

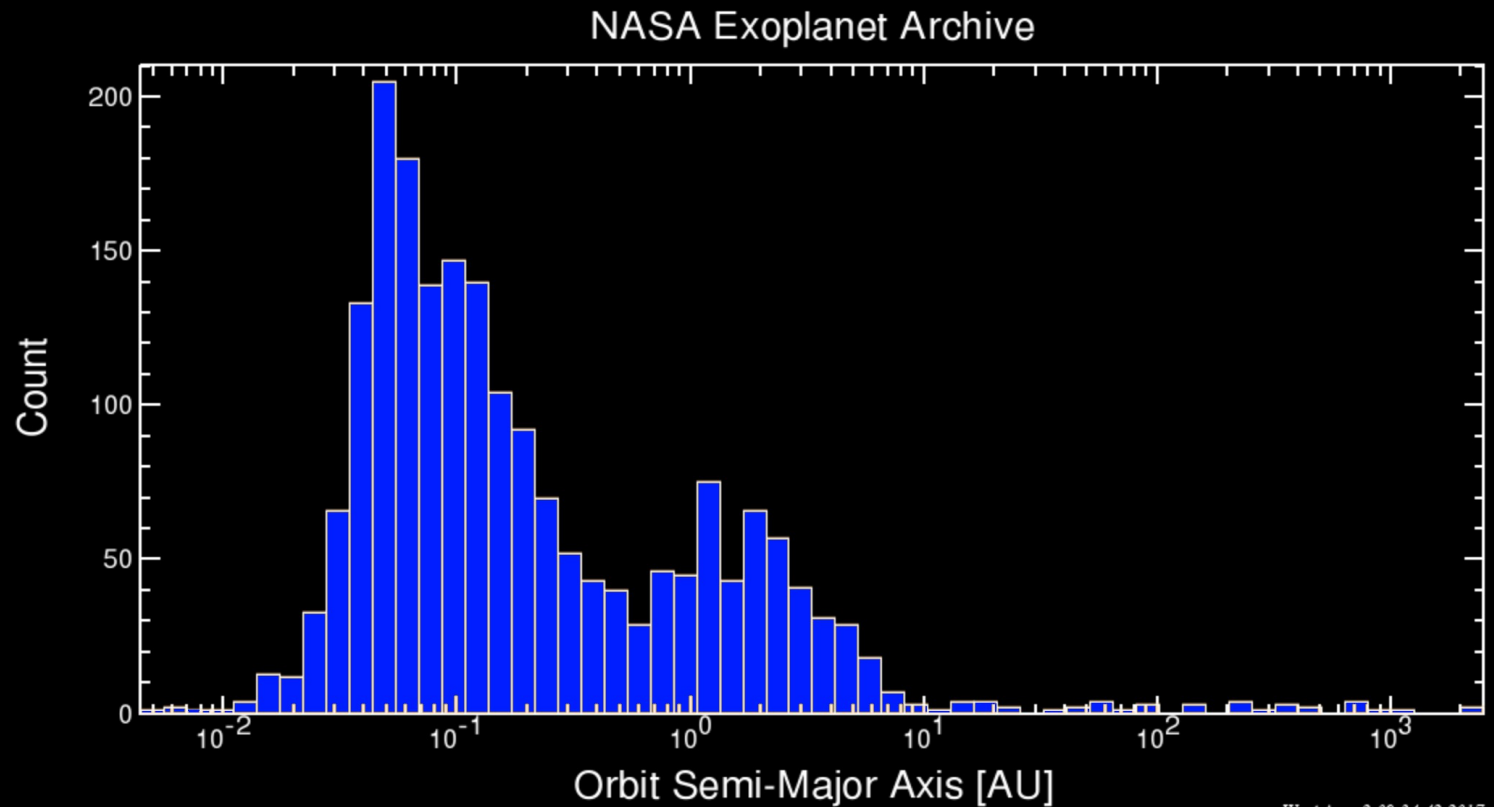
# Introduction to Microlensing Theory and Observations

Rachel Street

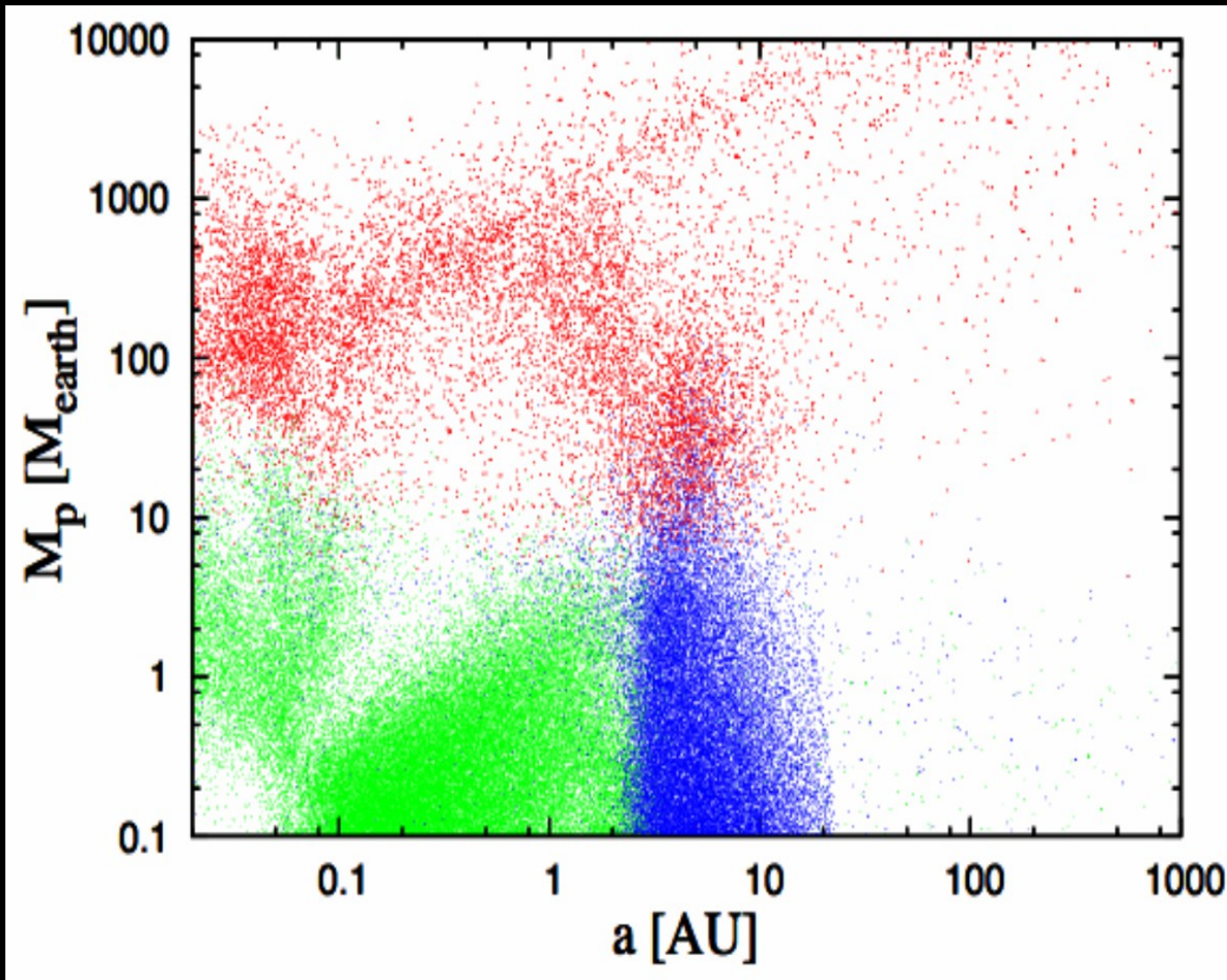
# Exoplanet Discovery Space

*In the last 25 years, we've found ~3,500 planets.*

*What's so important about microlensing?*



# Microlensing Discovery Space



**Synthetic  
distribution of  
planets when  
protoplanetary  
nebula vanishes**

*From Ida et al. 2013*

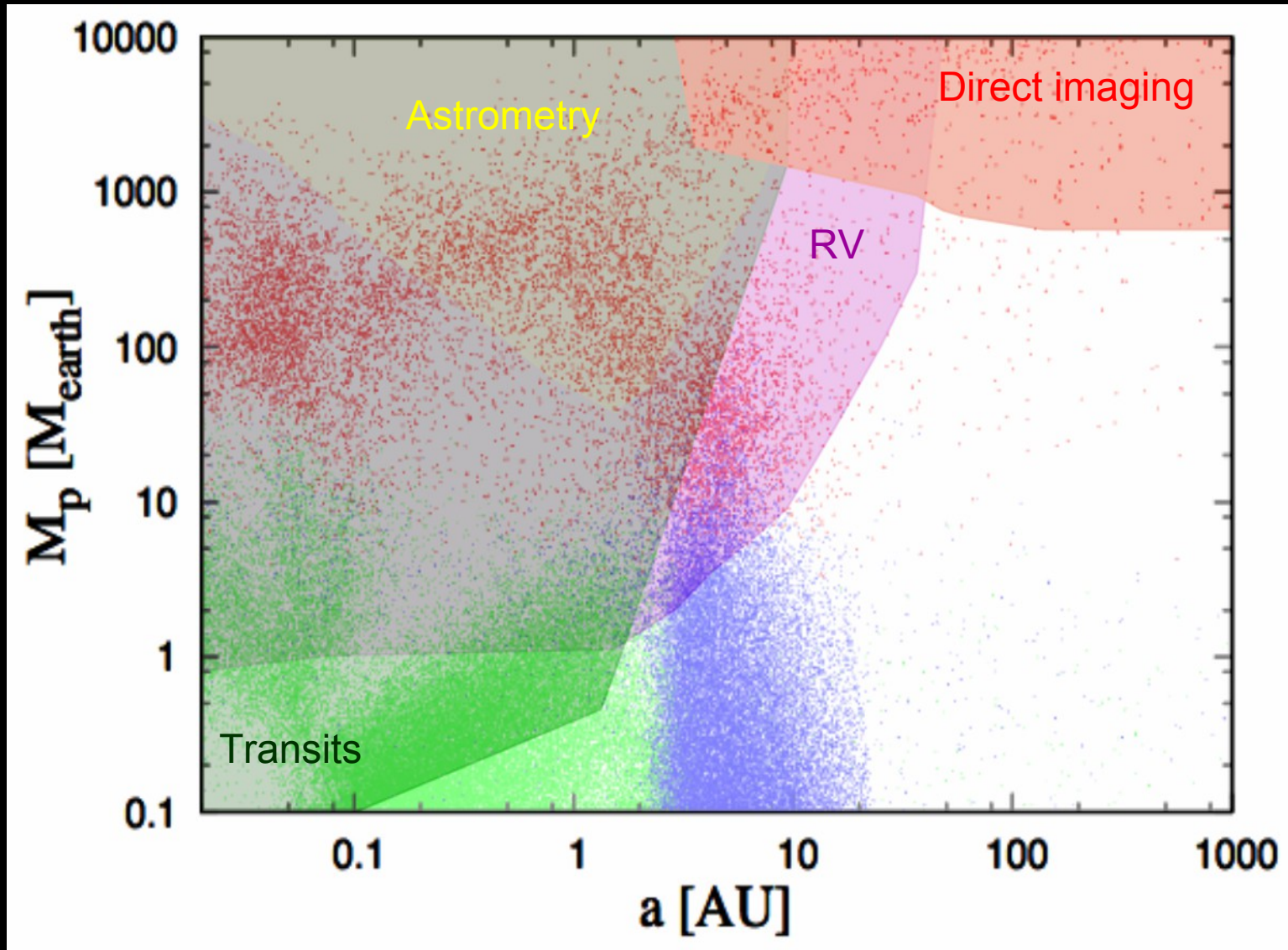
Rocky planets/low  
mass gas envelope

Icy planets/low  
mass gas envelope

Giant  
planets/massive gas  
envelope

# Microlensing Discovery Space

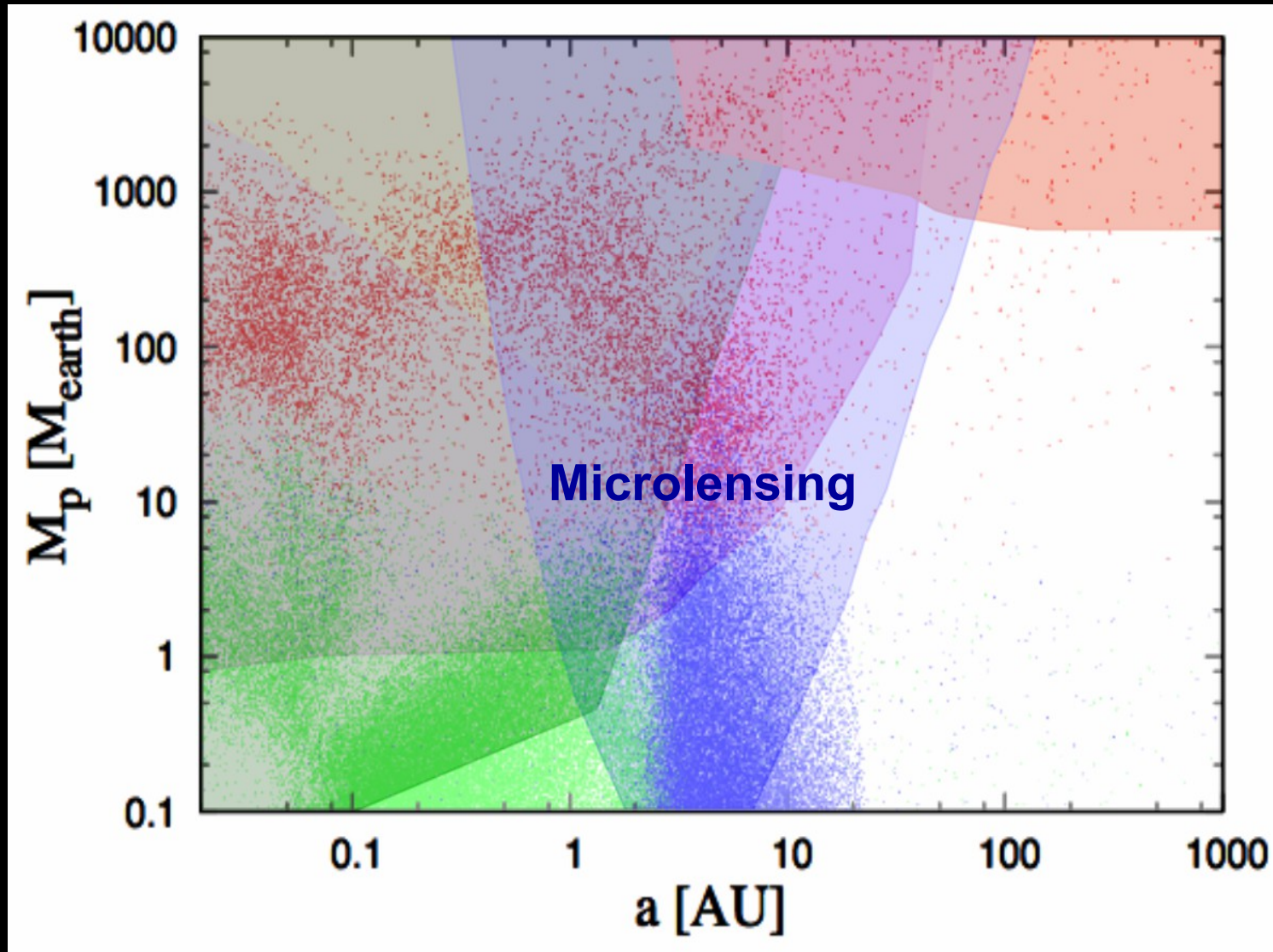
Approximate sensitivities of exoplanet detection techniques





