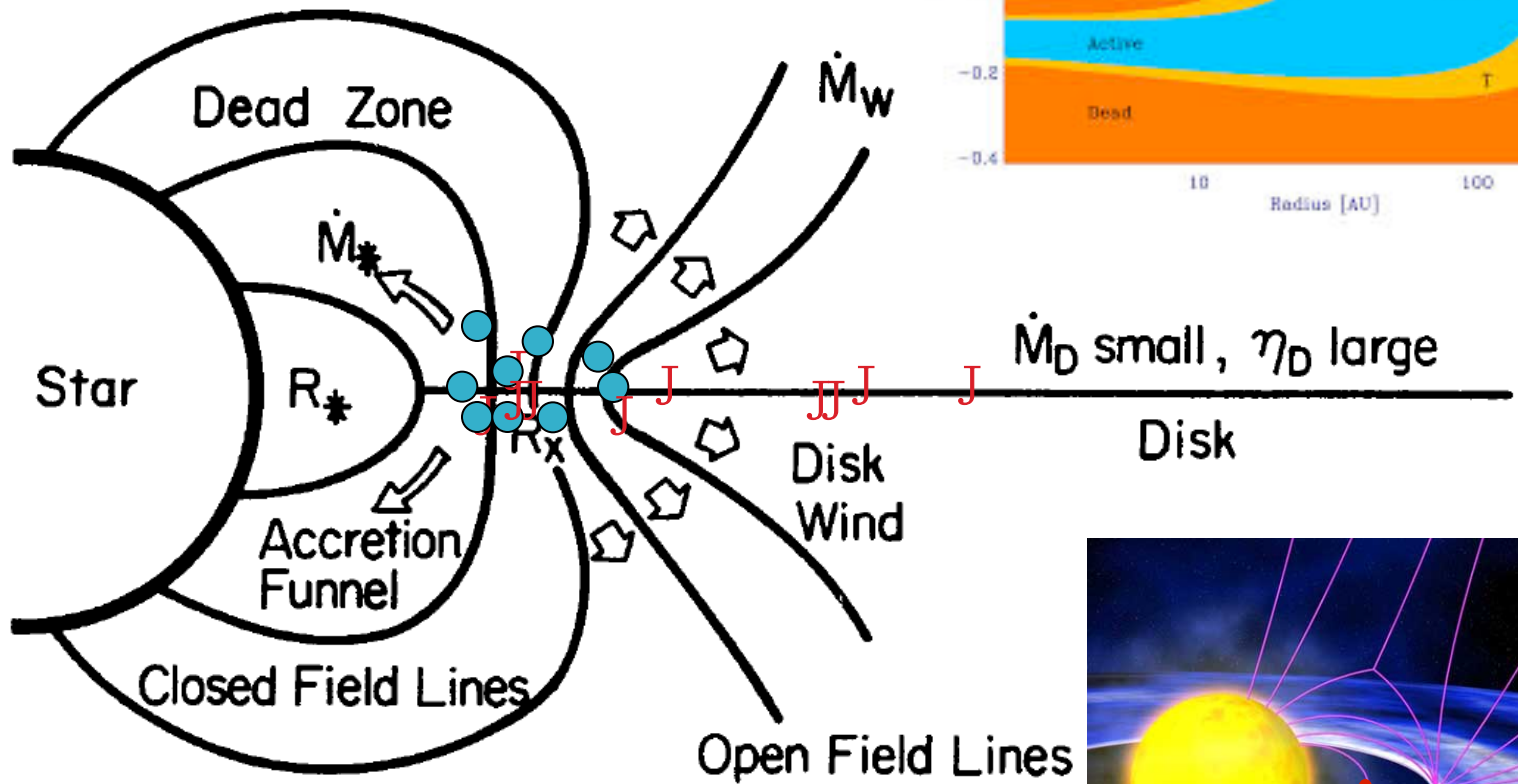
Also a constraint for planet formation models!



Lovis et al. 2010



# Stalling type II migration



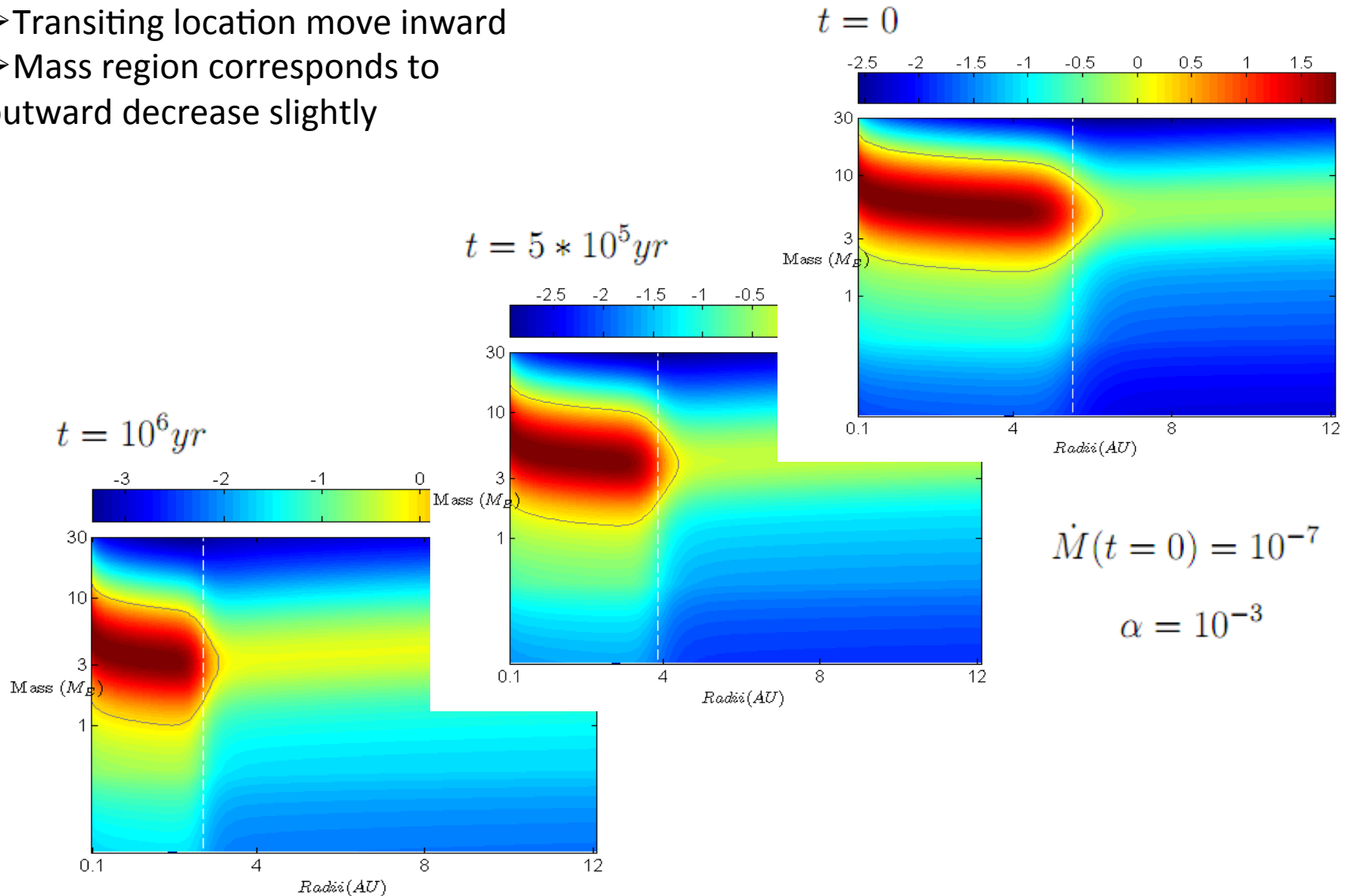


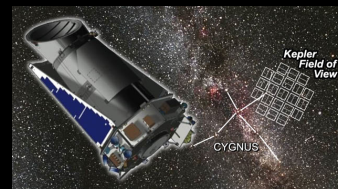
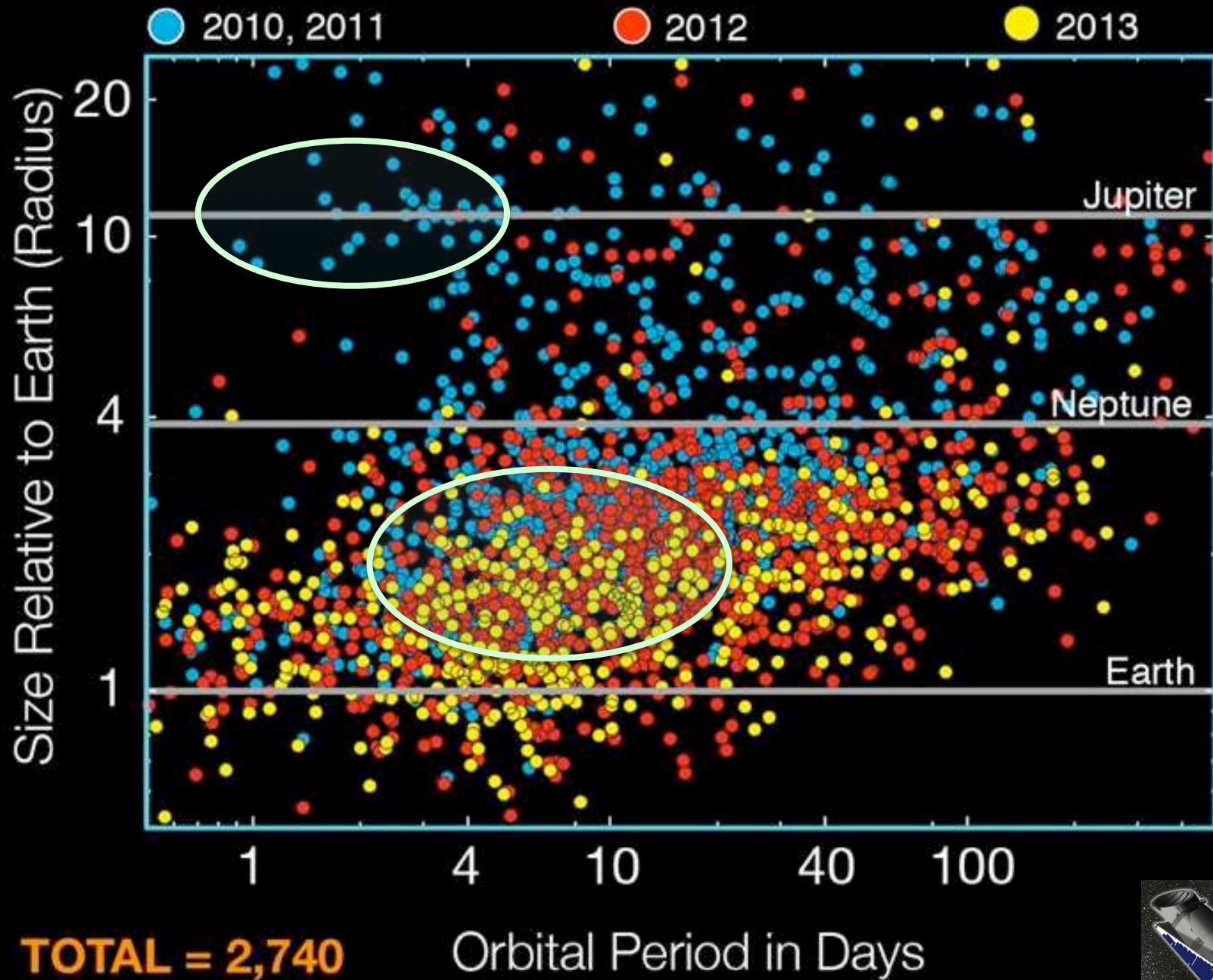
# Some major Challenges:

- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Multiple gas giants and eccentricity excitation
- Retention of gas giants: type II migration (Lin & Papaloizou)
- **Multiple planets: rapid & slow depletion of disk gas**
- Competing physics on multiple length & time scales

# Type I migration with evolving disk

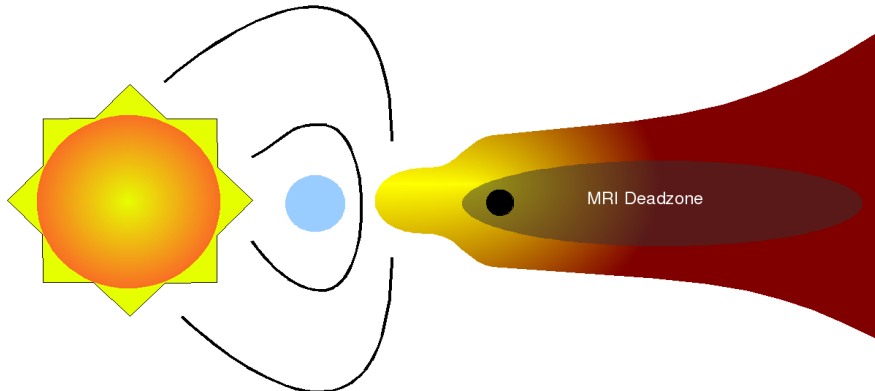
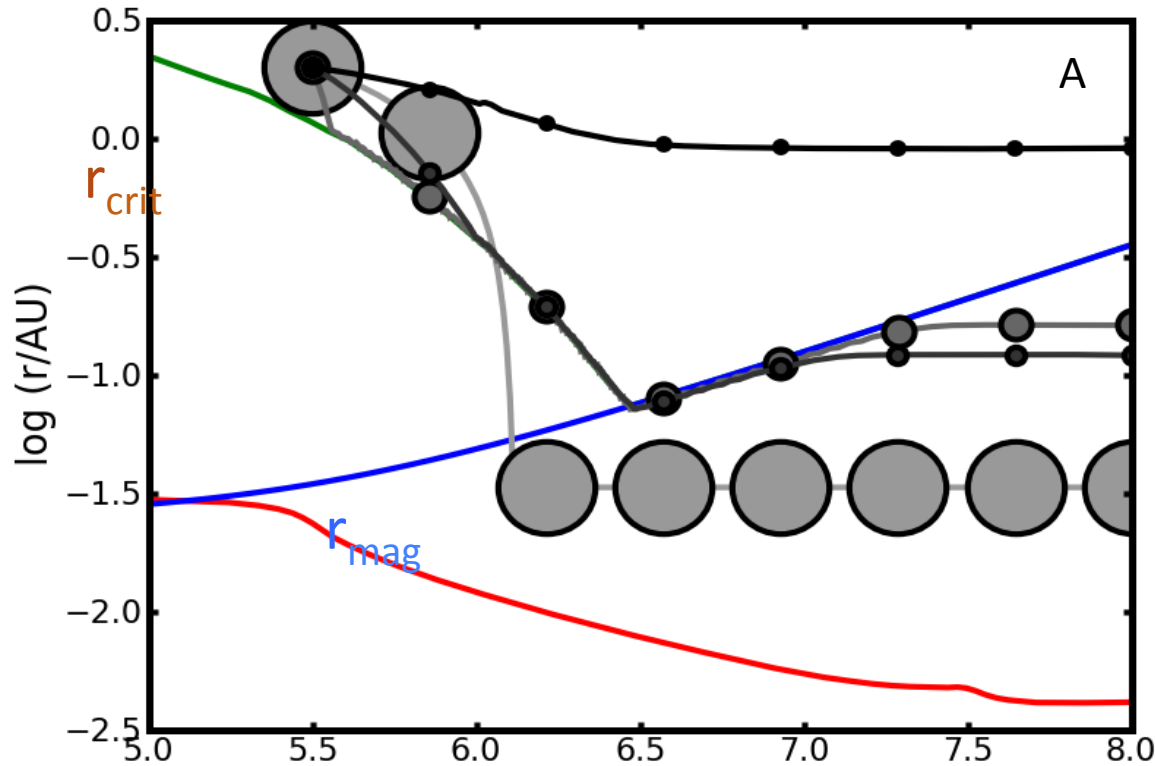
- Transiting location move inward
- Mass region corresponds to outward decrease slightly