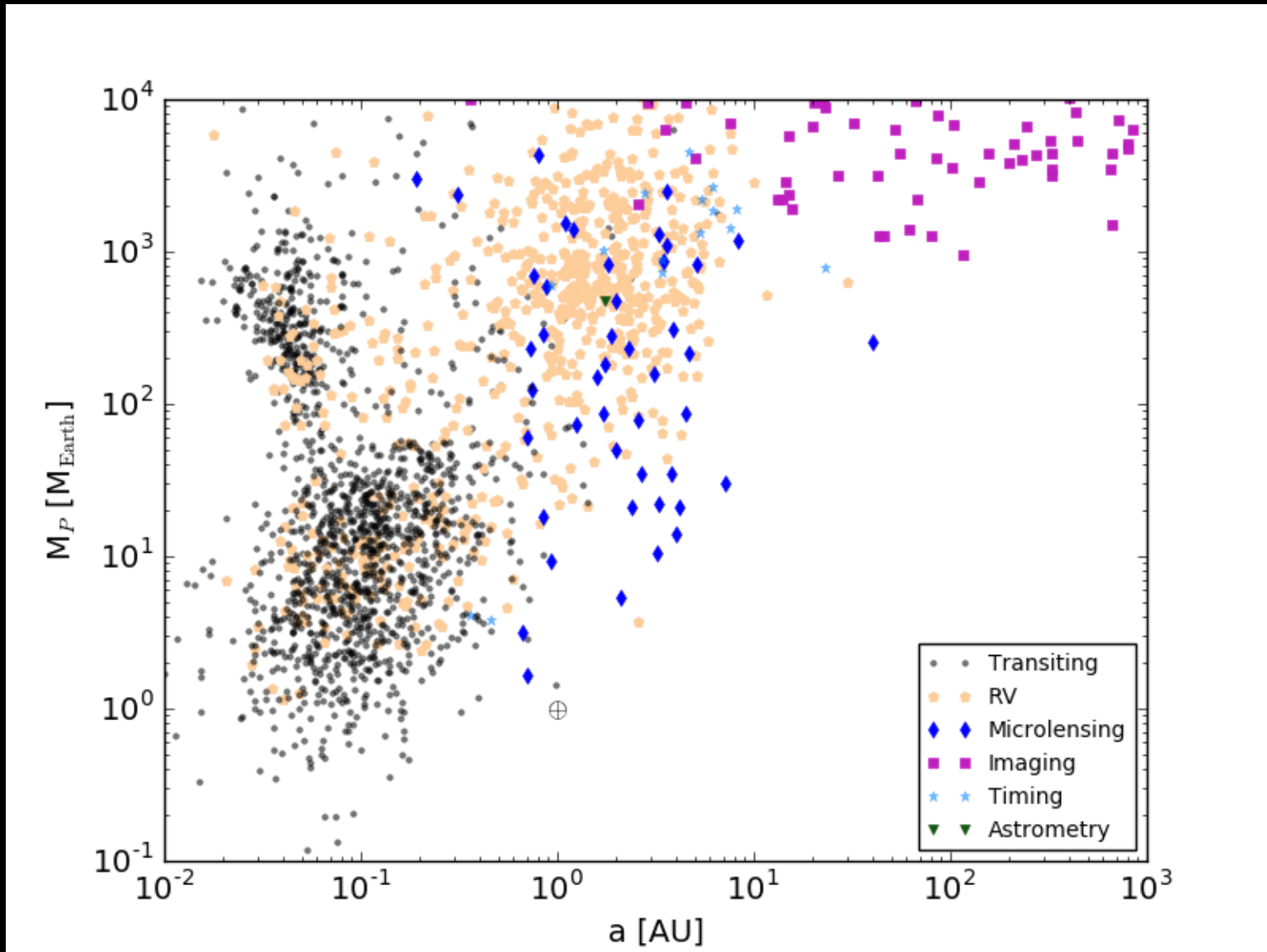
# Microlensing Discovery Space

Approximate sensitivities of exoplanet detection techniques

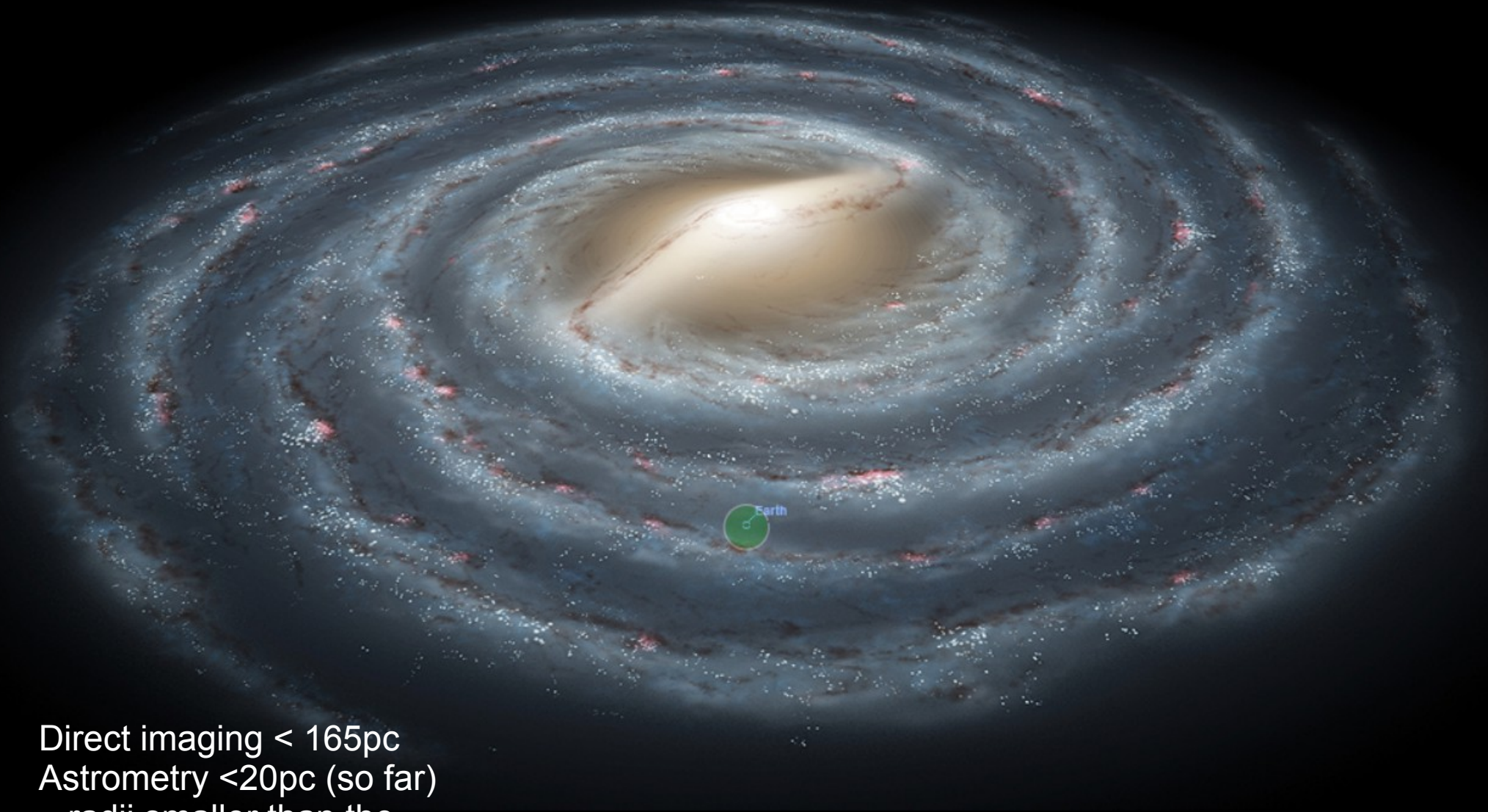


# Microlensing Discovery Space

Actual exoplanet detections by various techniques



# Microlensing Discovery Space

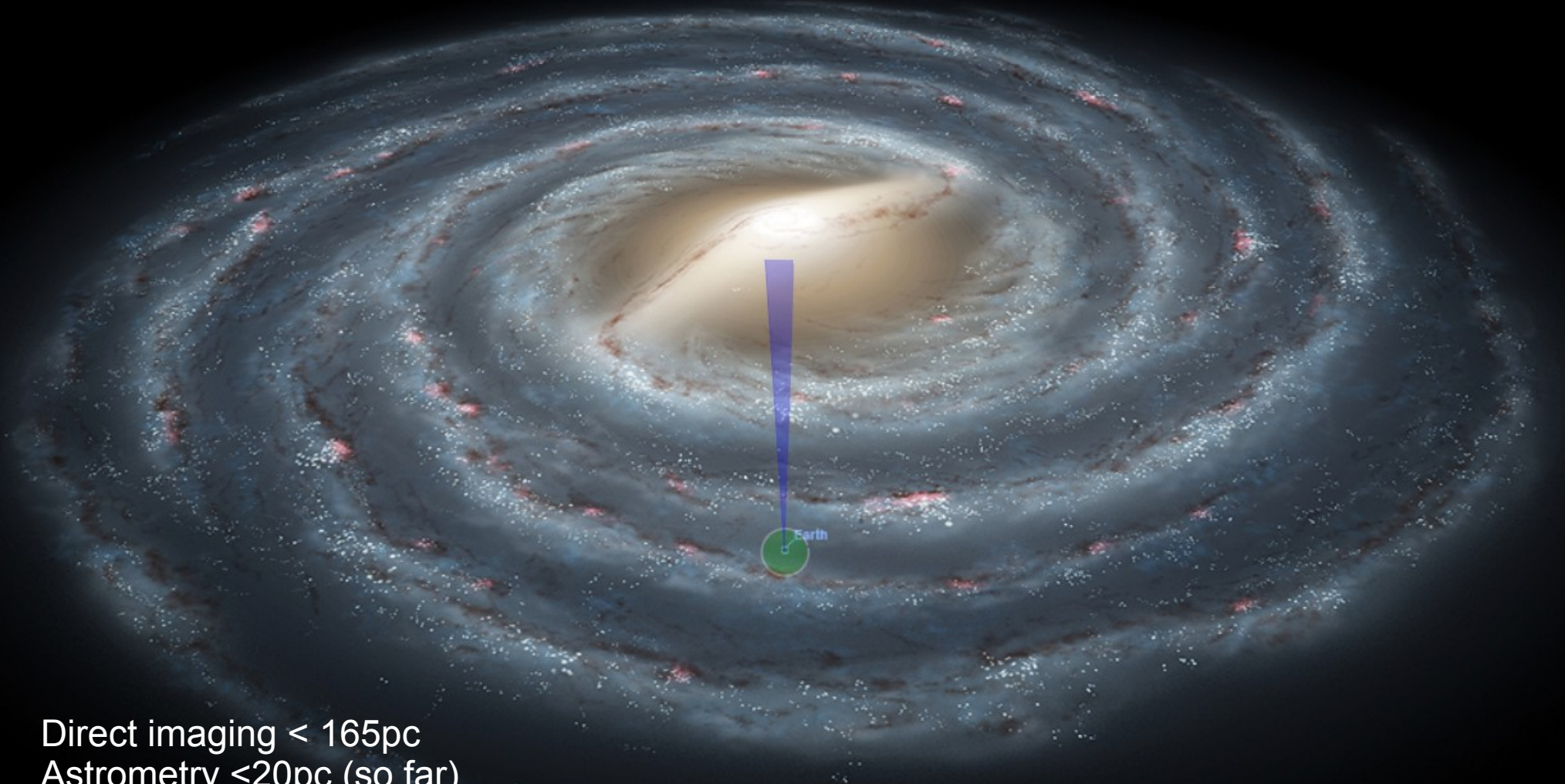


Direct imaging < 165pc  
Astrometry <20pc (so far)  
...radii smaller than the  
“Earth” circle

Transits/RV detections out to ~1300pc



# Microlensing Discovery Space



Direct imaging  $< 165\text{pc}$   
Astrometry  $< 20\text{pc}$  (so far)  
...radii smaller than the  
“Earth” circle

Transits/RV detections out to  $\sim 1300\text{pc}$   
Microlensing detections to  $\sim 8200\text{pc}$



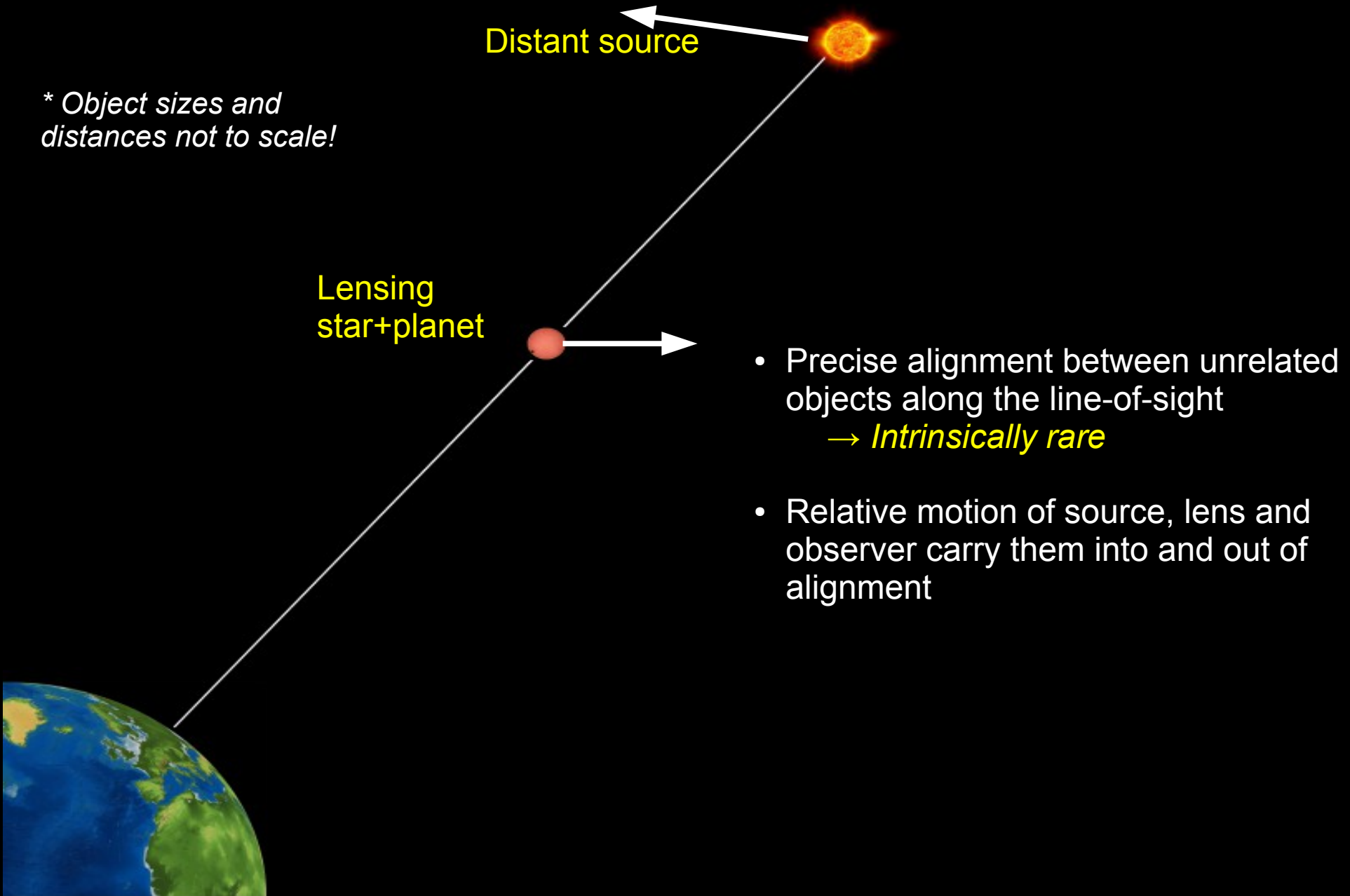
# Microlensing Discovery Space

Microlensing is sensitive to planets of all masses at separations of  $\sim 1-10$  AU, filling a critical gap between the sensitivities of other discovery techniques

It is capable of exploring planet formation in different stellar environments throughout the galaxy

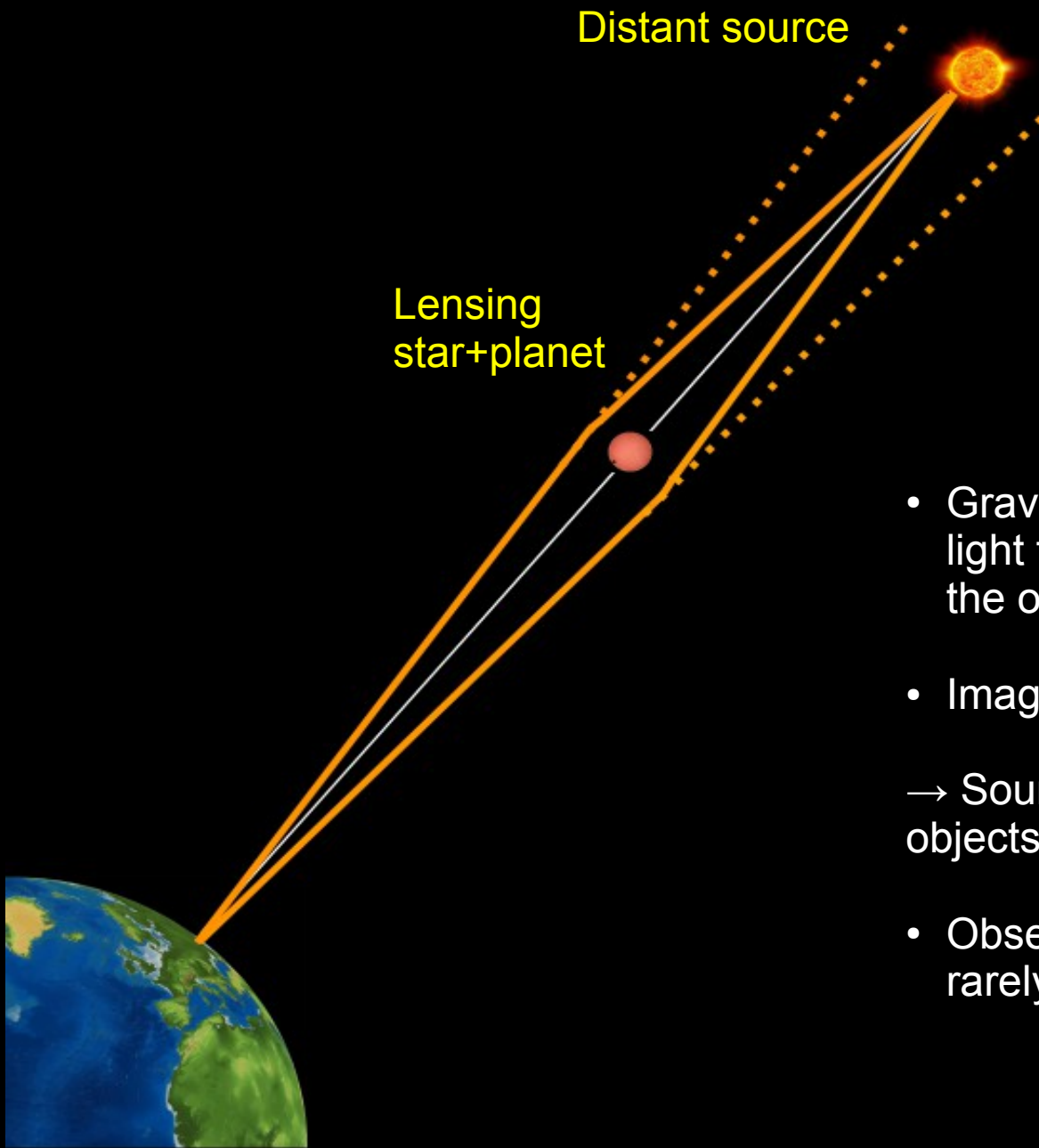
# Observing Microlensing Events

\* Object sizes and distances not to scale!



- Precise alignment between unrelated objects along the line-of-sight  
→ *Intrinsically rare*
- Relative motion of source, lens and observer carry them into and out of alignment

# Observing Microlensing Events

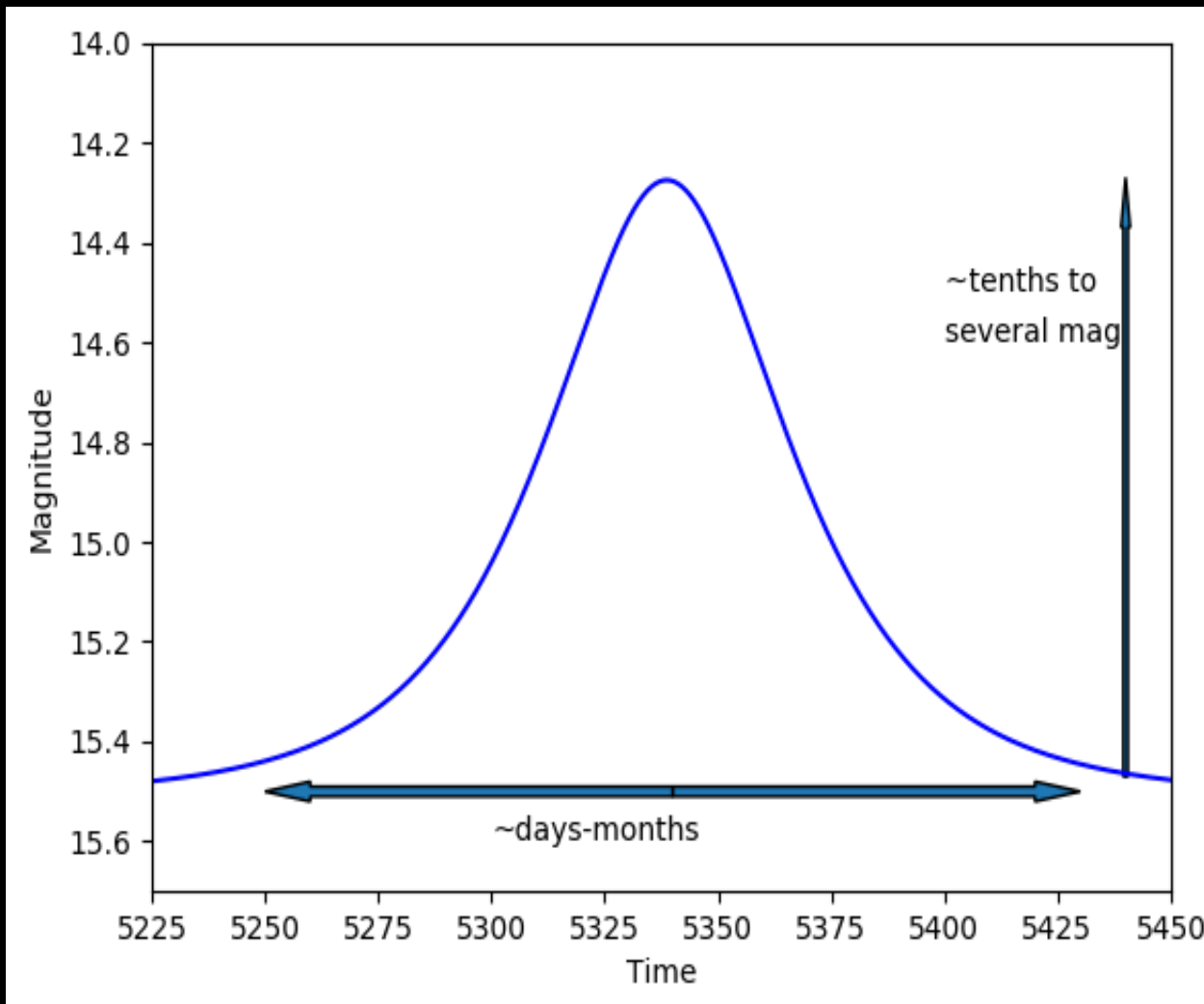


- Gravity of the lensing body deflects the light from the source. More of it reaches the observer
- Images of the source are created
- Source appears to brighten and fade as objects move into/out of alignment
- Observe only light from the source – very rarely from the lens