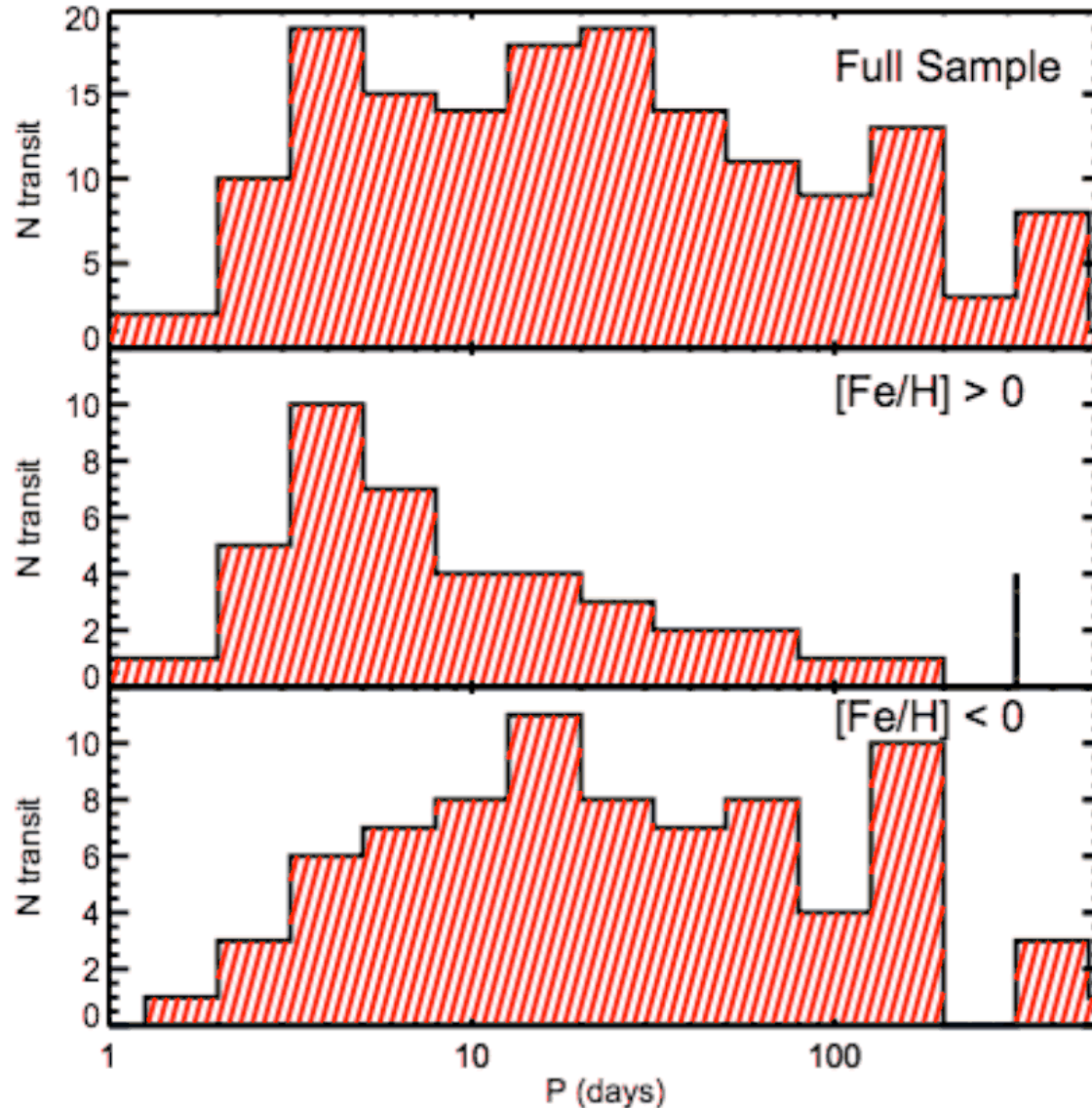
# Super Earths: some key issues

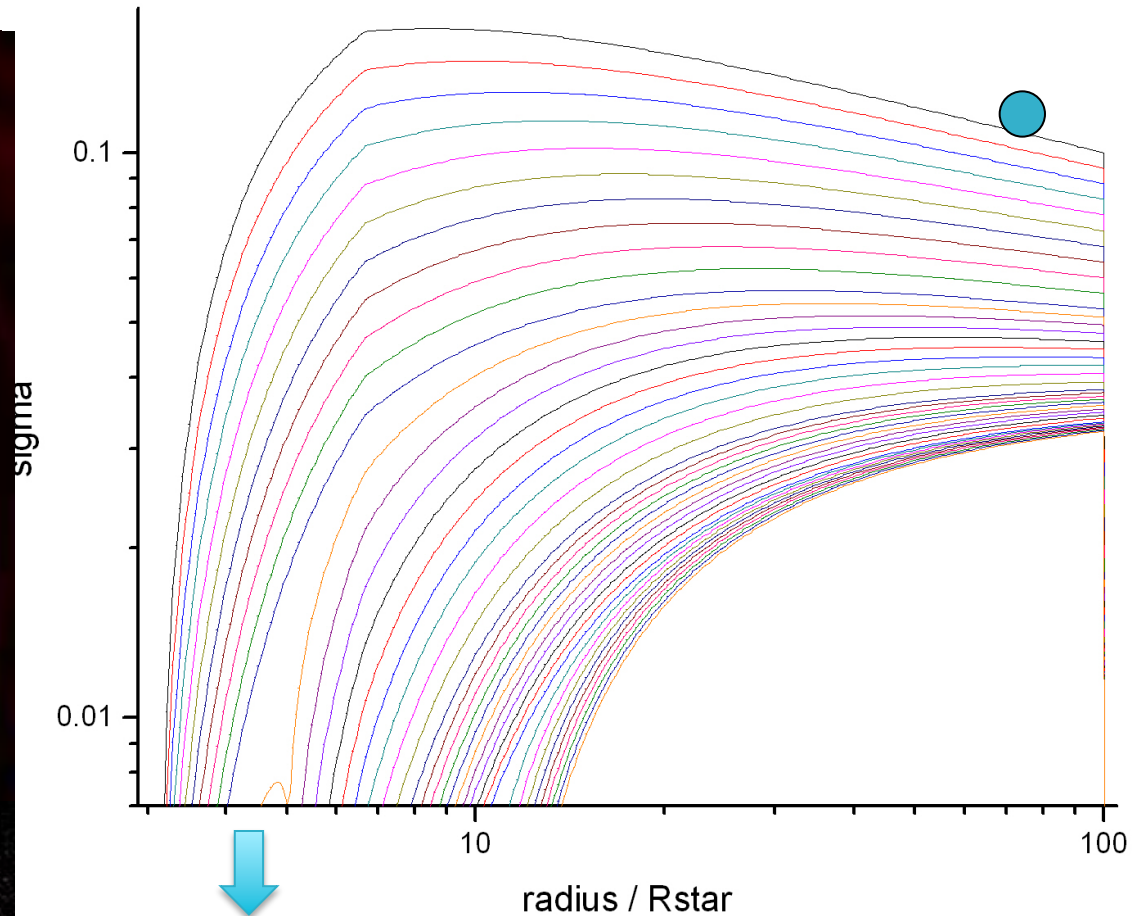
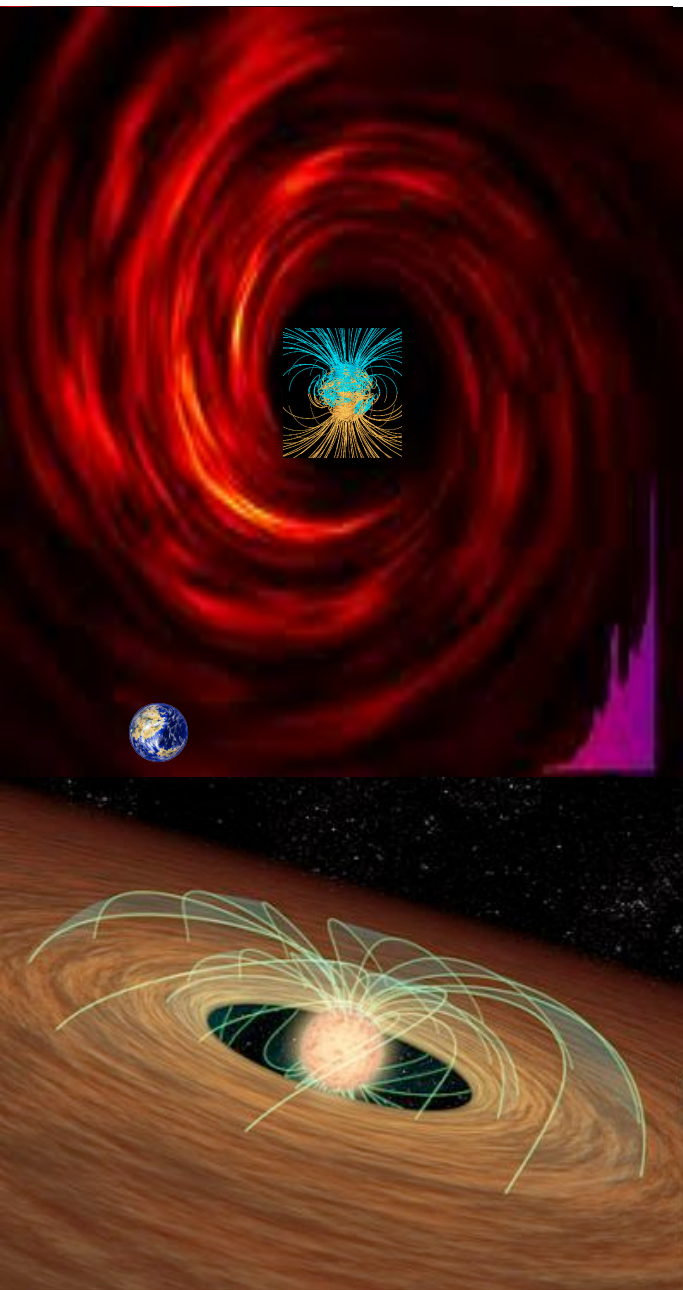
- How to differentiate type I and II migration?