# Microlensing lightcurves

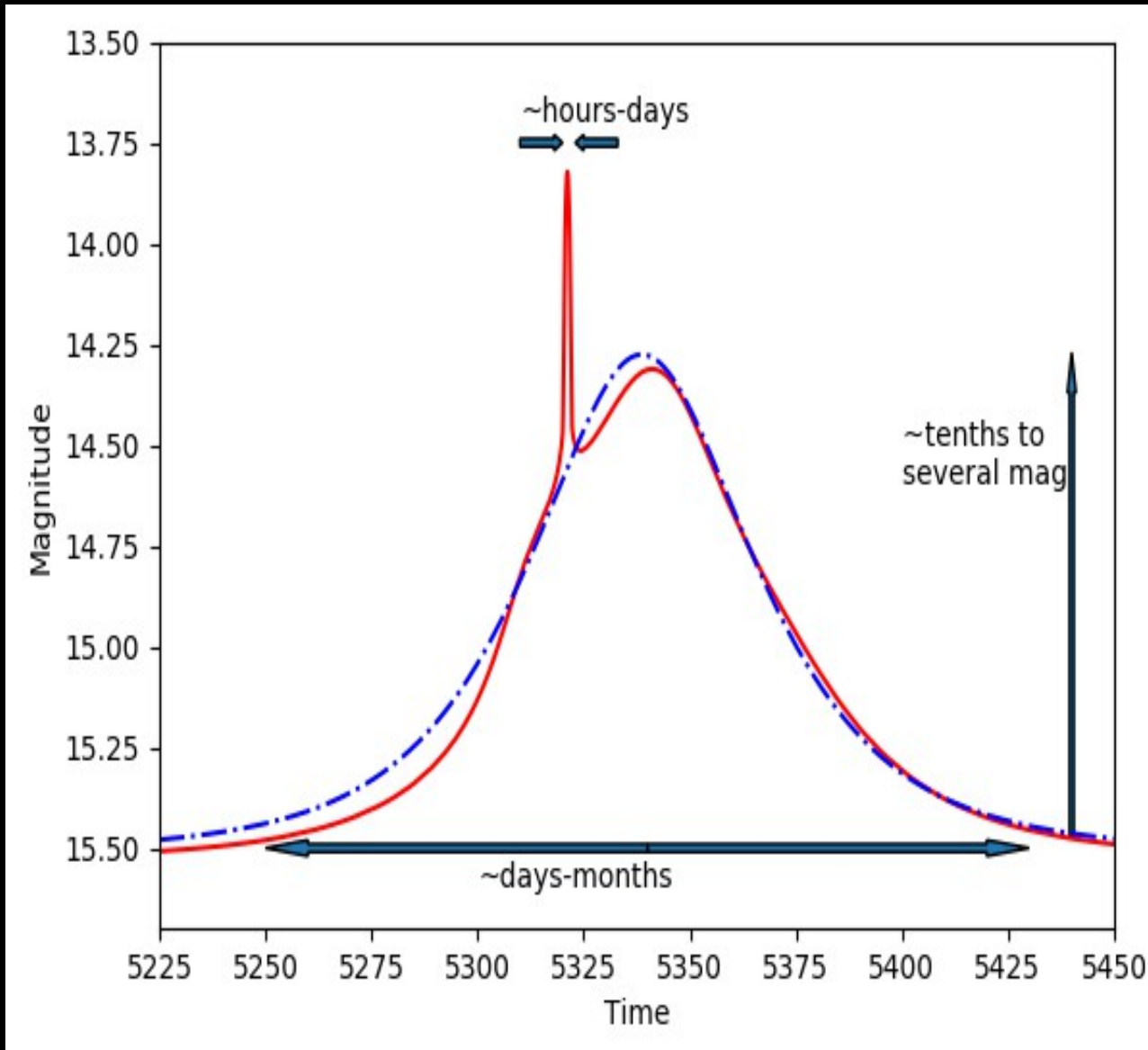
## *Single-object lens*



- Magnification depends on angular separation *not* lens mass
- All wavelengths are magnified by the same amount

# Microlensing lightcurves

## *Star + planet lens system*



Presence of a 2<sup>nd</sup> mass causes additional lensing during the event



Deviation from the smooth single-lens curve

= 'anomaly'

# Microlensing Targets

Intrinsically rare events, small probability of alignment

→ need to monitor many potential source stars

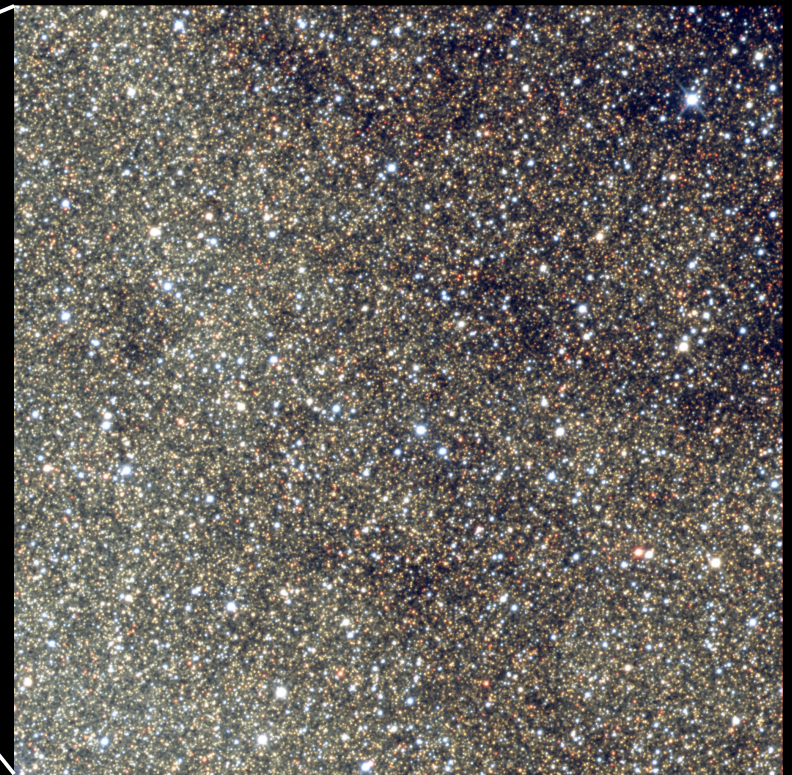


From OGLE

Introduces observational limitations:

Blending

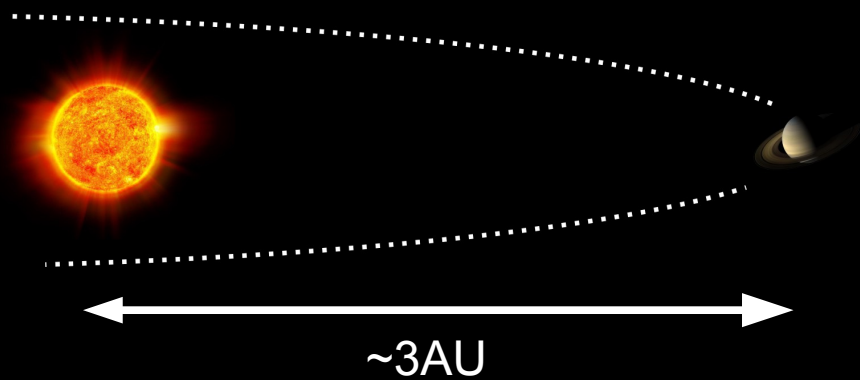
Extinction



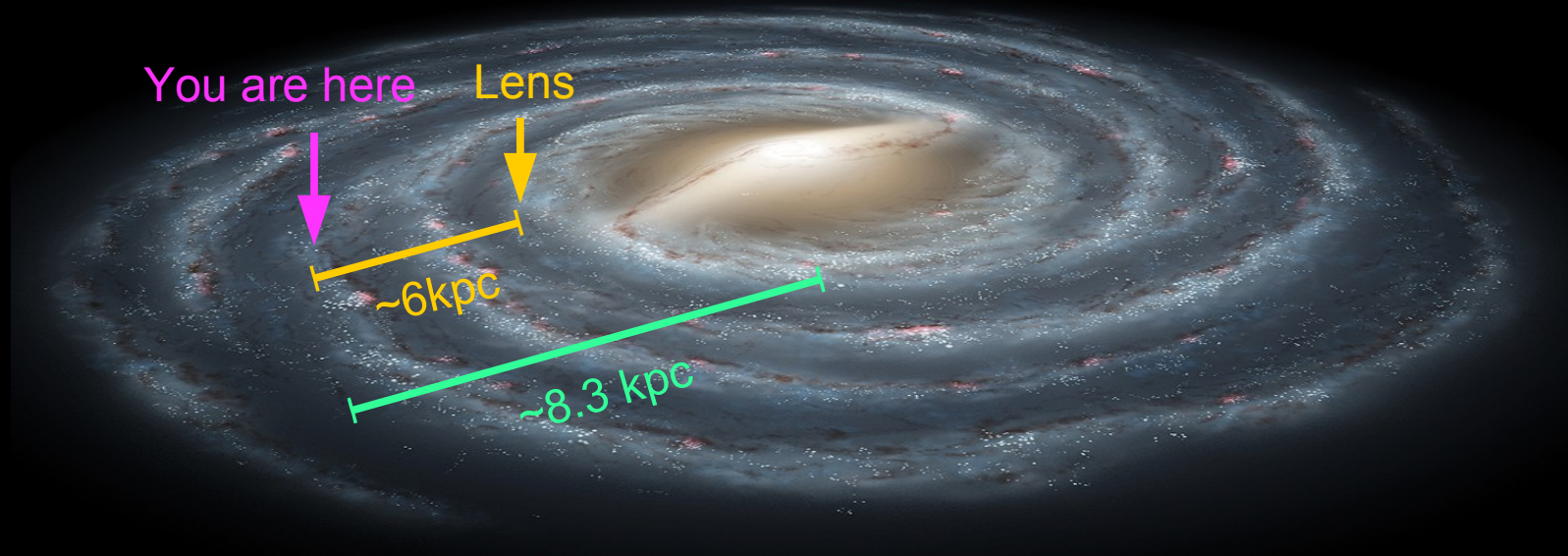
From LCO



# “Typical” exoplanetary system discovered by microlensing



A Saturn-mass planet in a  $\sim 3\text{AU}$  orbit around an M dwarf,  $\sim 6\text{ kpc}$  from Earth toward the Galactic Bulge.



# Microlensing Observations

Microlensing depends on the coincidental alignment of a foreground planet system with a background source

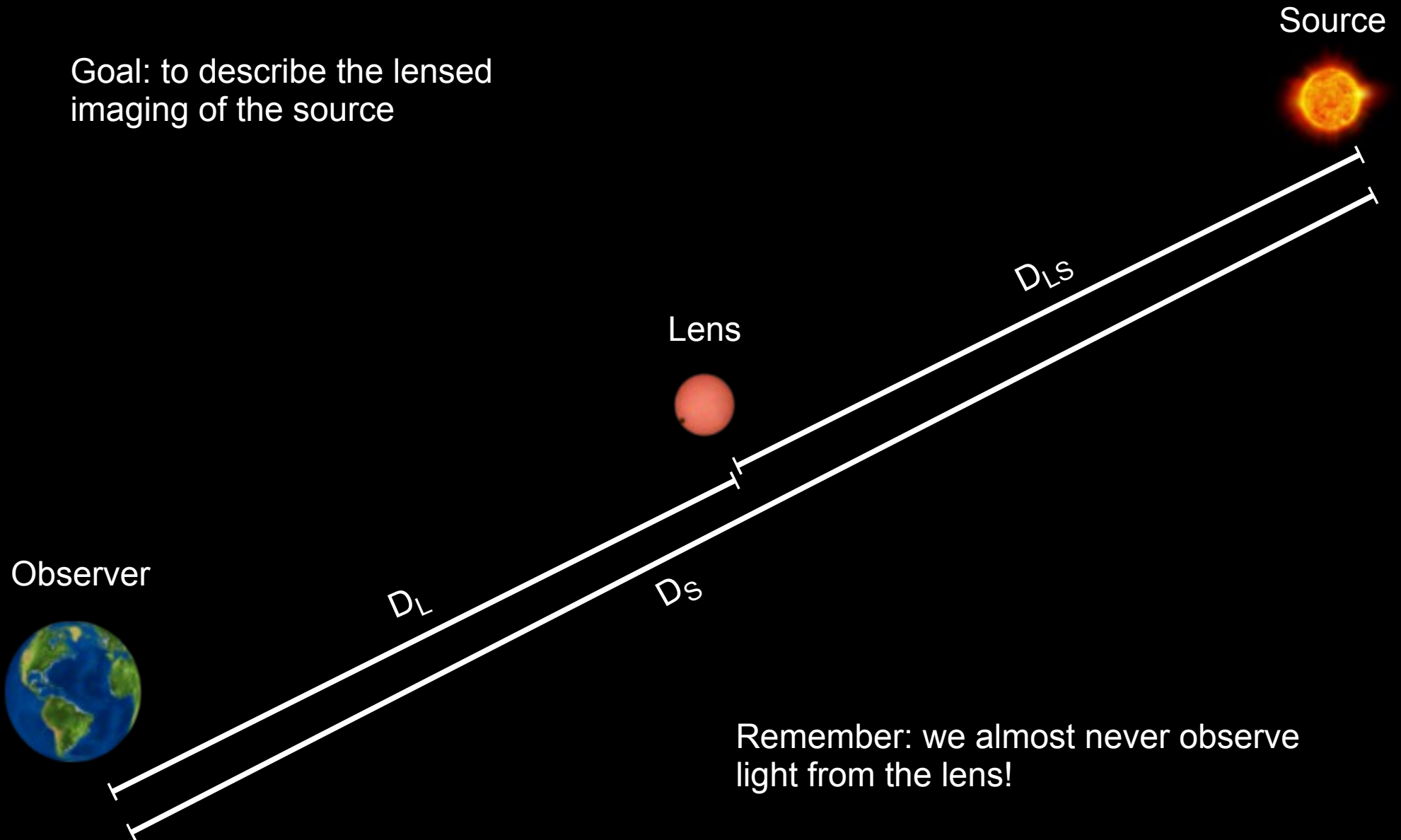
The gravity of the foreground system causes more light from the source to reach the observer, so it appears to brighten and fade over time

Gravity bends all wavelengths of light equally, so microlensing is independent of passband

Planets can be found around the foreground system by looking for rapid deviations ('anomalies') from a smooth lensing lightcurve

# Distance Scales

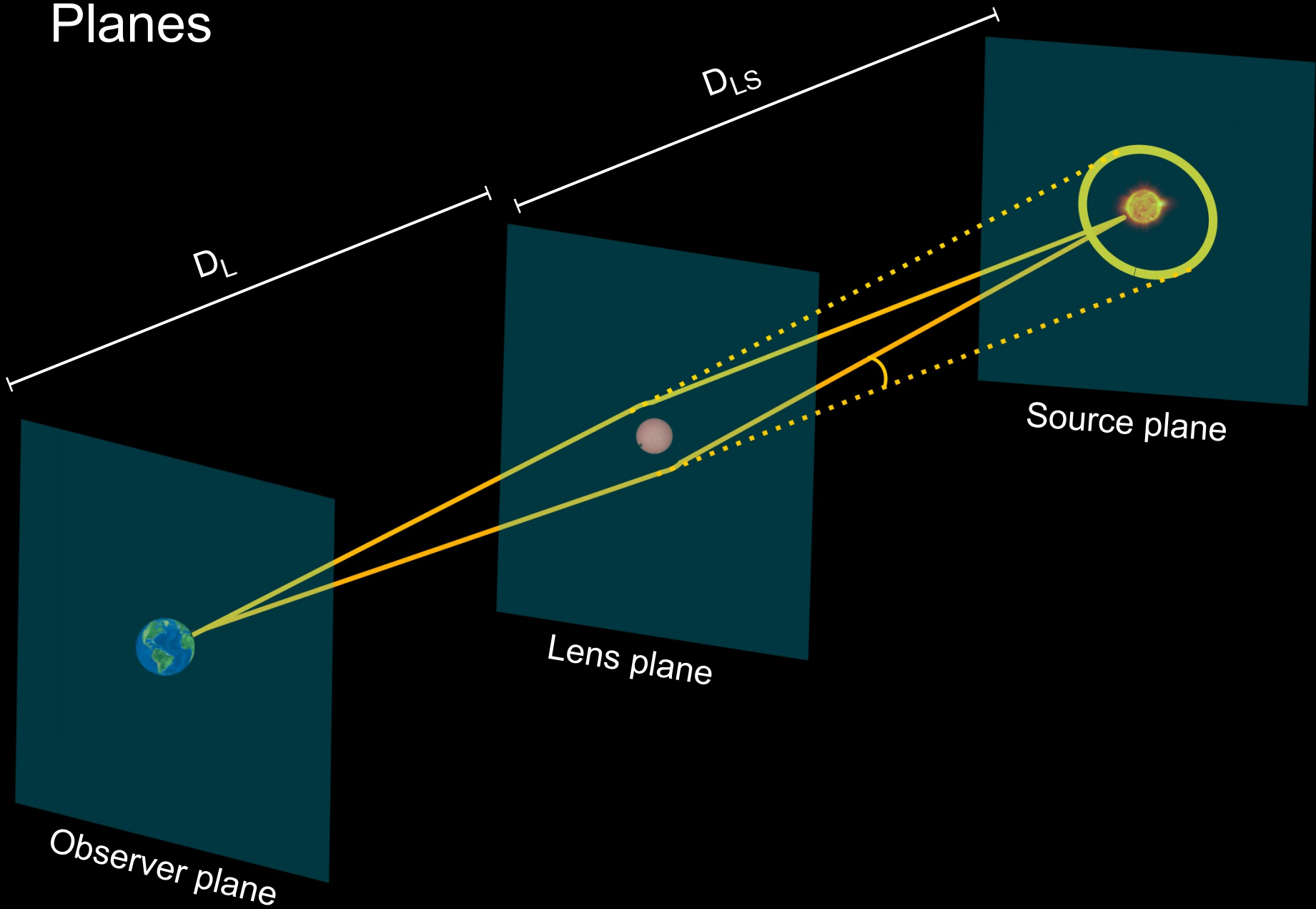
Goal: to describe the lensed imaging of the source



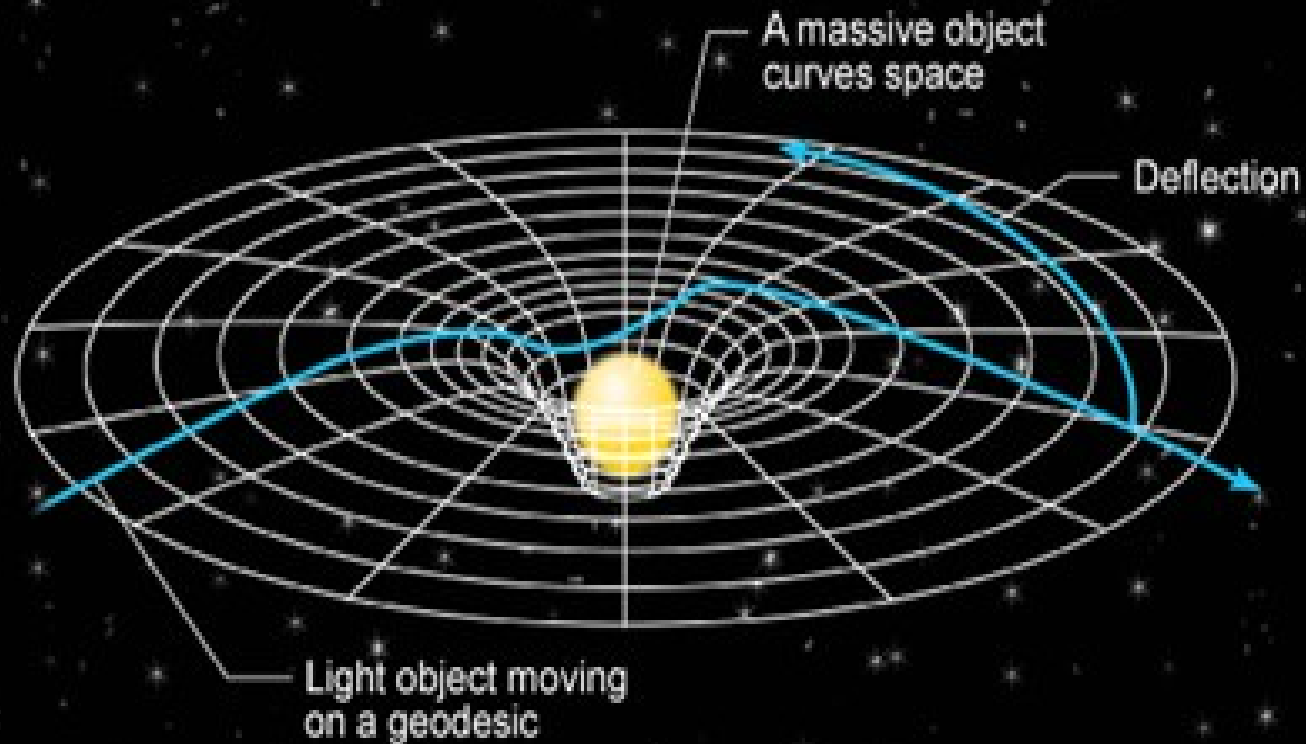
Remember: we almost never observe light from the lens!



# Planes



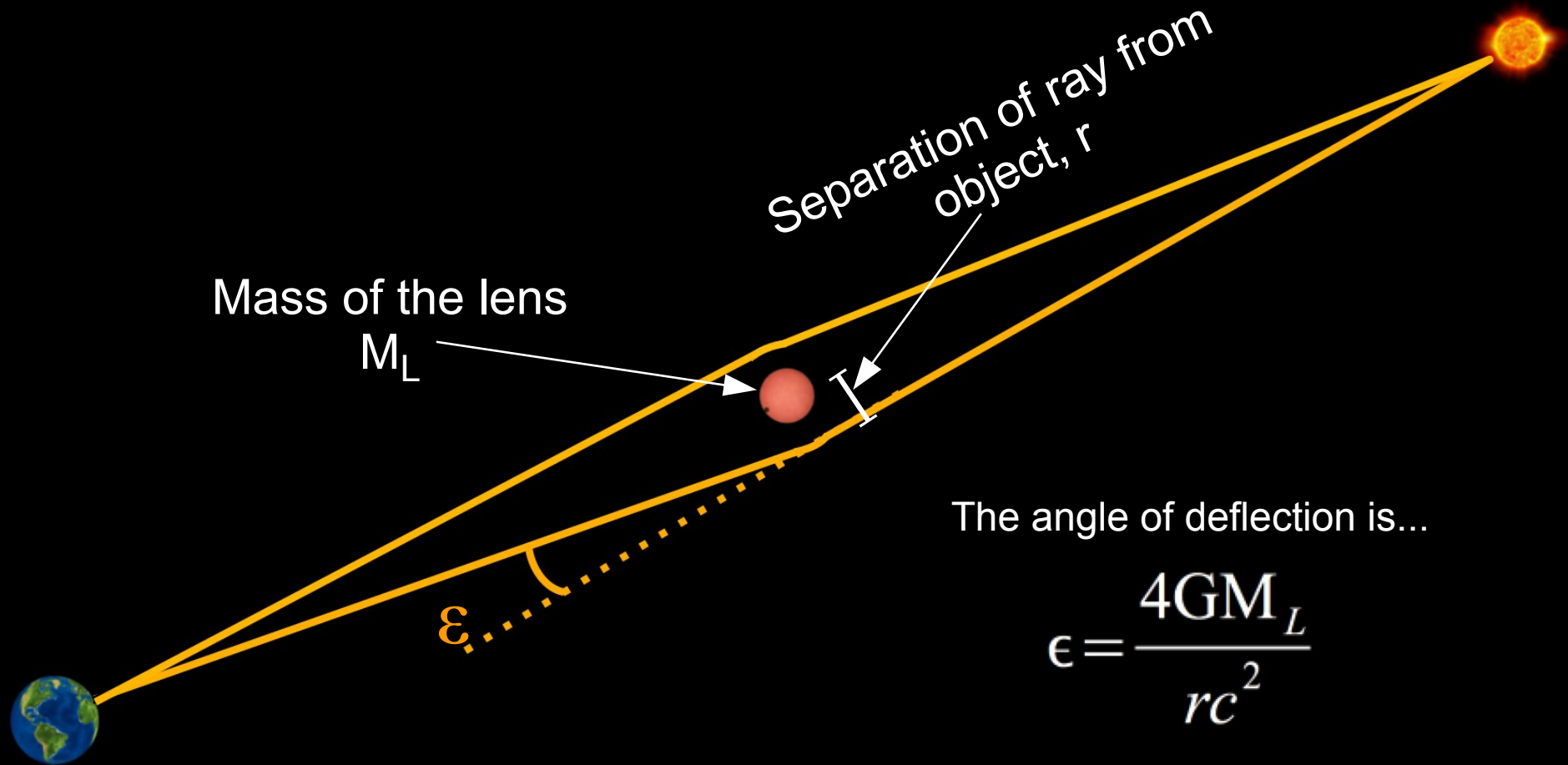
# Bending light rays



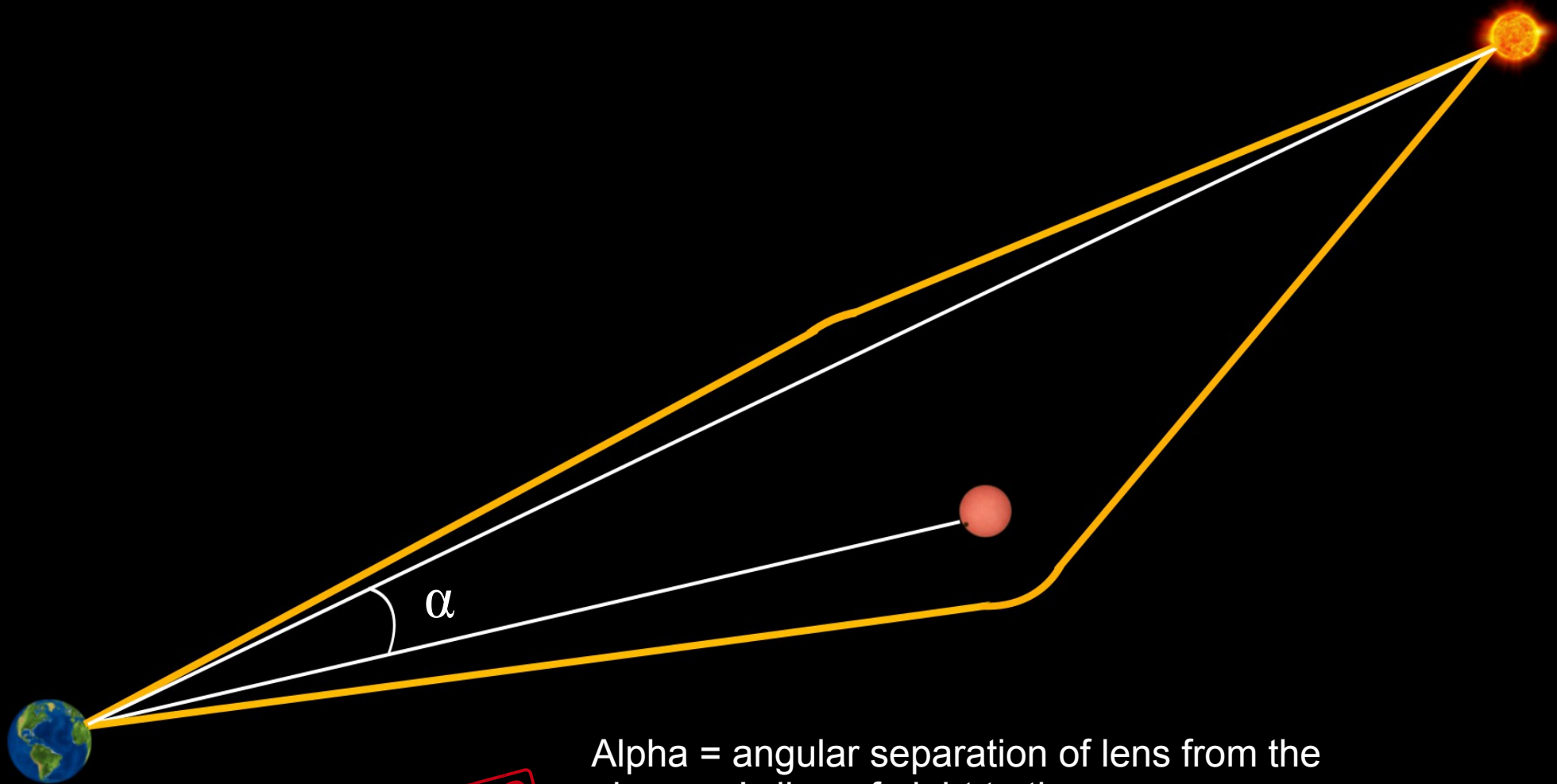
General Relativity tells us that massive objects warp spacetime

Lightrays traveling through warped spacetime are deflected as they pass stars and planets

# Deflection of light



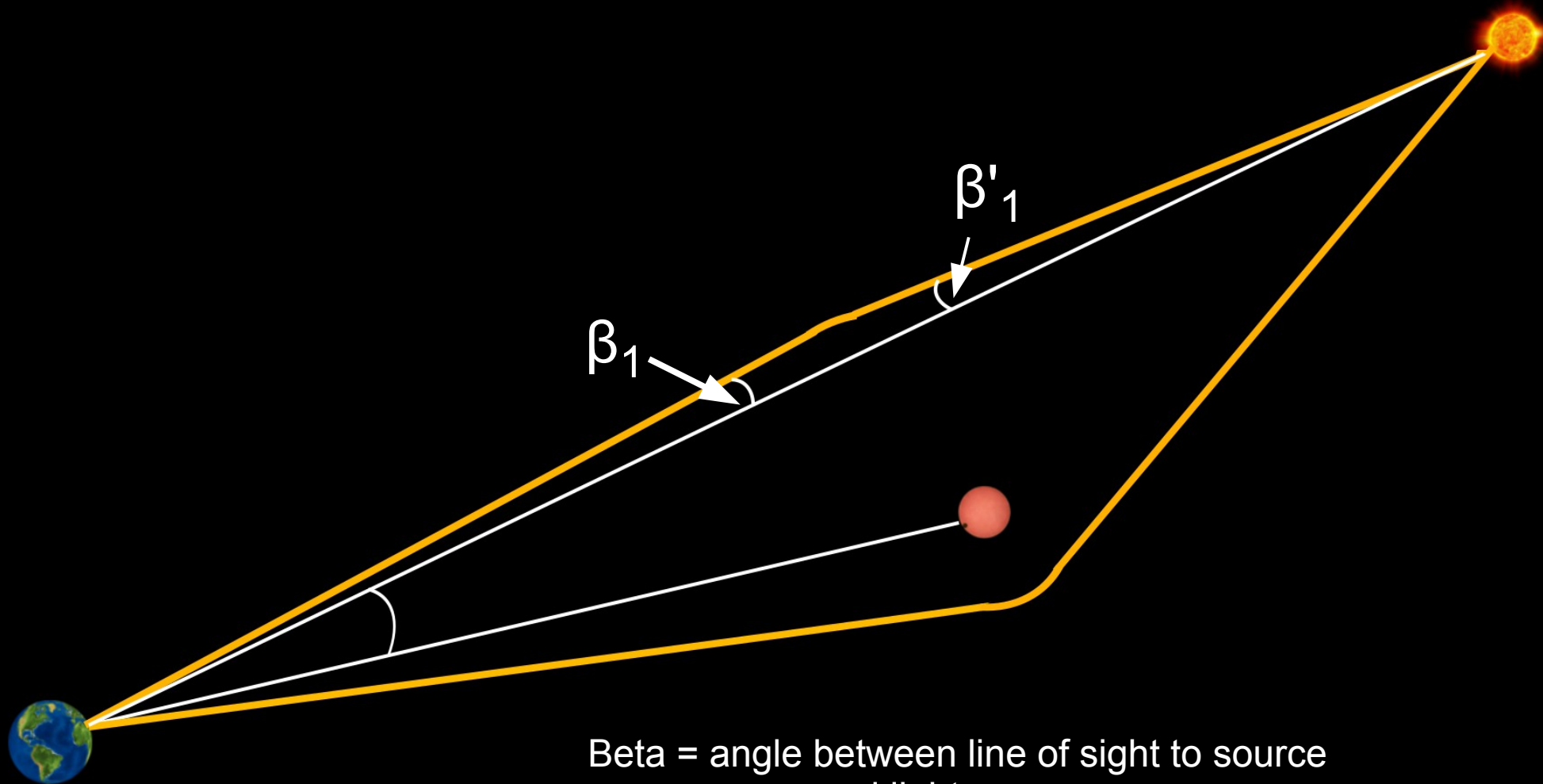
# Angles of microlensing



**WARNING**

Alpha = angular separation of lens from the observer's line-of-sight to the source (Function of time)