**Hot Jupiters park  
Closer than  
Super Earths**

# Period distribution of hot Jupiters: Dependence on stellar metallicity

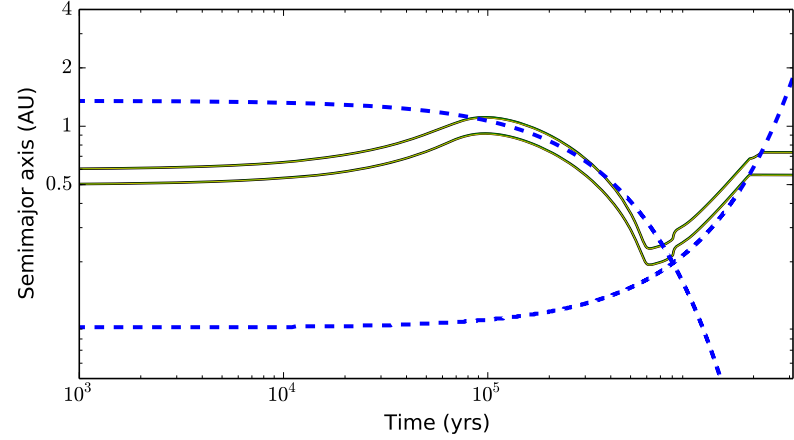
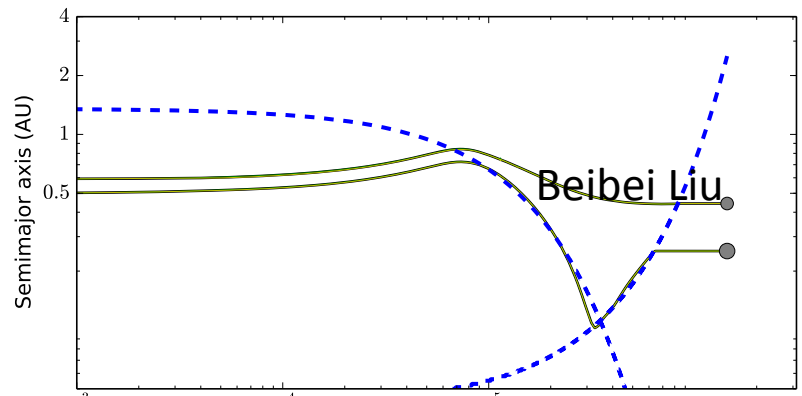
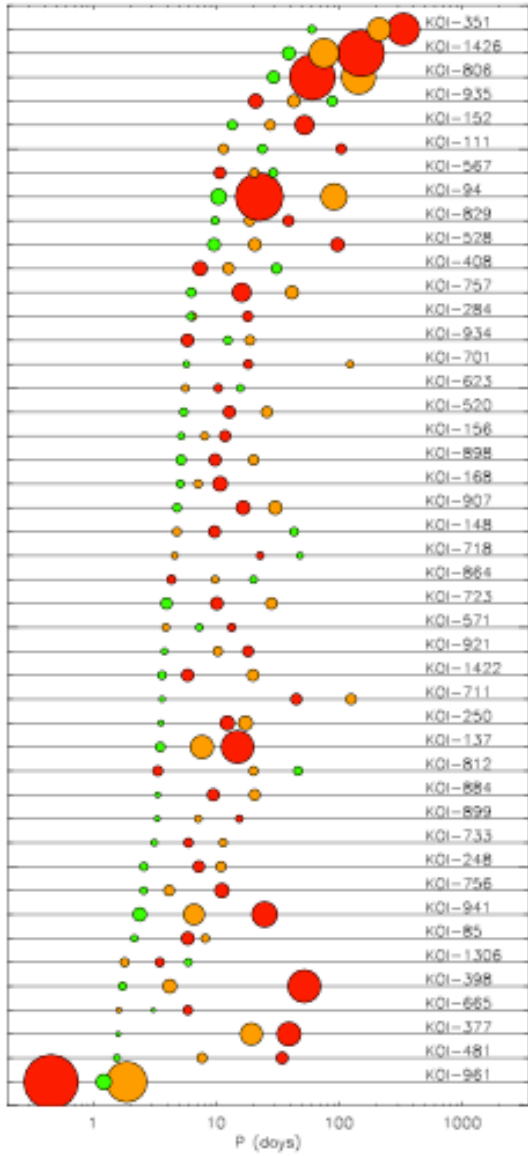





**Migration of a Super Earth in protostellar disk around a magnetized T Tauri star.** The Super Earth: (a) grows & migrate inward to inner-edge; (b) migrates slightly outwards with the expanding disk inner edge; (c) halts migrating after gas is mostly depleted. (Ju et al 2014 in preparation)

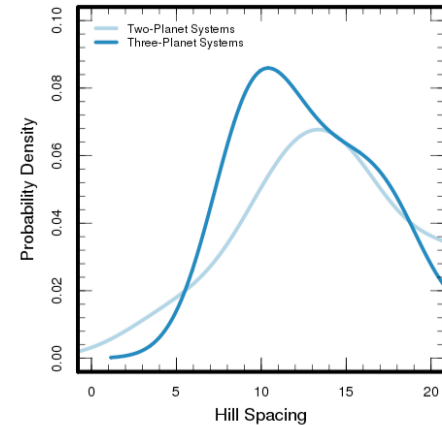
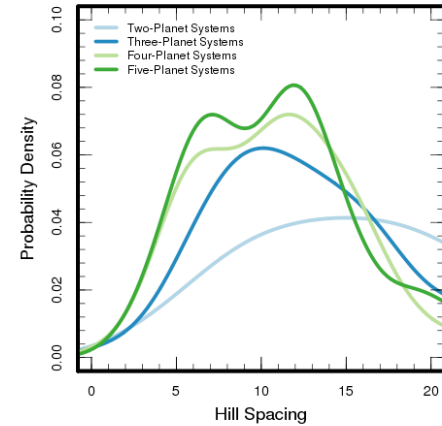
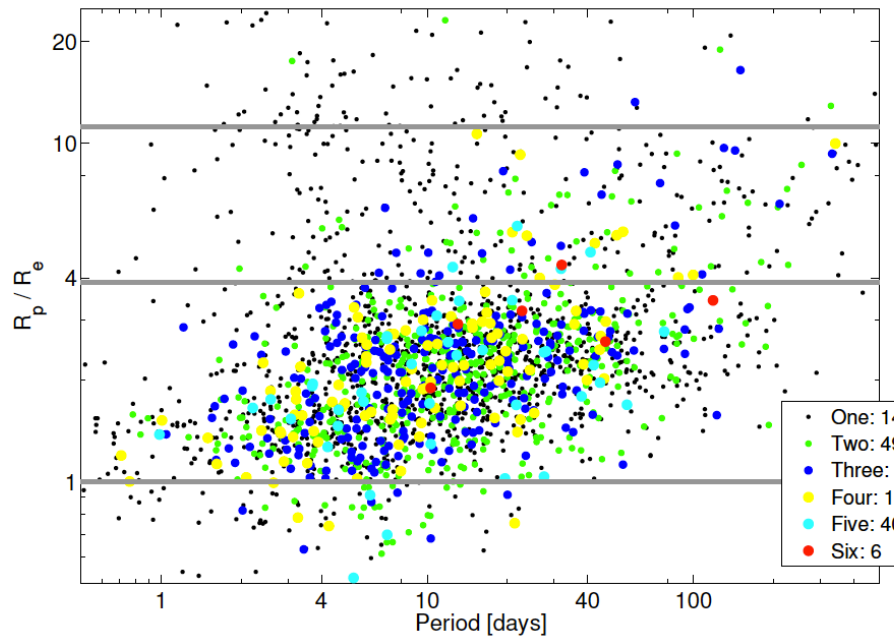

 To model P distribution of Kepler's new-found planetary candidates.

KIAA undergraduate student Ju Wenhua (Princeton) and Xu Rui (CfA, Harvard) 54/66



# New Candidate Catalog (Batalha et al. 2012)

What can we learn from Multiple systems !!!



How compact can multiple systems be?