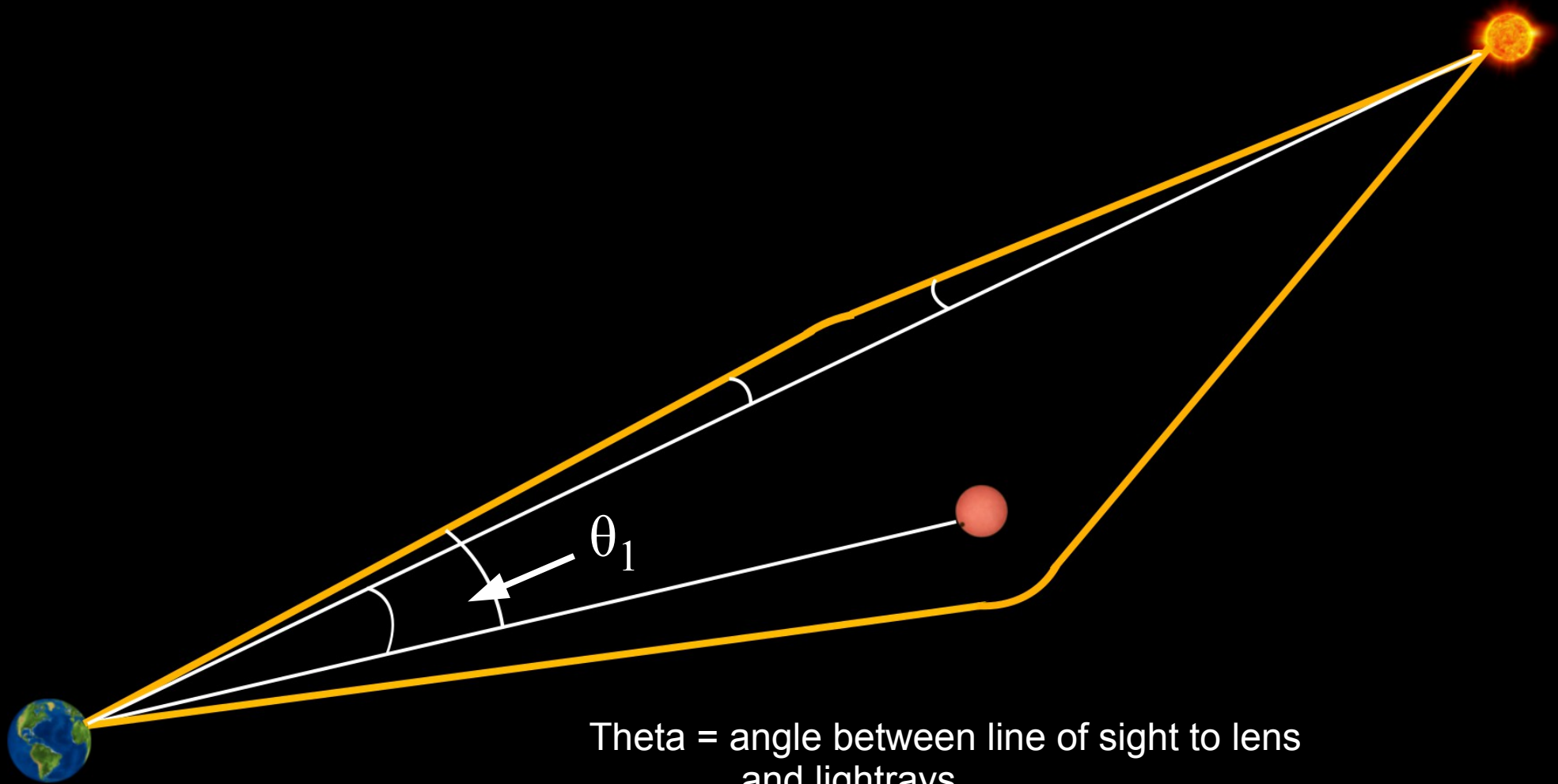
# Angles of microlensing



Beta = angle between line of sight to source and lightrays



# Angles of microlensing

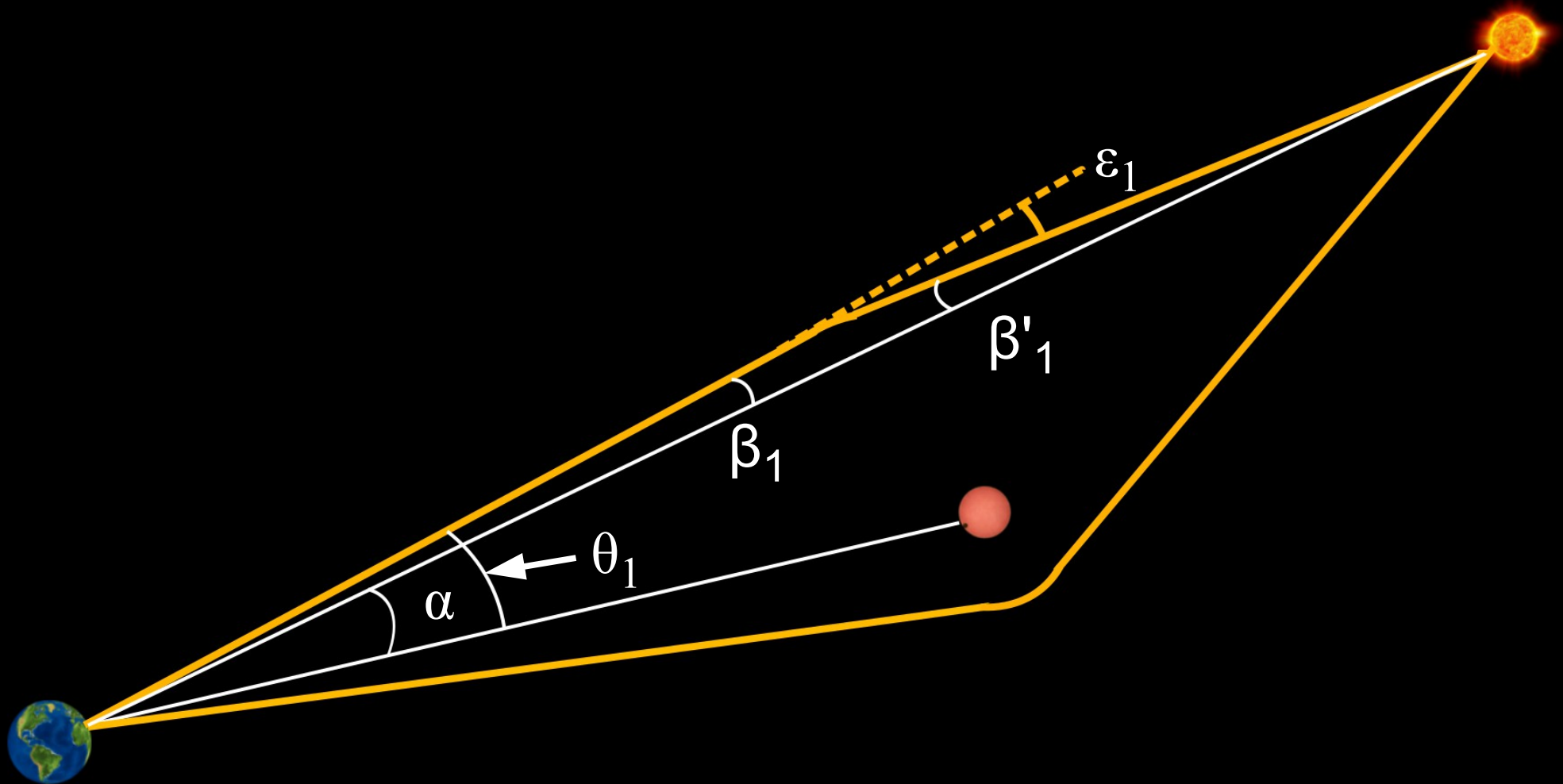


Theta = angle between line of sight to lens  
and lightrays

# Deflection of light

$$\theta_1 = \alpha + \beta_1$$

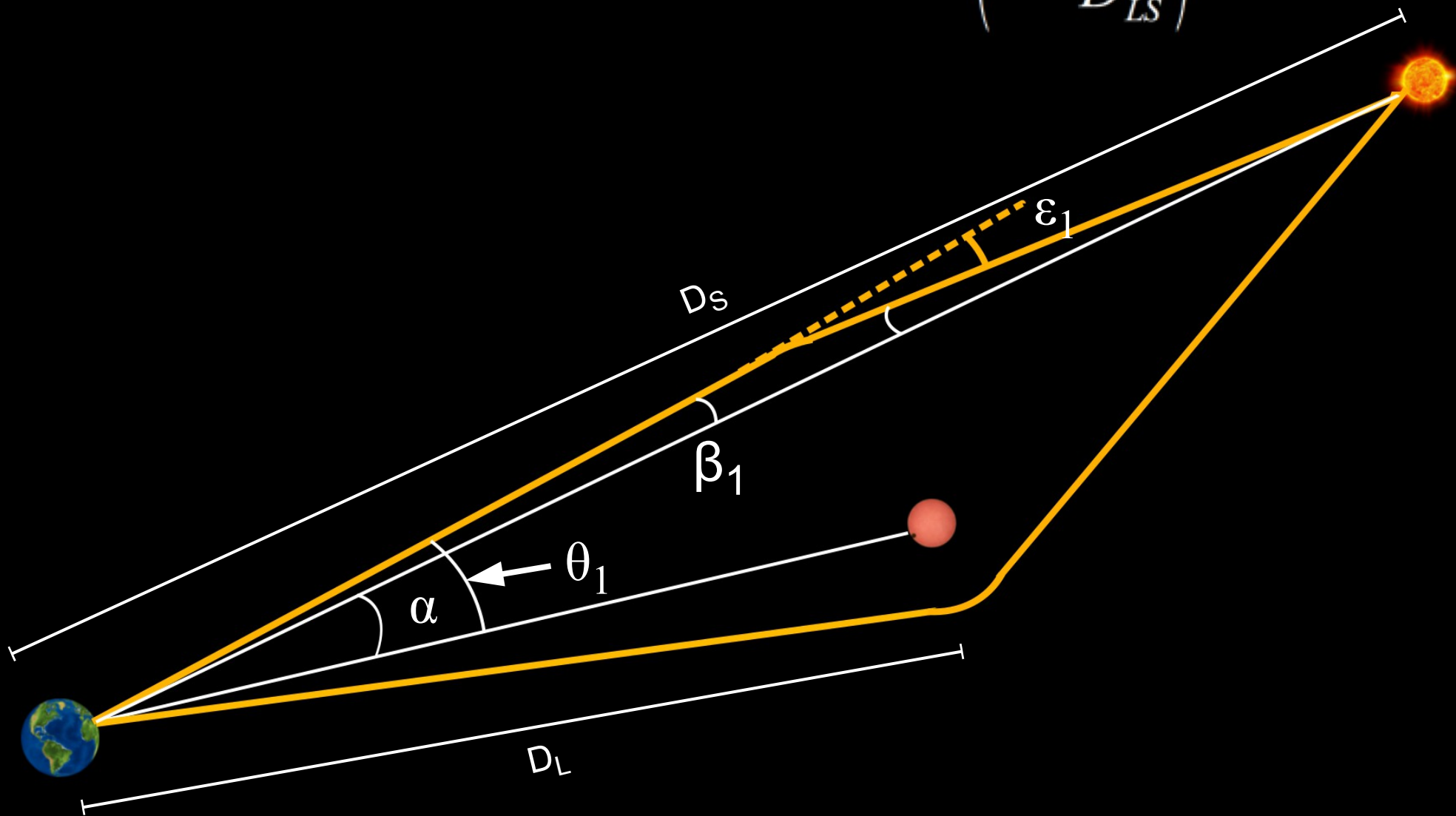
$$\epsilon_1 = \beta_1 + \beta'_1$$



# Deflection of light

$$\theta_1 = \alpha + \beta_1$$

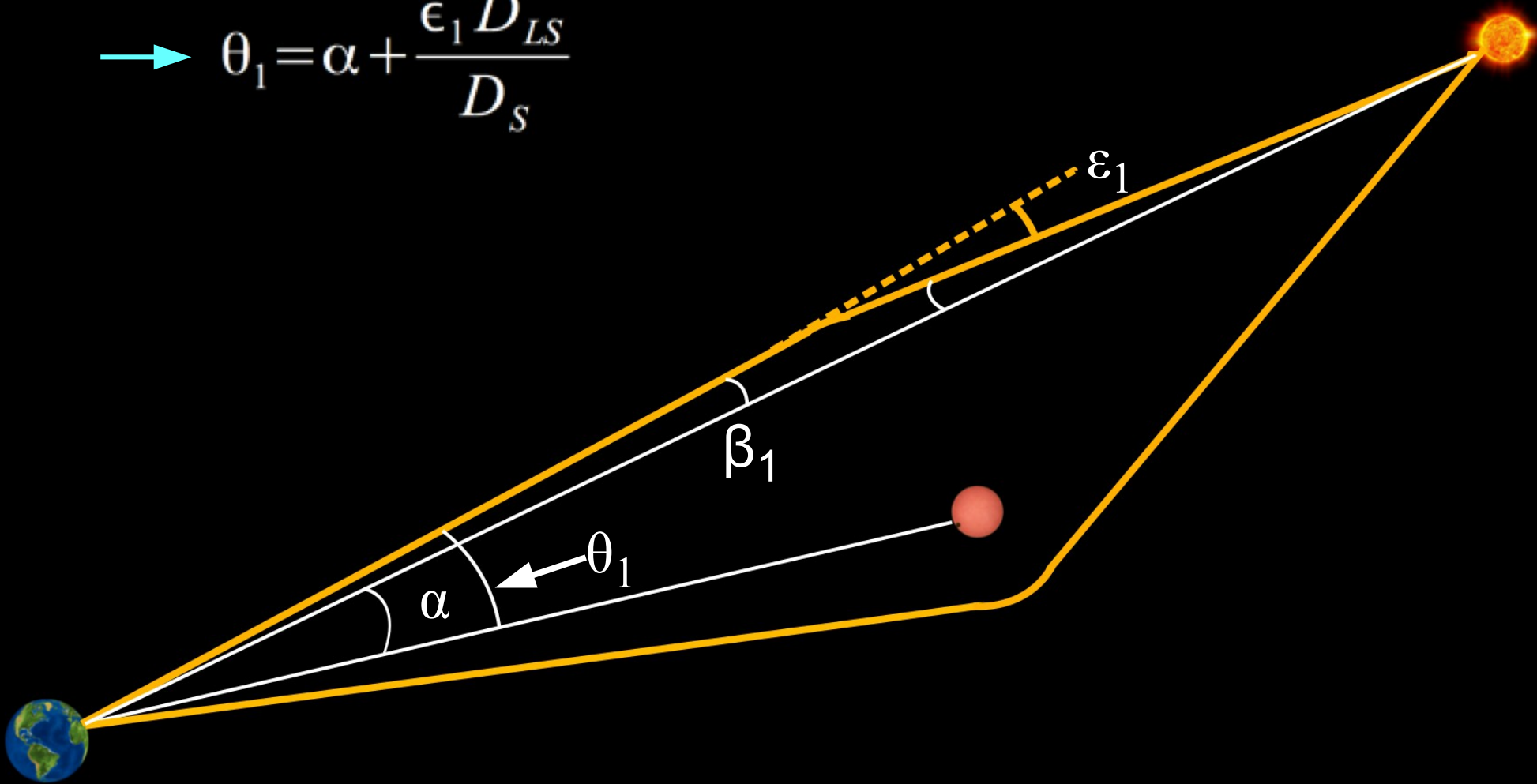
$$\epsilon_1 = \beta_1 \left( 1 + \frac{D_L}{D_{LS}} \right)$$



# Deflection of light

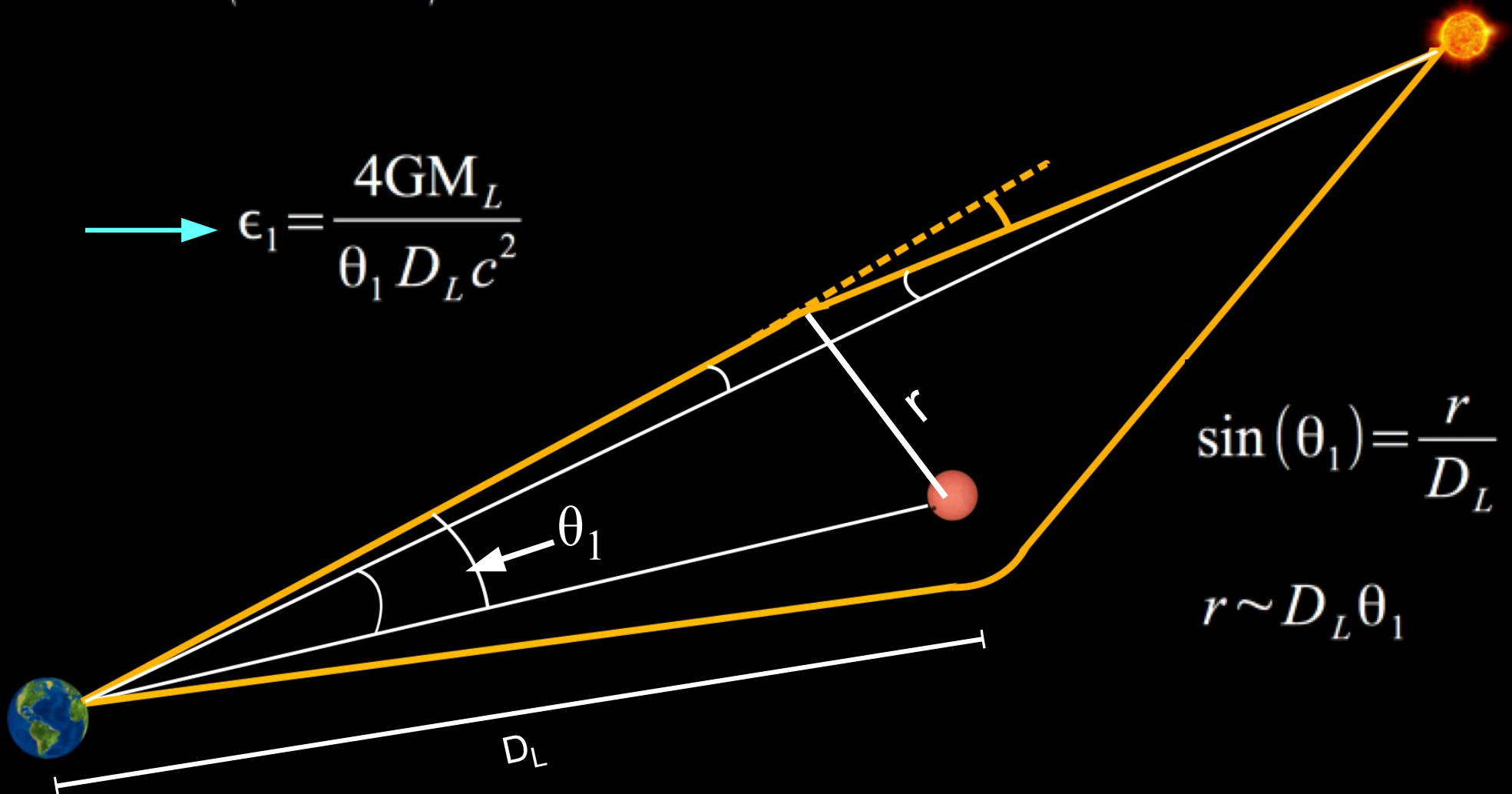
$$\theta_1 = \alpha + \beta_1 \quad \epsilon_1 = \beta_1 \left( 1 + \frac{D_L}{D_{LS}} \right)$$

$$\theta_1 = \alpha + \frac{\epsilon_1 D_{LS}}{D_S}$$



# Deflection of light

$$\epsilon_1 = \beta_1 \left( 1 + \frac{D_L}{D_{LS}} \right) = \frac{4GM_L}{rc^2}$$

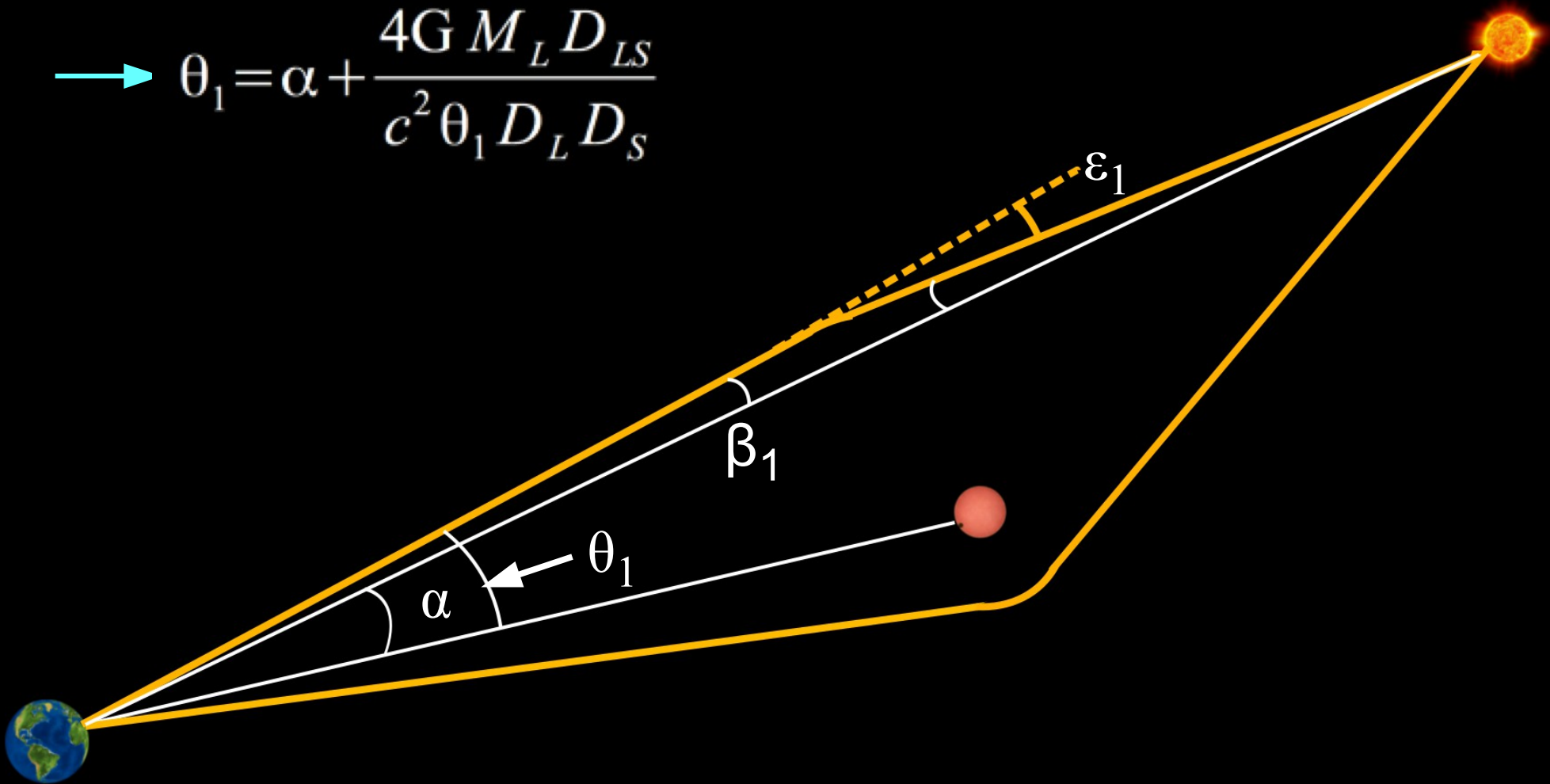




# Deflection of light

$$\theta_1 = \alpha + \frac{\epsilon_1 D_{LS}}{D_S}$$

$$\rightarrow \theta_1 = \alpha + \frac{4G M_L D_{LS}}{c^2 \theta_1 D_L D_S}$$

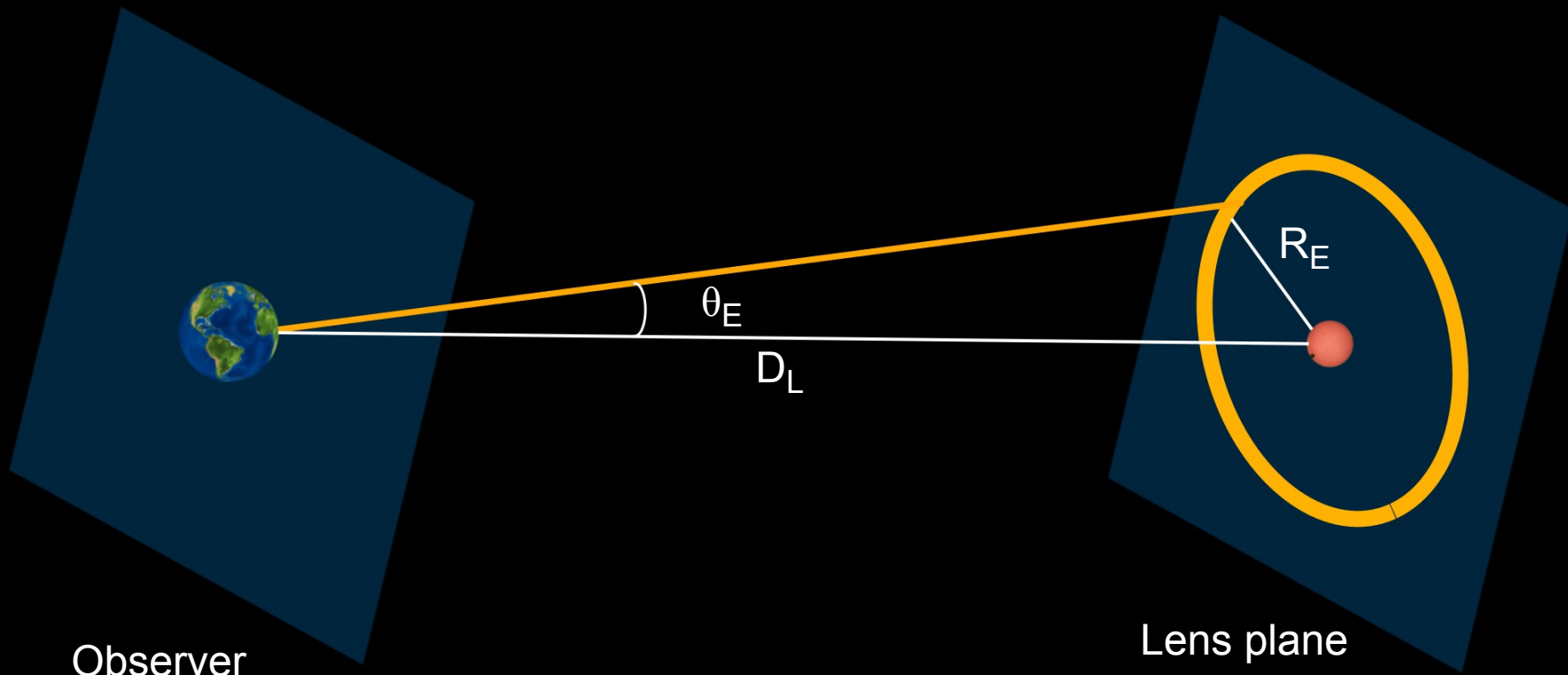


The Lens Equation...

...and the Einstein radius

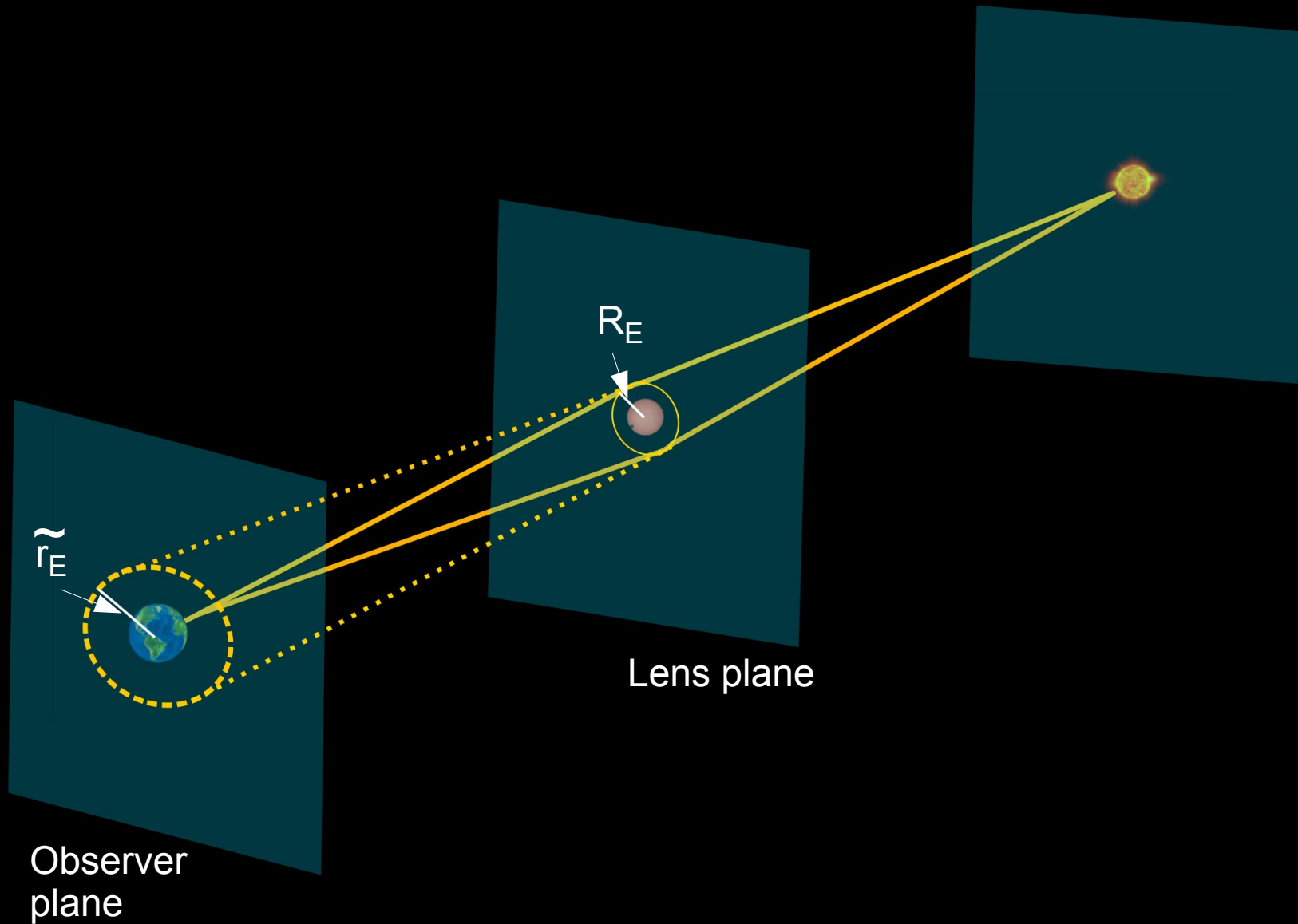
$$\theta_1^2 - \alpha \theta_1 - \frac{4G M_L D_{LS}}{c^2 D_L D_S} = 0$$

$$\theta_E = \sqrt{\frac{4G M_L D_{LS}}{c^2 D_L D_S}} \quad (\text{Sometimes written } \theta_0)$$



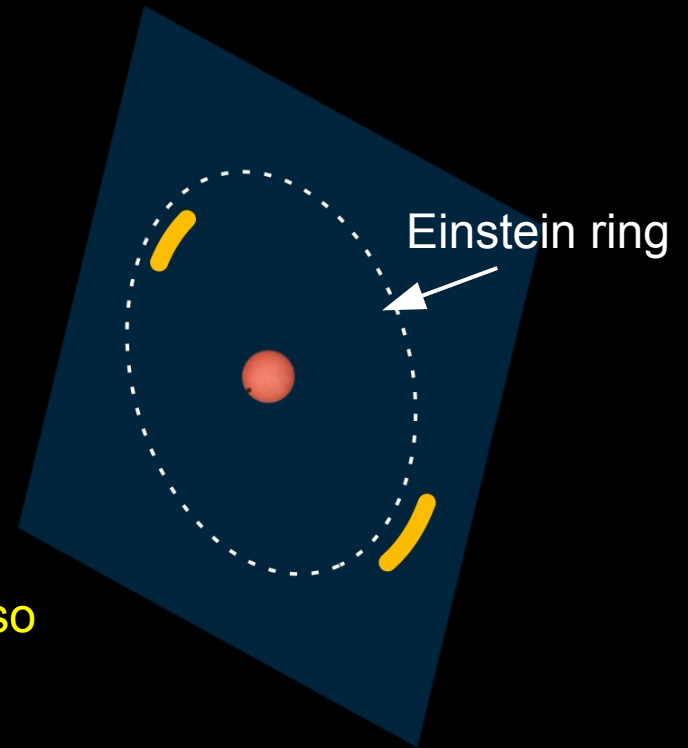
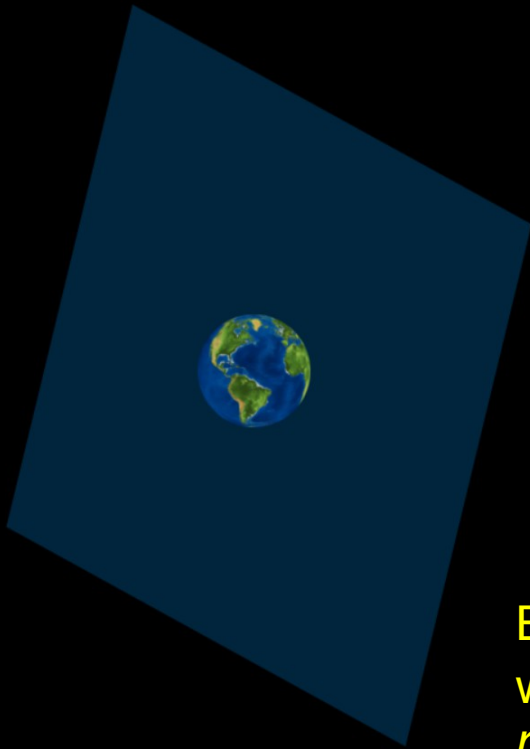
# Projected Einstein Radius

The radius of the Einstein ring projected back to the observer's plane



Two solutions  $\rightarrow$  Two images (for single lenses)

$$\theta_{1,2} = \frac{\pm \alpha + \sqrt{\left(\frac{1}{2} \alpha\right)^2 + \theta_E^2}}{2}$$

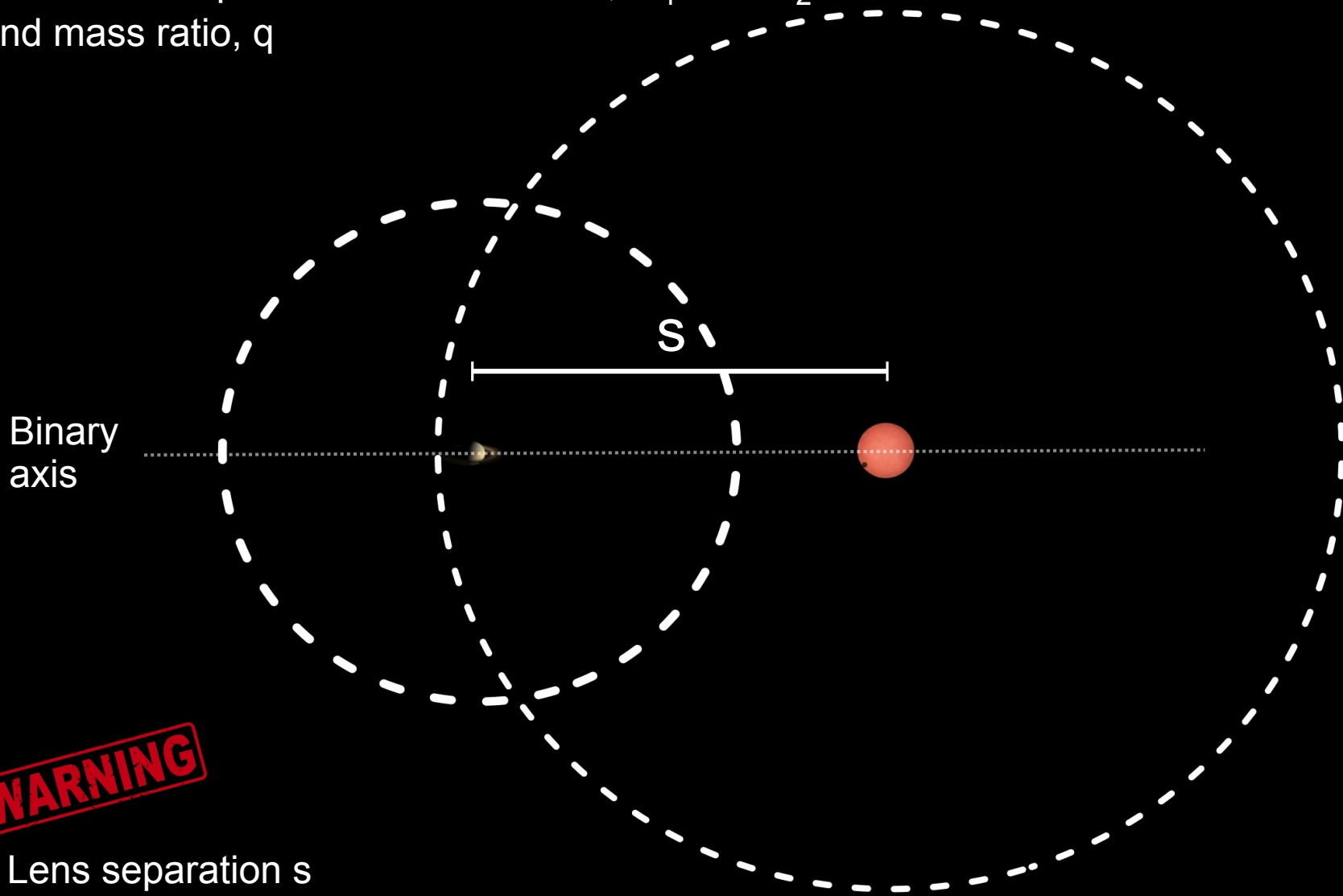


But  $\theta_{1,2}$  are too small to resolve, so we actually observe just the *magnification* of the source

# Two-body microlensing

Lens is a composition of two masses,  $M_1$  and  $M_2$   
and mass ratio,  $q$

Lens plane

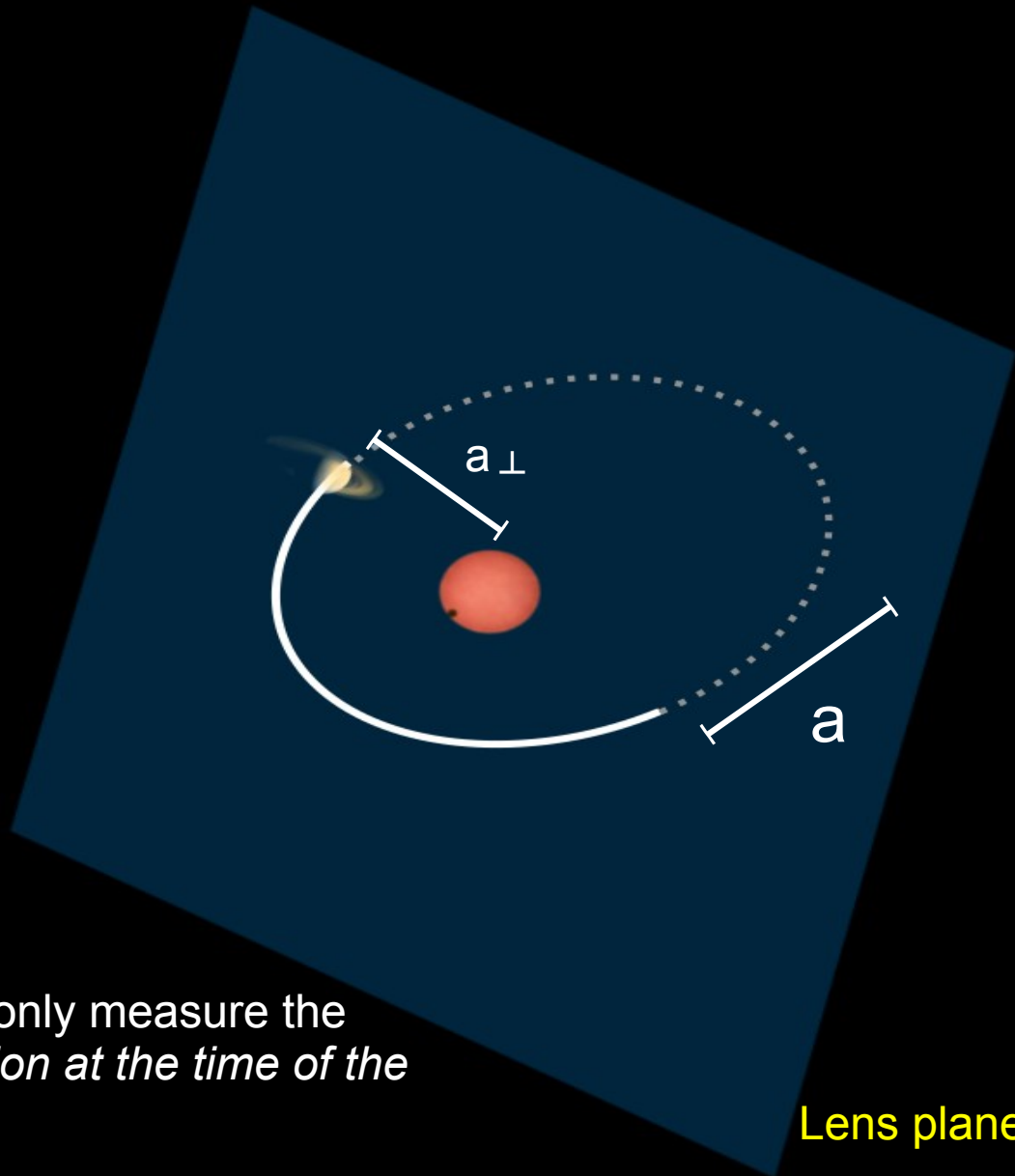


**WARNING**

Lens separation  $s$   
is sometimes also called  $s_0$ ,  $d$ , or  $b$



# Two-body microlensing

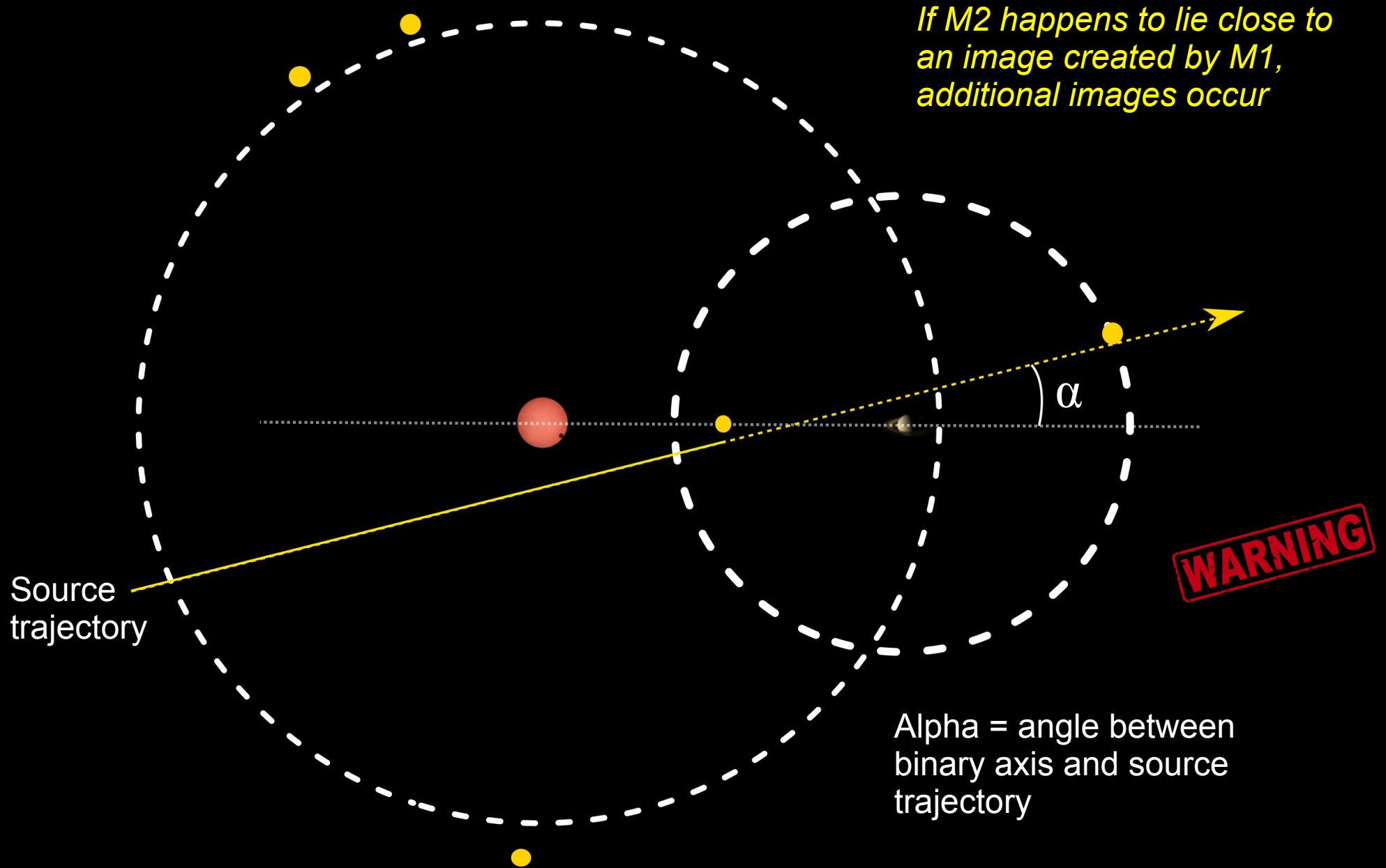


**WARNING**

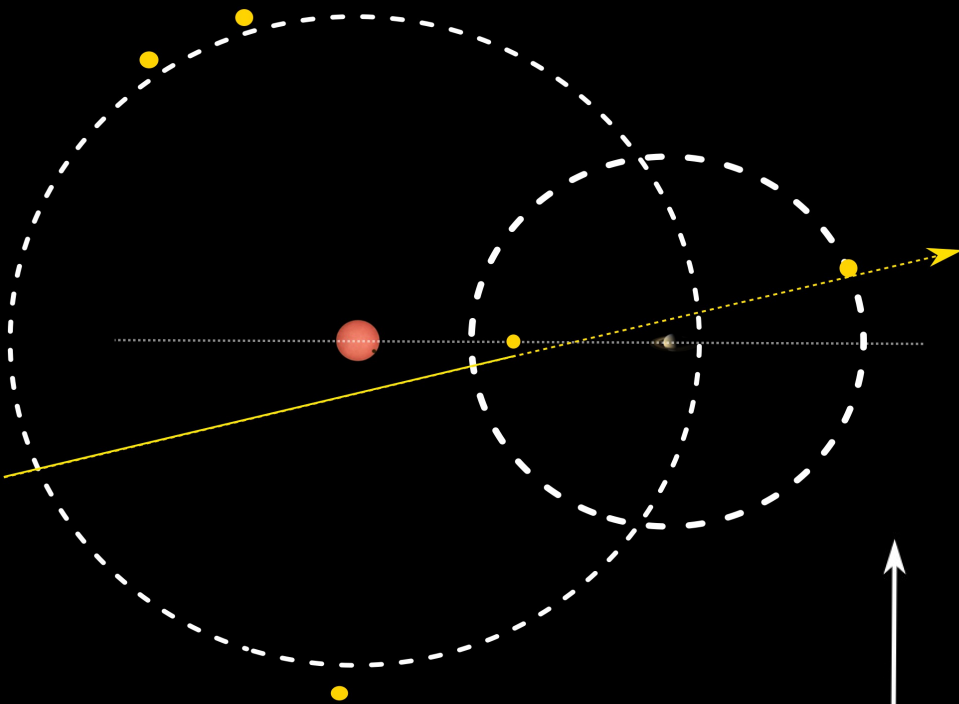
Microlensing can only measure the *projected separation at the time of the event*