Stability and coplanarity

Kevin Schlaufman

Xiaojia Zheng

56/66

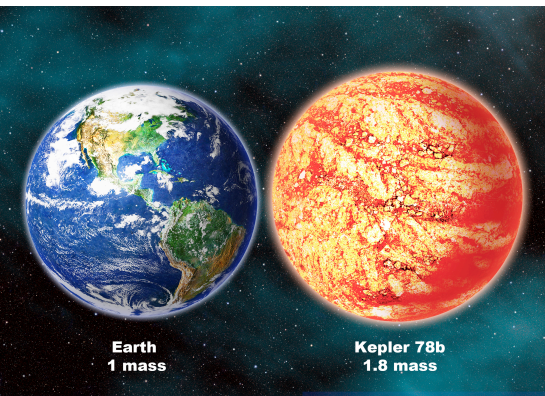
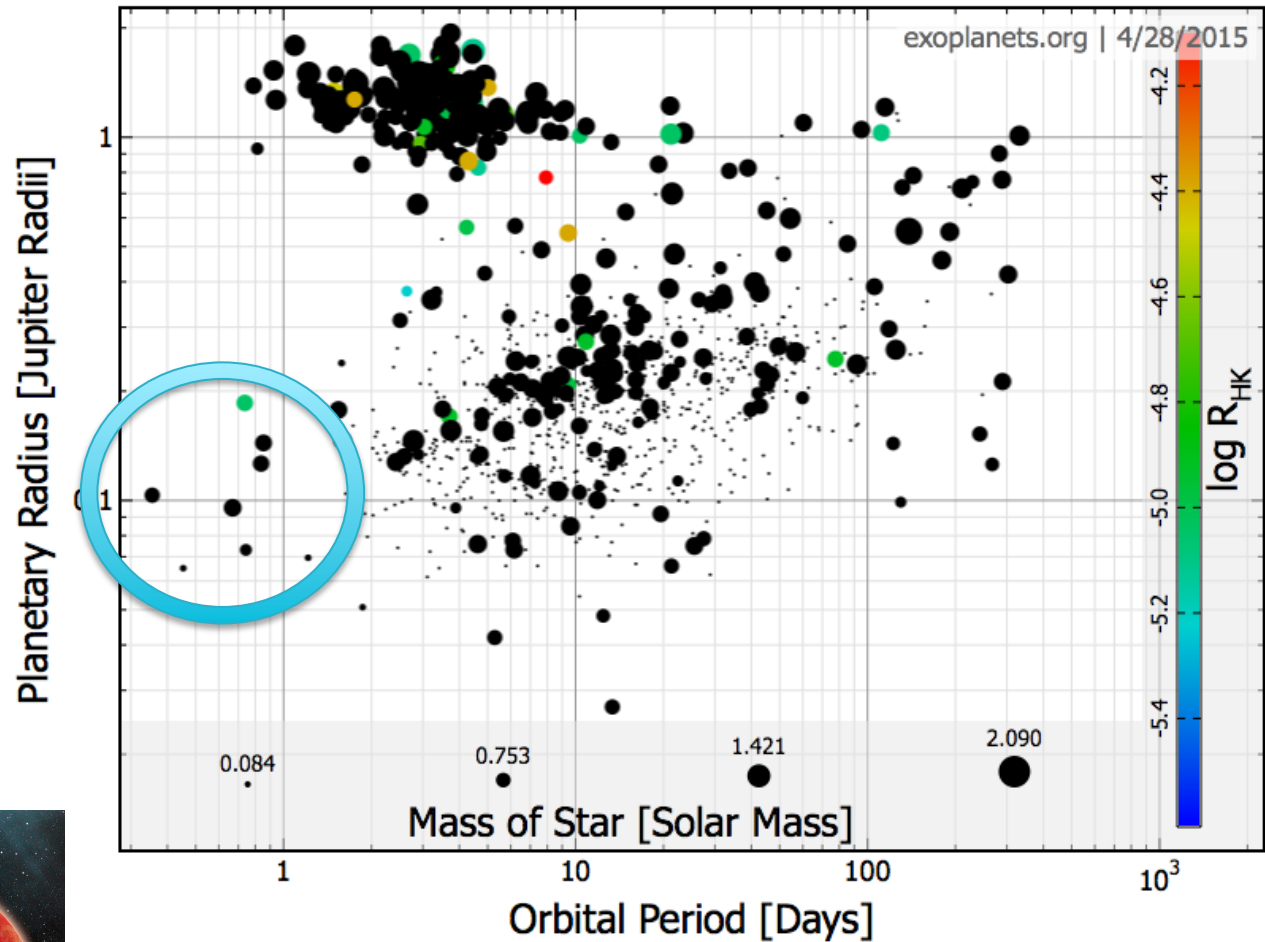




# Some major Challenges:

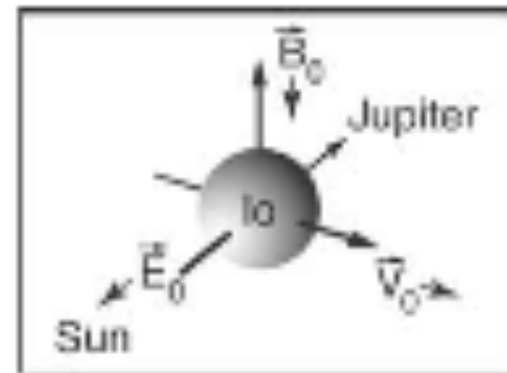
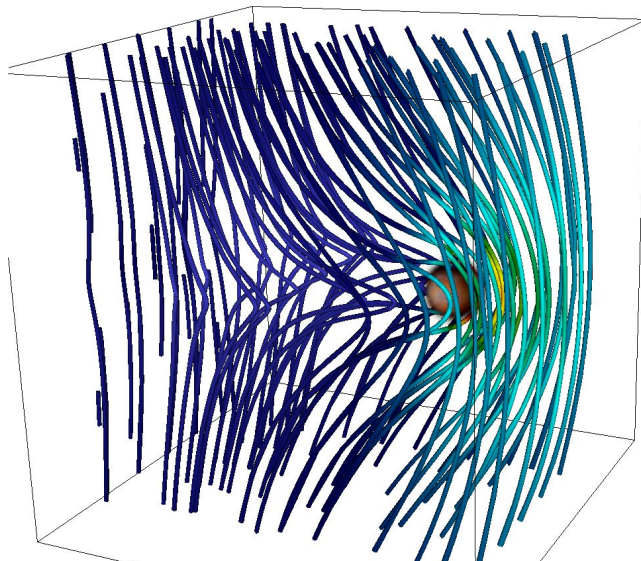
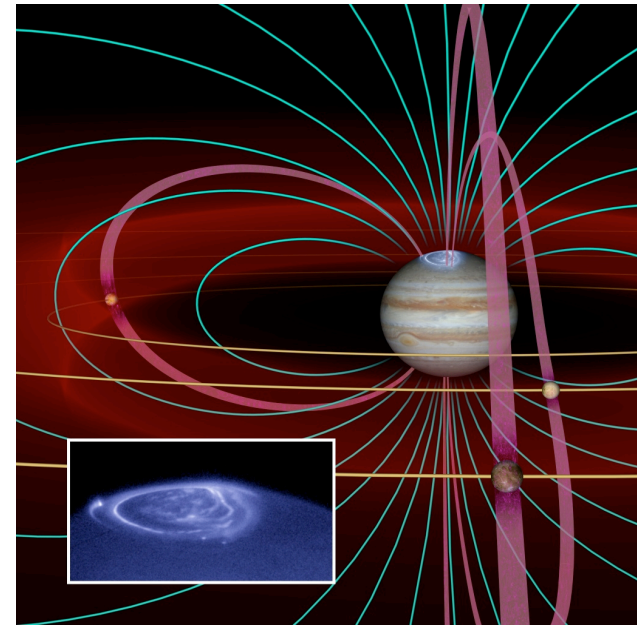
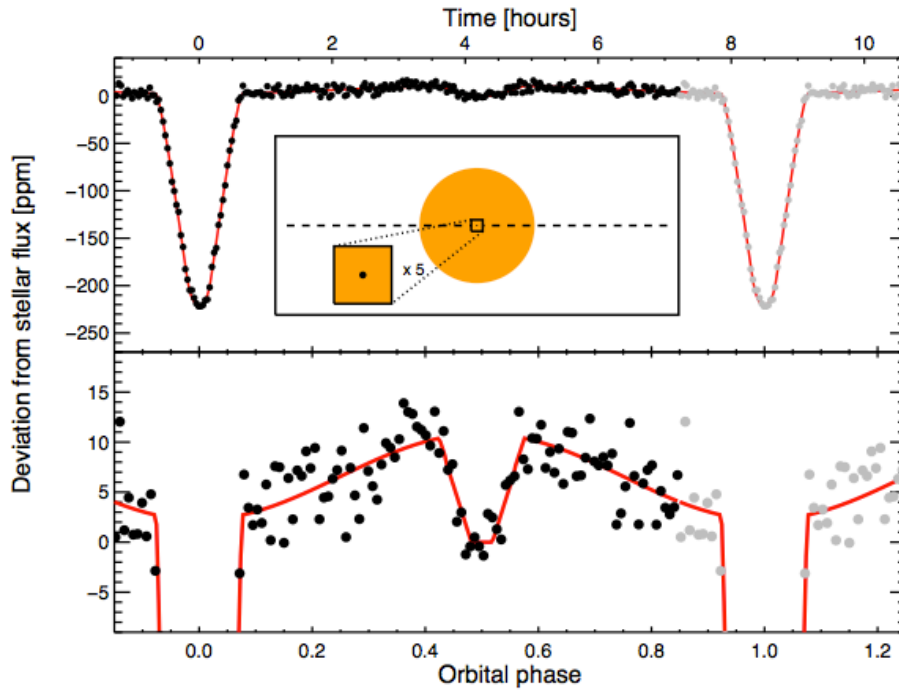
- Retention of grains: m-size barrier (Whipple)
- Fragmentation: km-size barrier (Benz)
- Planetesimal-growth barrier: Isolation mass barrier (Safronov, Wetherill), Oligarchics (Kokubo, Ida)
- Retention of embryos: type I migration (Goldreich, Tremaine, Ward)
- Proliferation of multiple, widely spread embryos
- Diversity of planetary architecture
- Onset of efficient gas accretion (Pollack, Bodenheimer)
- Multiple gas giants and eccentricity excitation
- Retention of gas giants: type II migration (Lin & Papaloizou)
- Multiple planets: rapid & slow depletion of disk gas
- **Competing physics on multiple length & time scales**