Lens plane

# Binary lenses may create more images

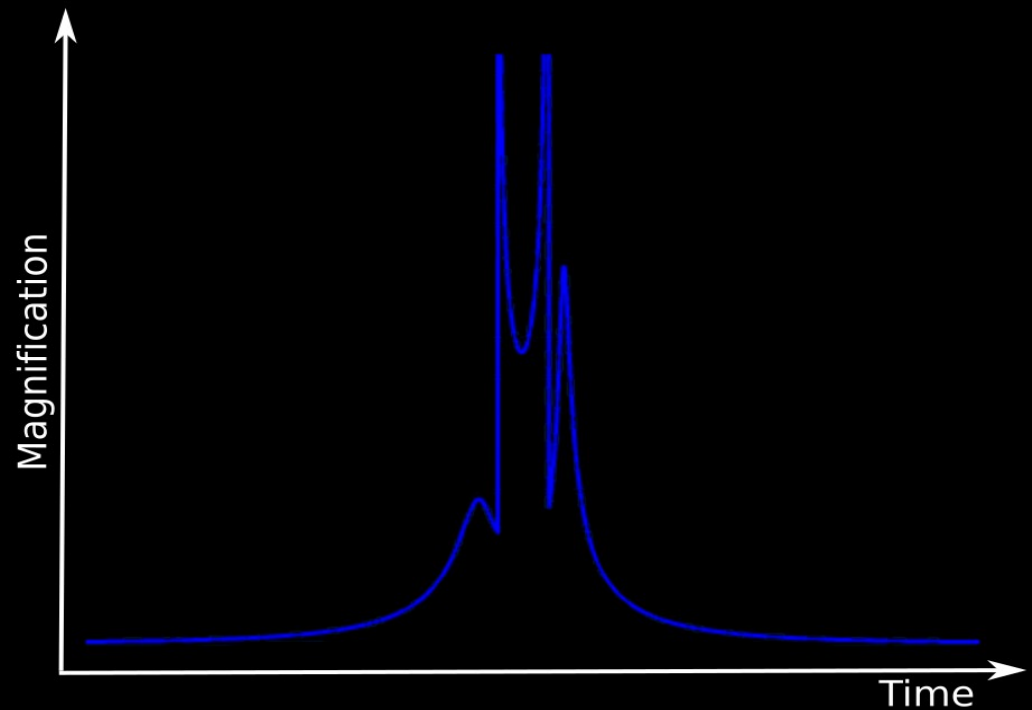


# Binary lenses create more images



Can have 3 or 5, depending on event parameters

This results in an amazing variety of lightcurves



# Microlensing Theory 101

Single lenses produce two images of the source.  
Binary lenses produce 3 or 5

If a planet orbiting the lens happens to approach one of the images during the event, the image is perturbed and additional light is received from the source

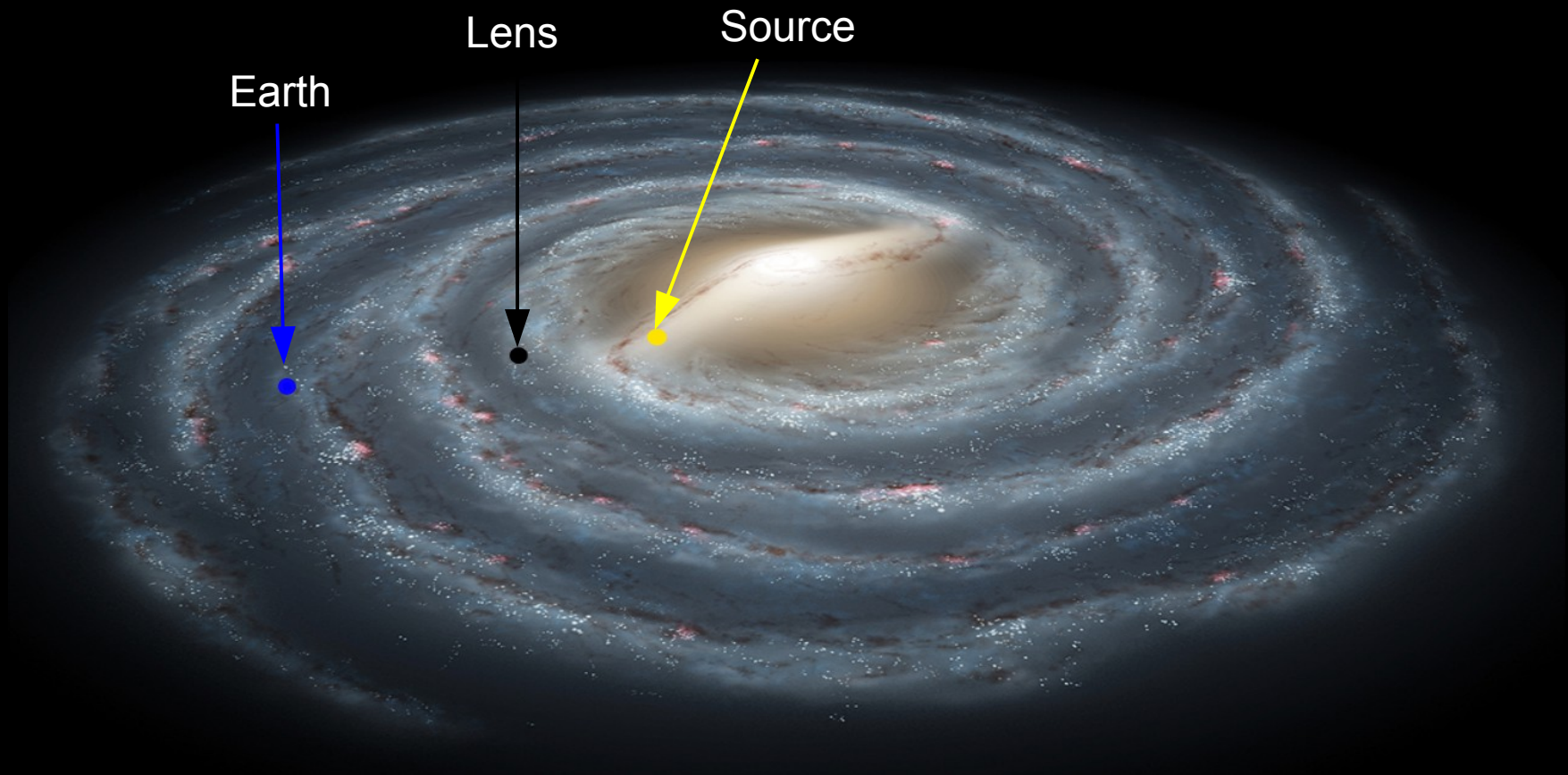
The resulting anomaly is visible in the lightcurve of the event.

For more information, see  
<http://microlensing-source.org/tutorial/pspl/>

# Example Microlensing Event

M dwarfs are the most common type of star:  
Source star typically in the Galactic Bulge:  
Lens distance:

$M_L = 0.5 M_{\text{Sun}}$   
 $D_S = 7.5 \text{ Kpc from Earth}$   
 $D_L = 6 \text{ Kpc from Earth}$





# Example Microlensing Event

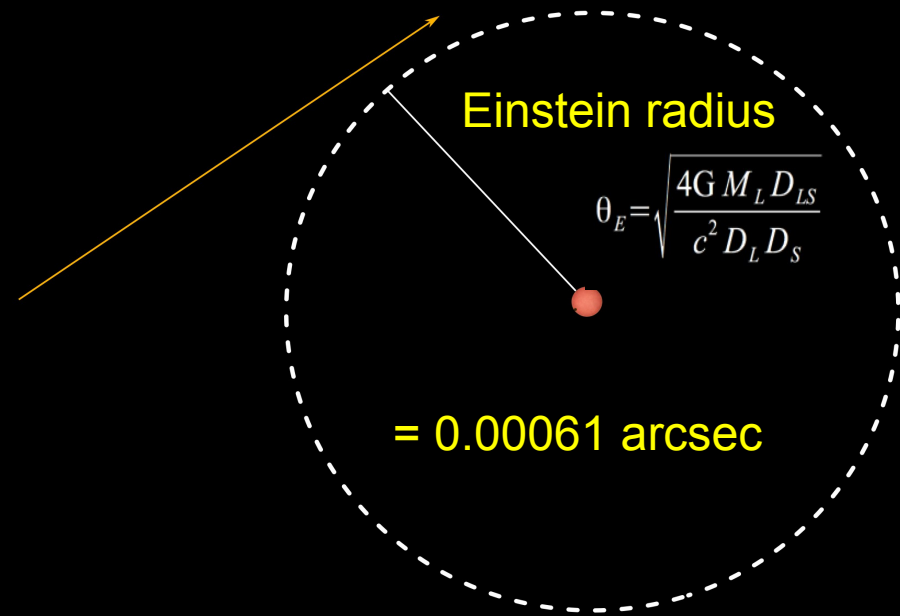
M dwarfs are the most common type of star:  
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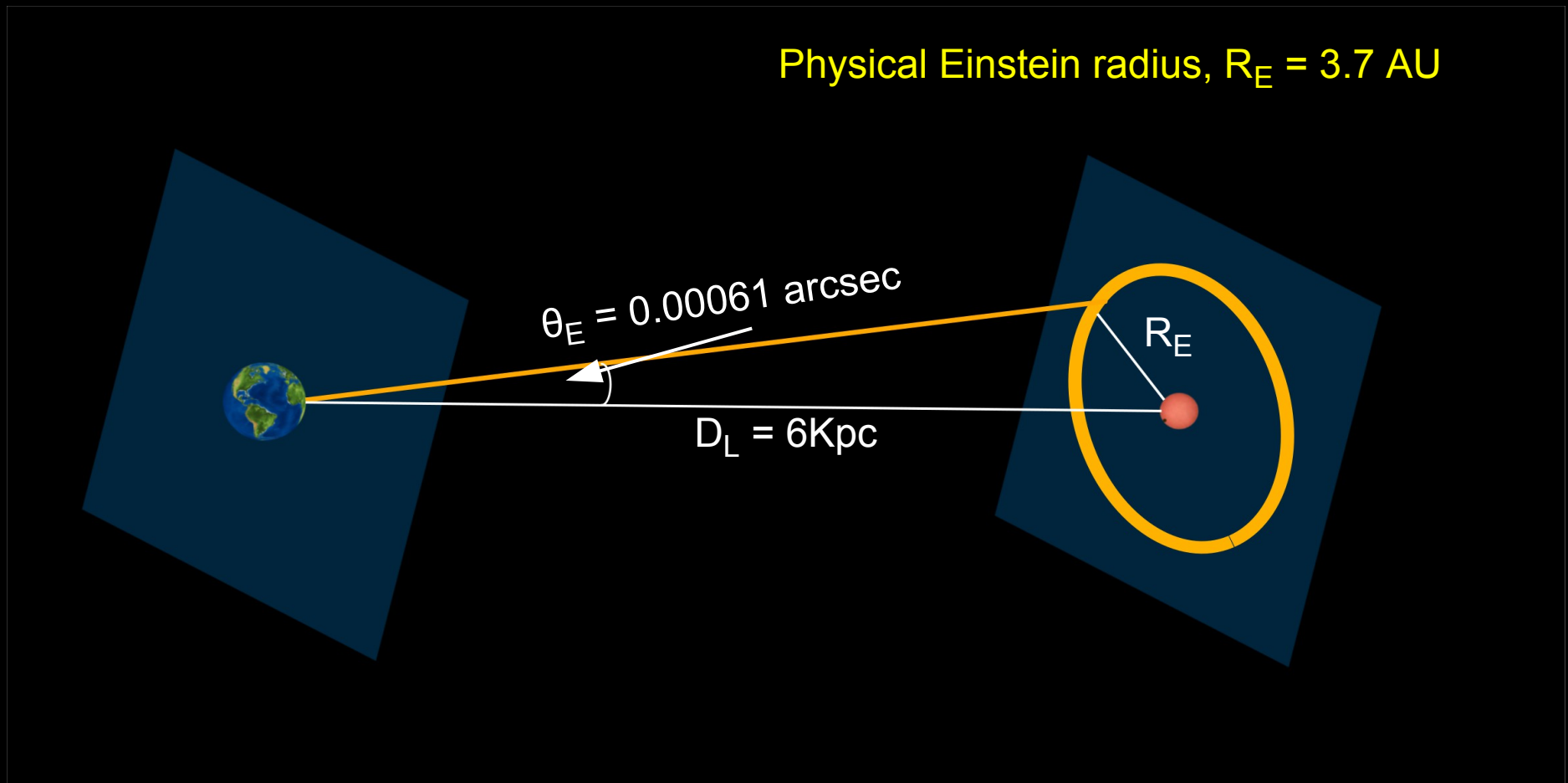
Separation of lensed images too small to resolve

Very small cross-section of interaction!

- Intrinsically rare
- Need to look towards dense starfields for potential sources



# Example Microlensing Event



This is why microlensing is a great way to look for exoplanets at 1-10 AU -  
They're most easily detectable when they're located close to images forming around  $R_E$

# Example Microlensing Event

Einstein crossing timescale,  $t_E$ , is the time taken for the source to pass behind the Einstein ring of the lens

$$t_E = \frac{\theta_E}{\mu_{rel}}$$

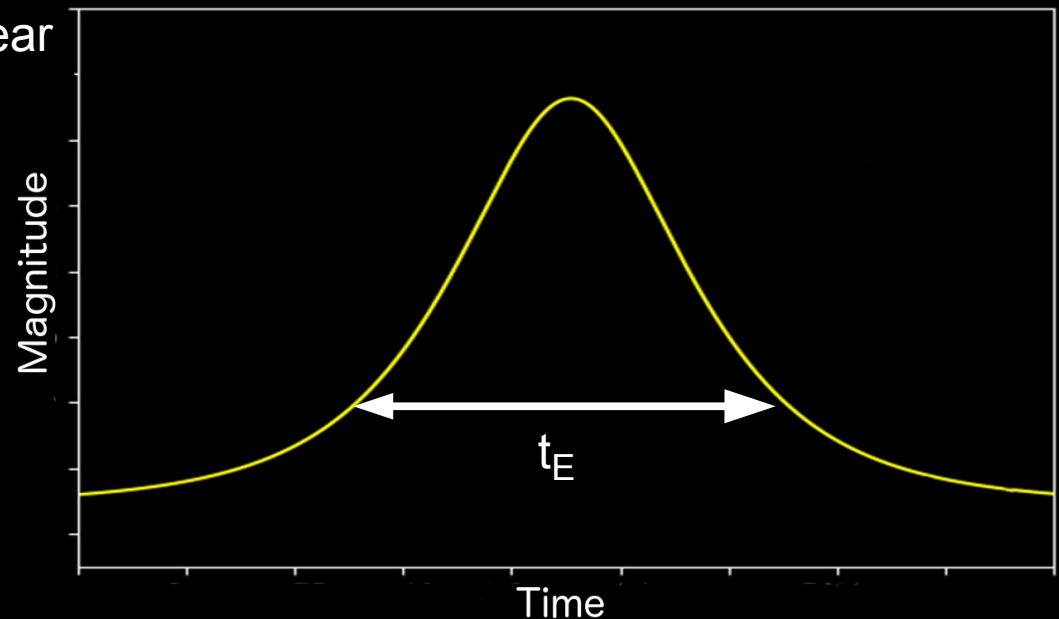
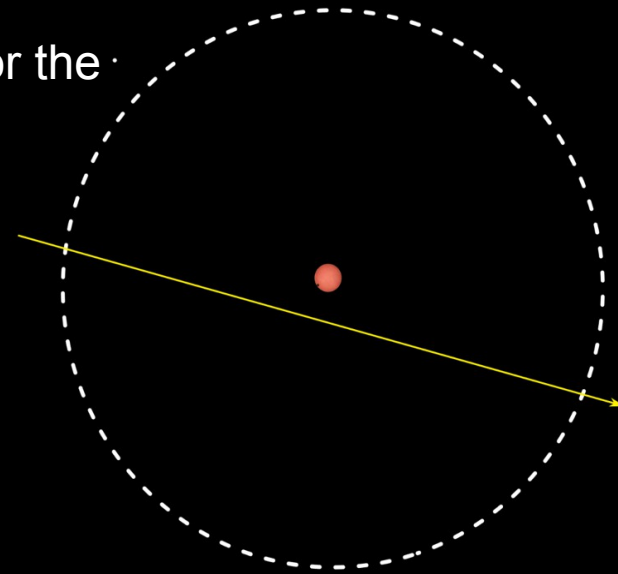
$\mu_{rel}$  is lens-source relative proper motion

Typical proper motion  $\sim 0.1$  arcsec/year

Relative proper motion  $\sim 0.005$  arcsec/year

$\rightarrow t_E \sim 45$  days

$\rightarrow$  To detect microlensing events we need to observe  $\sim$ once / day



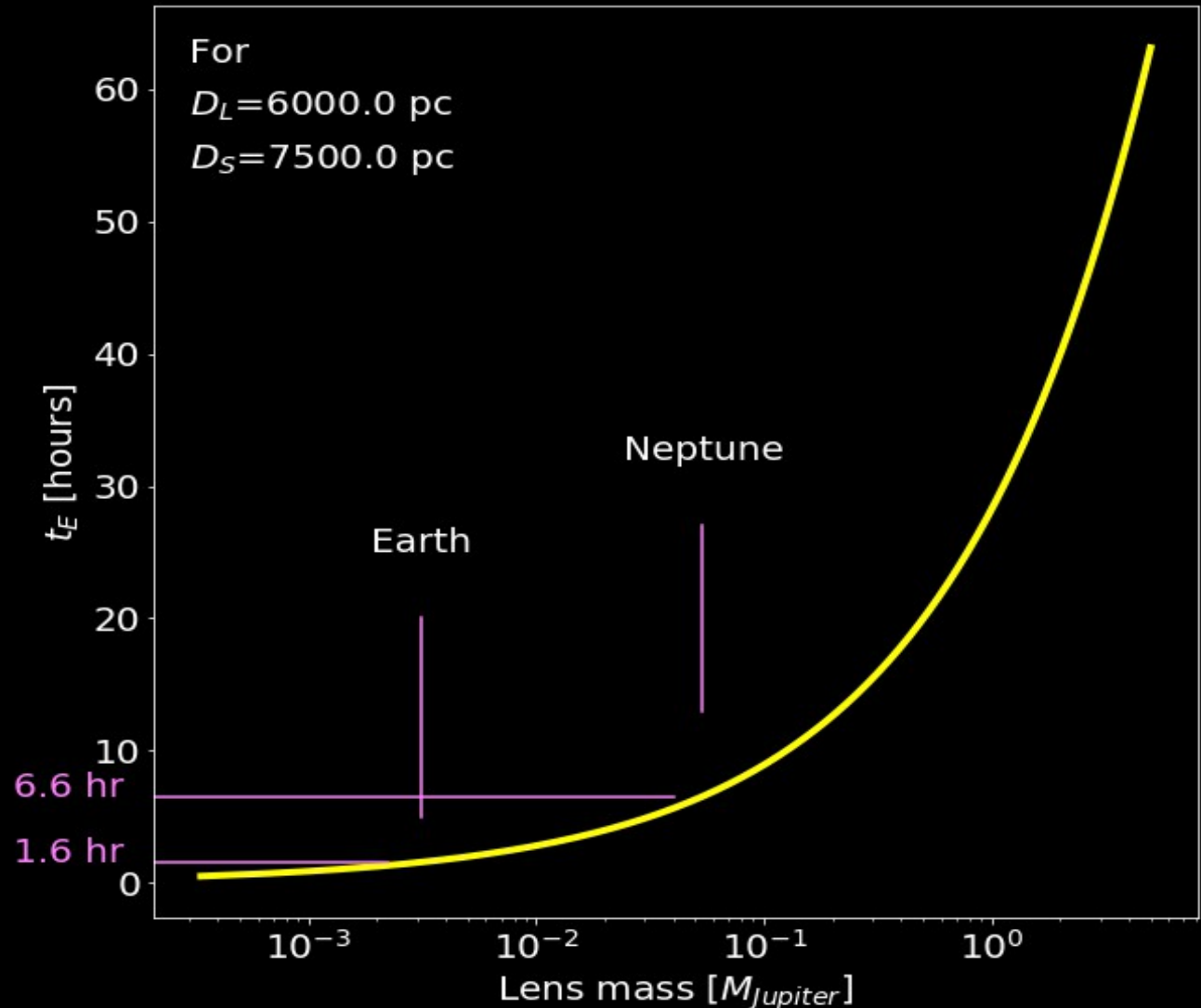
# Example Microlensing Event

Einstein crossing timescale,  $t_E$ , for a typical stellar event is ~months

But for planet-mass lenses  $t_E$  is <1 day

$$t_E = \frac{\theta_E}{\mu_{rel}}$$

→ To detect planetary anomalies, we need to observe ~every 15min



# References and Resources

Liebes, S. (1964), *Physical Review*, 133, B835

Paczynski, B. (1986), *ApJ*, 301, 503

Wambsganss, J. (1998), *Living Reviews in Relativity*, 1, 12

Gould, A. (2000), *ApJ*, 542, 785

See also [microlensing-source.org](http://microlensing-source.org)