# Close-in super Earths

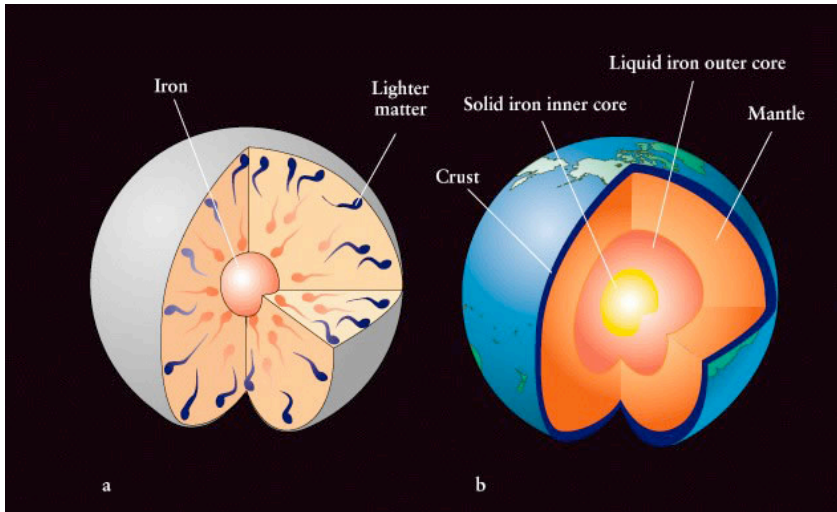


# Inside the stellar magnetosphere

Kepler-78b



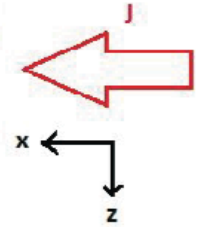
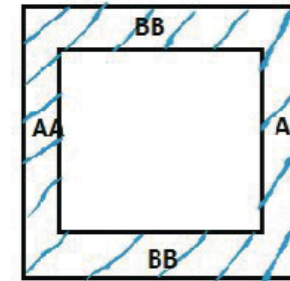
# Geology and conductivity



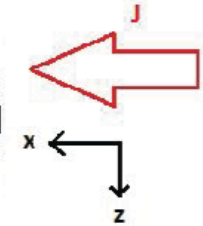
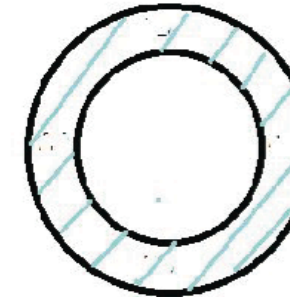
□ High conductivity region

▨ High resistivity region

Electric conductivity depends only on height, i.e. on  $x$  in AA and on  $z$  in BB



Electric conductivity depends only on radius



$$\mathcal{R}_p^{-1} = \int_{z=0}^{R_{max}} \int_{y=0}^{\sqrt{R_{max}^2 - z^2}} dy dz \left( \int_{x=0}^{\sqrt{R_{max}^2 - z^2 - y^2}} \frac{dx}{\sigma_p(r)} \right)^{-1}$$

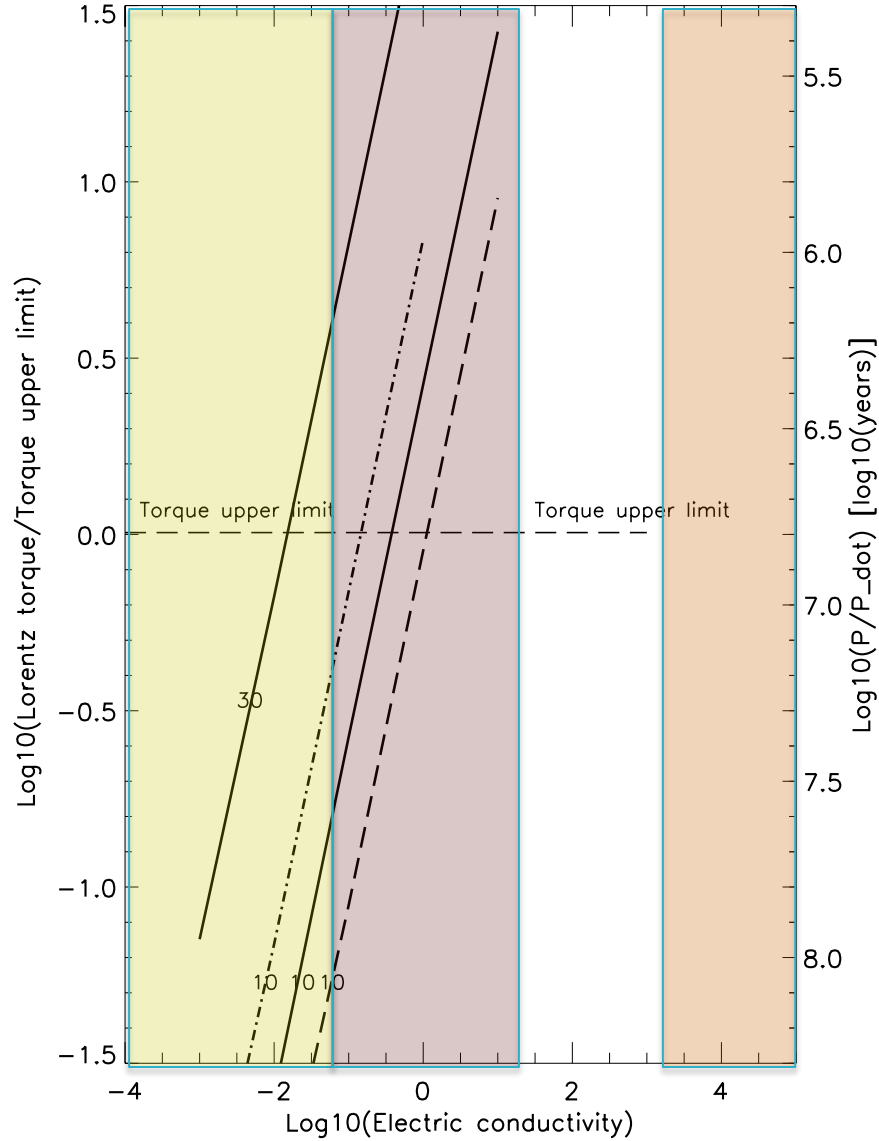
$$\mathcal{R}_\perp = \left( [2s] \int_z \sigma(z) dz \right)^{-1}$$

$$\mathcal{R}_\parallel = \frac{1}{R_p^2} \int_z \frac{dz}{\sigma(z)}$$

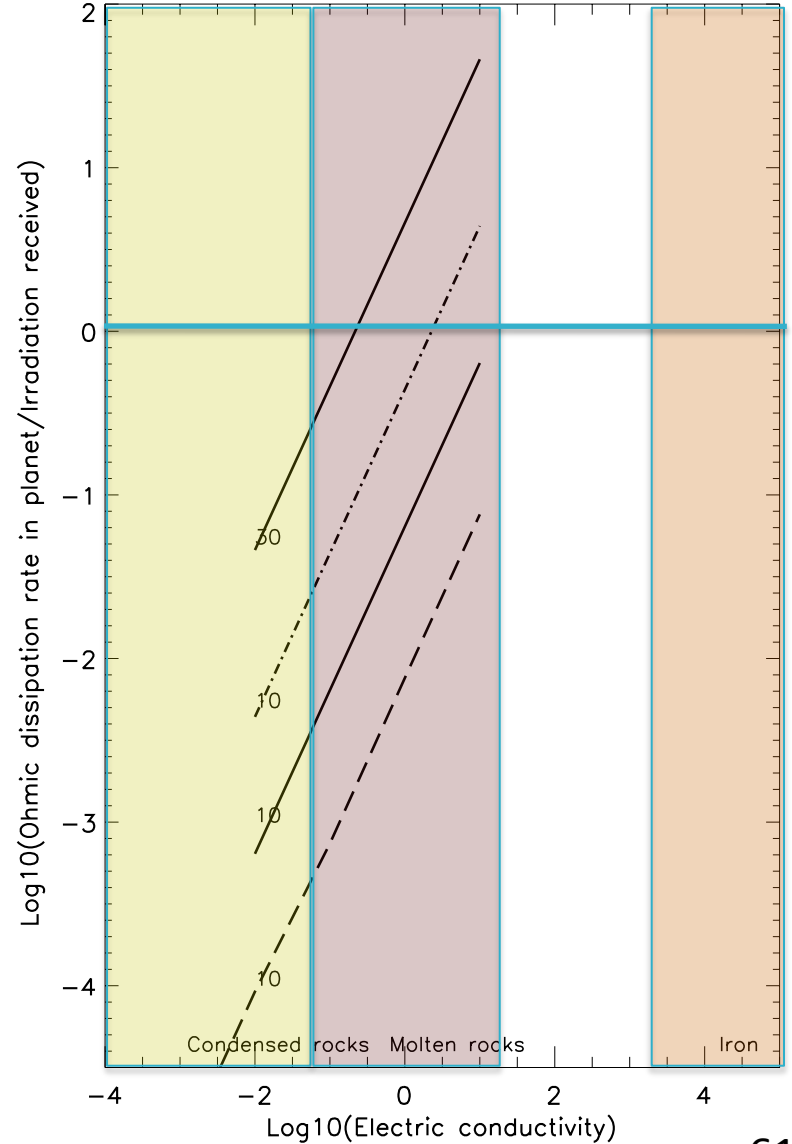
$$\mathcal{R}_\perp = (2/R_p) 1/[\sigma(inner) + \sigma(outer)] \text{ and } \mathcal{R}_\parallel = (1/2R_p)[1/\sigma(inner) + 1/\sigma(outer)].$$

# Torque and power

Torque on the planet



Ohmic dissipation rate on the planet



# Foot prints and stellar spots

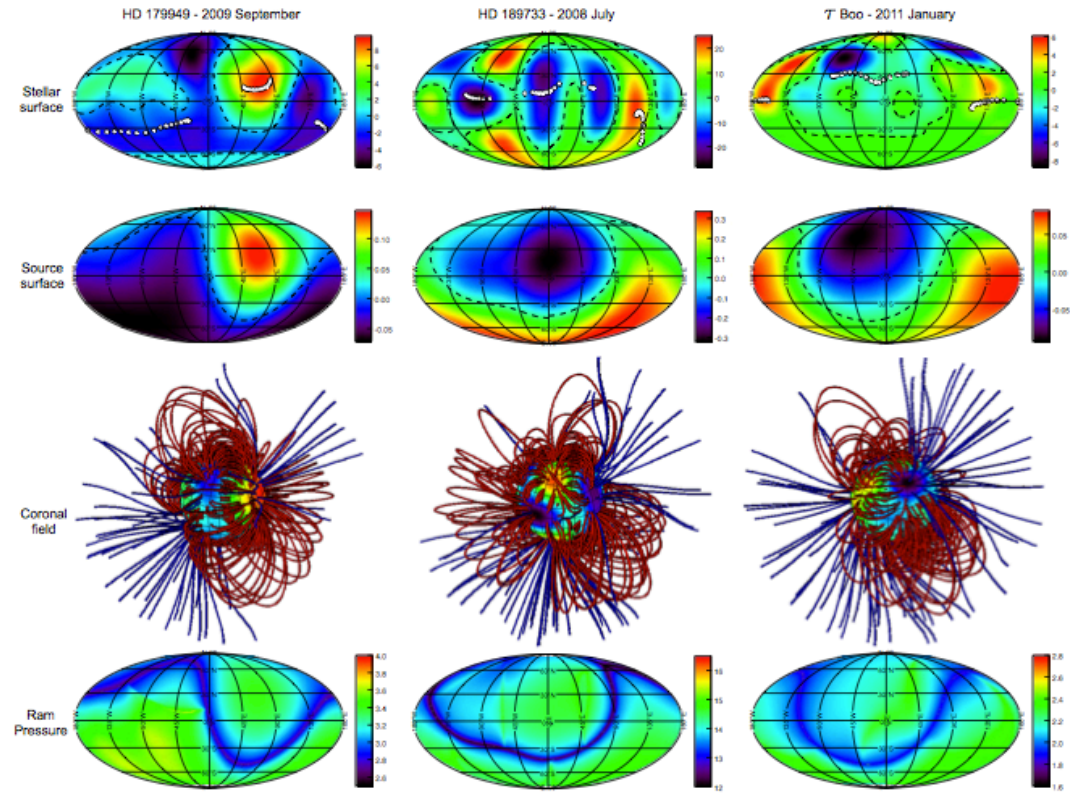
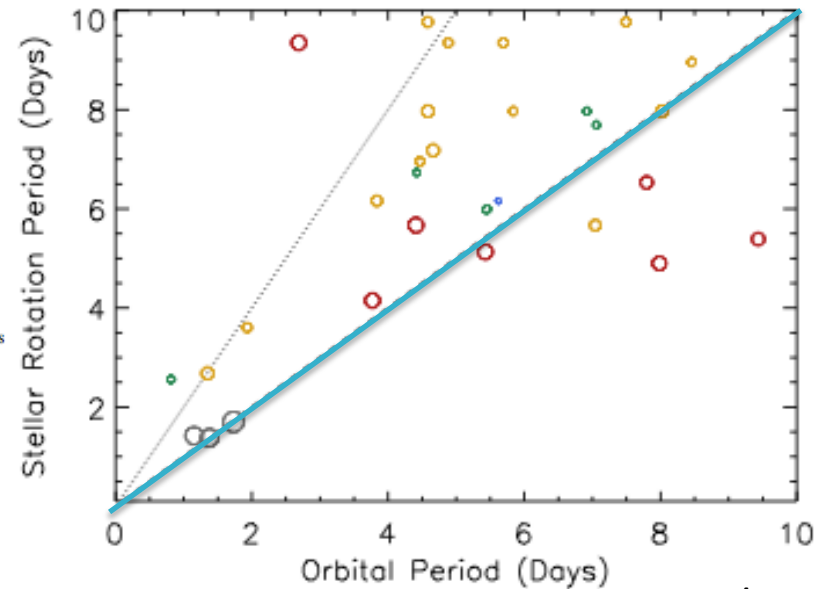
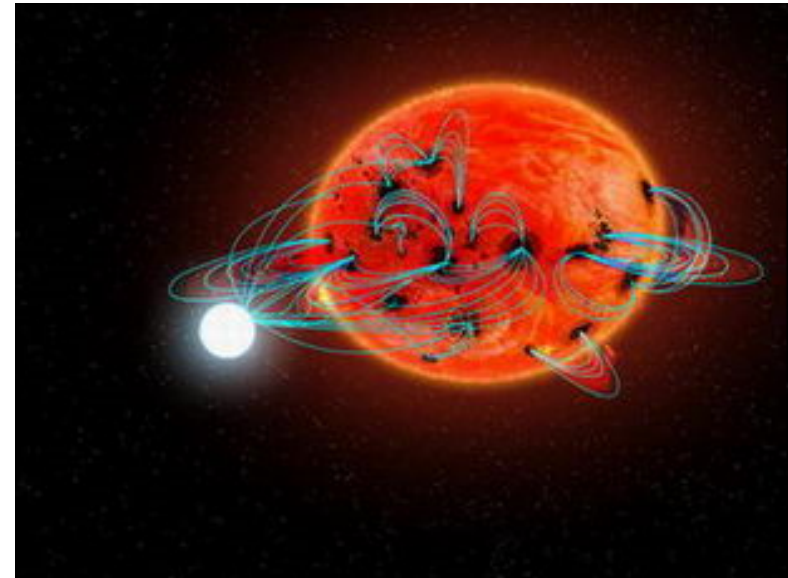


Figure 1. Examples of the magnetic field geometries of HD 179949 (2009 September), HD 189733 (2008 July), and  $\tau$  Boo (2011 January). For each star, maps



See et al 2015

# Other issues

Late-stage evolution in debris disks

Post formation dynamical evolution

Non planar planetary systems

Planets around different mass stars

The role of elemental differentiation in natal disks

Planets in binary stars

Planets around stars in clusters

Planets' magnetic and tidal interaction with their host stars

Planets' consumption by their host stars

Planets' survival around evolved stars

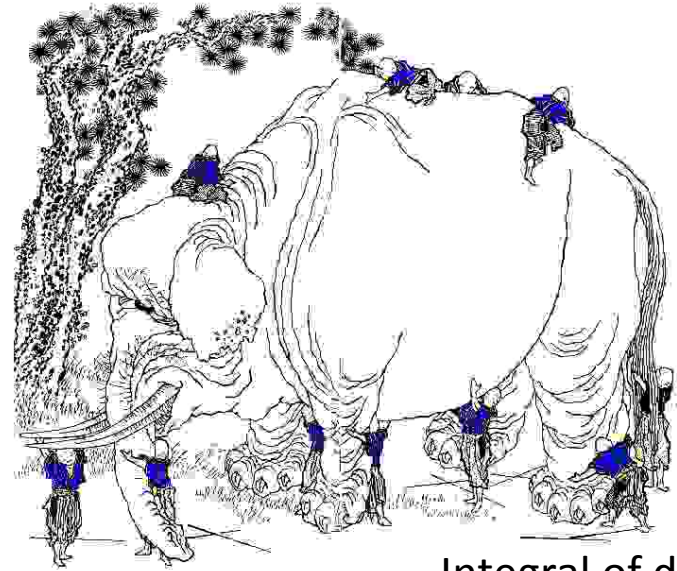
Planets' internal structural evolution

Planets' atmospheric dynamics

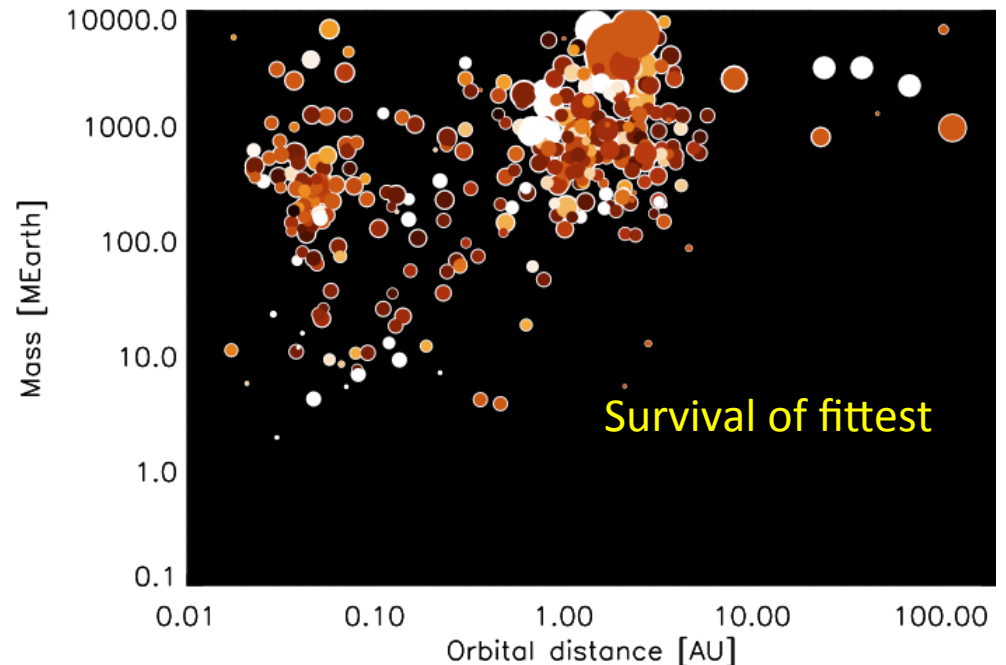
How is habitability affected by dynamical interaction between planets

# Precision COSMOGONY

- Ubiquity of planets:  
case study vs **Science**
- Diversity of systems:  
realm of possibilities
- Population census  
missing info & big picture
- Solar system connection  
Anthropic principle

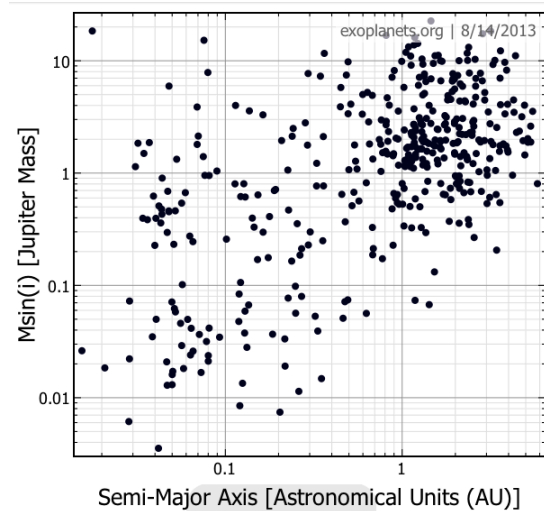
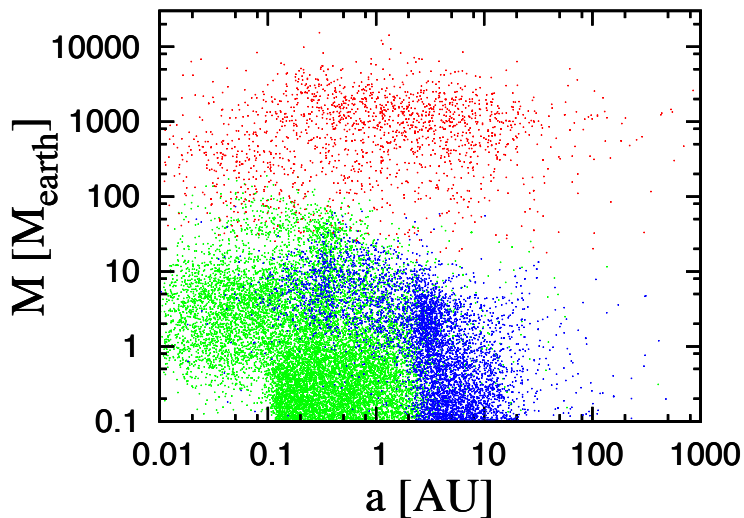
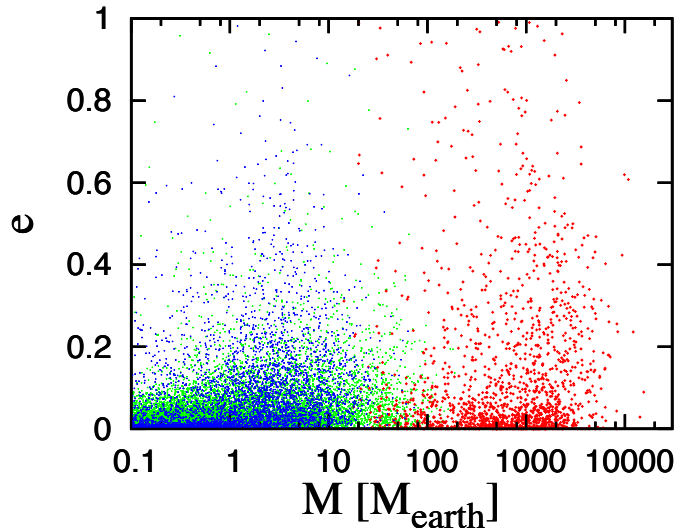
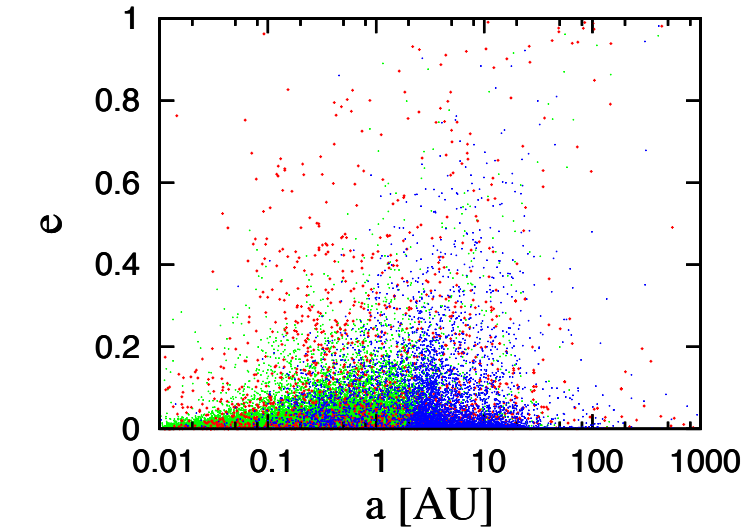


Integral of details





# Updated version of population synthesis models



# Summary

- Planet formation is a robust process and their dynamical architecture is diverse.
- Planetary origin and destiny are determined largely by the structure & evolution of the disks.
- **Migration** due to planet-disk interaction played a big role in the asymptotic properties of the planets.
- Theory of planetary astrophysics is relevant to many other astrophysical contexts.