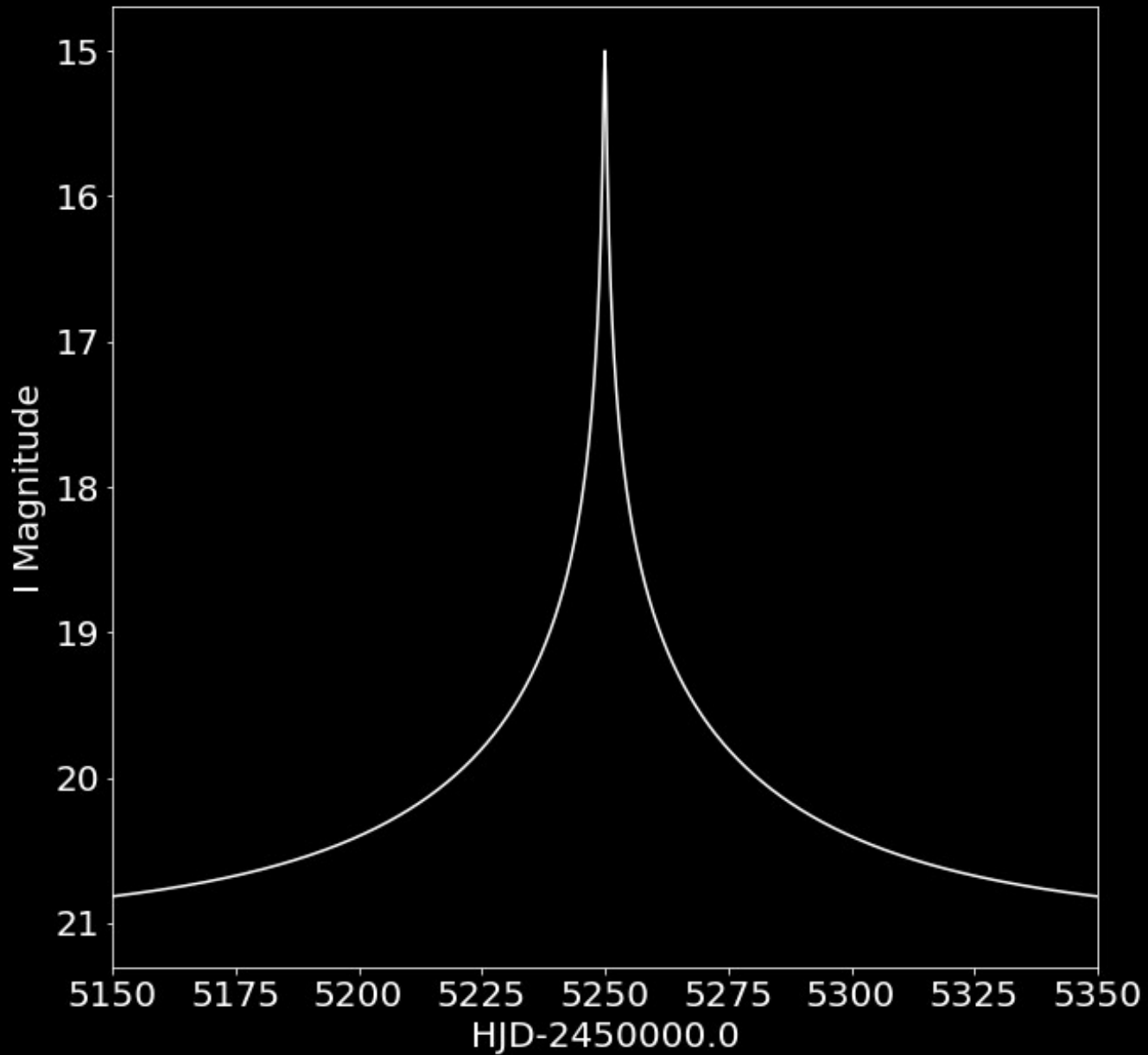
# Planet-Hunting Lightcurve Challenge

Goal:

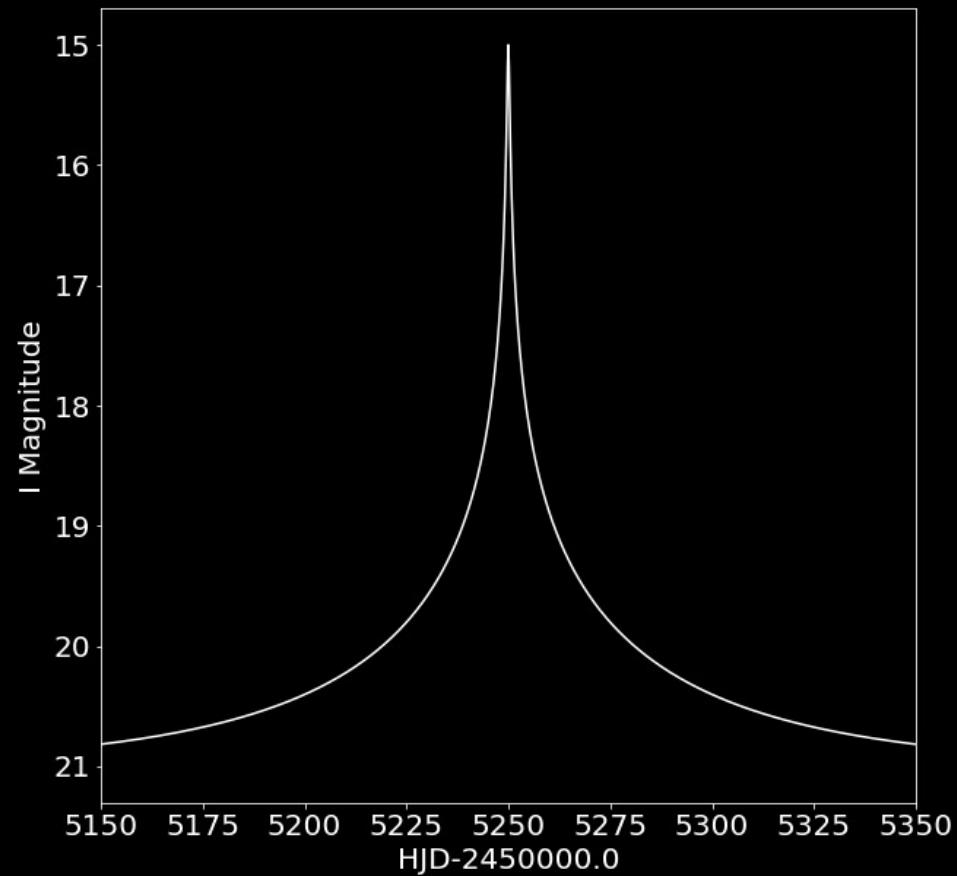
*Develop experience in identifying planetary microlensing signatures*



# Lightcurve Challenge



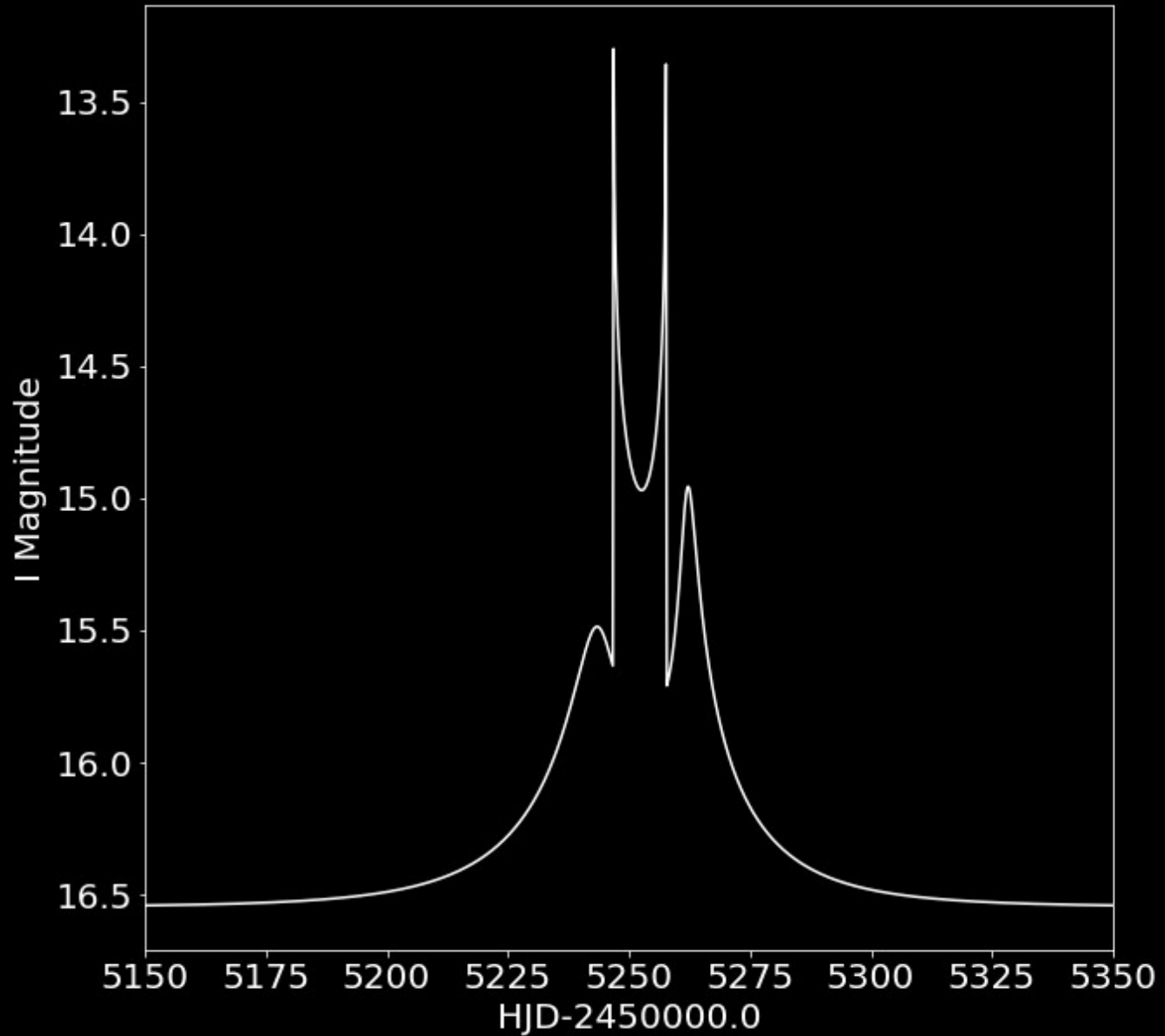
# Lightcurve Challenge



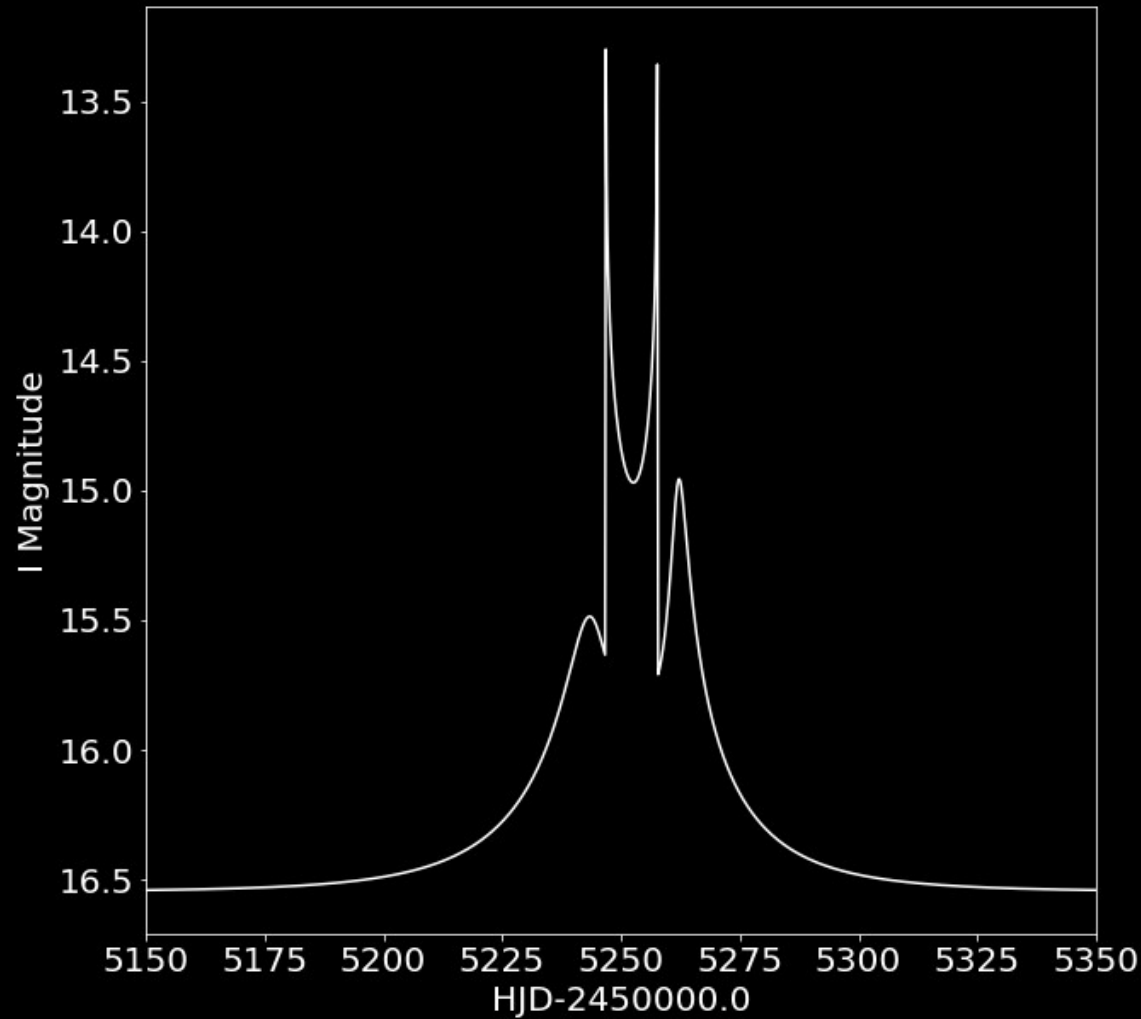
Classification:  
*Single star event*

Reason:  
 $t_E \sim 90\text{days}$   
*Symmetrical, no anomalies*

# Lightcurve Challenge



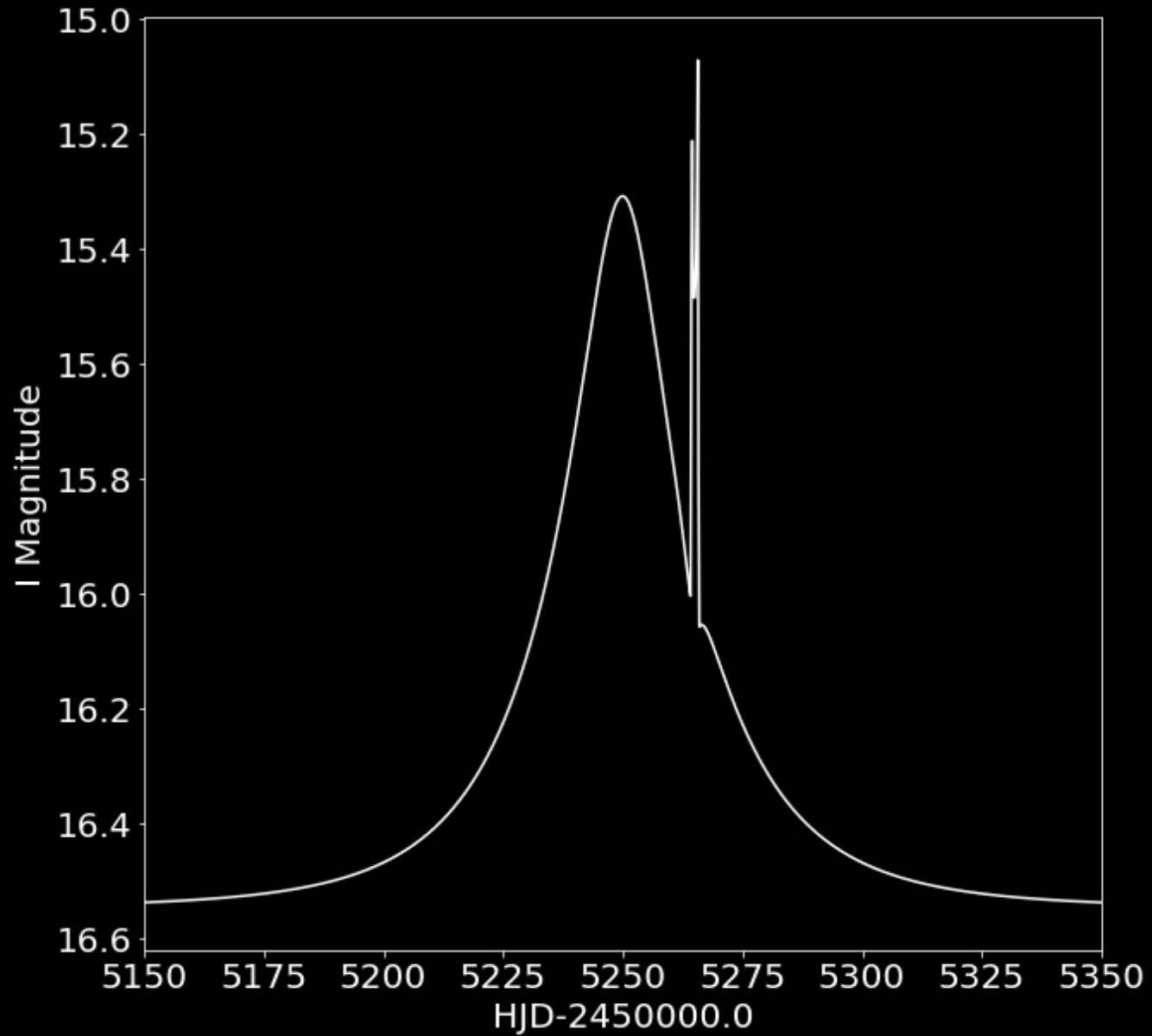
# Lightcurve Challenge



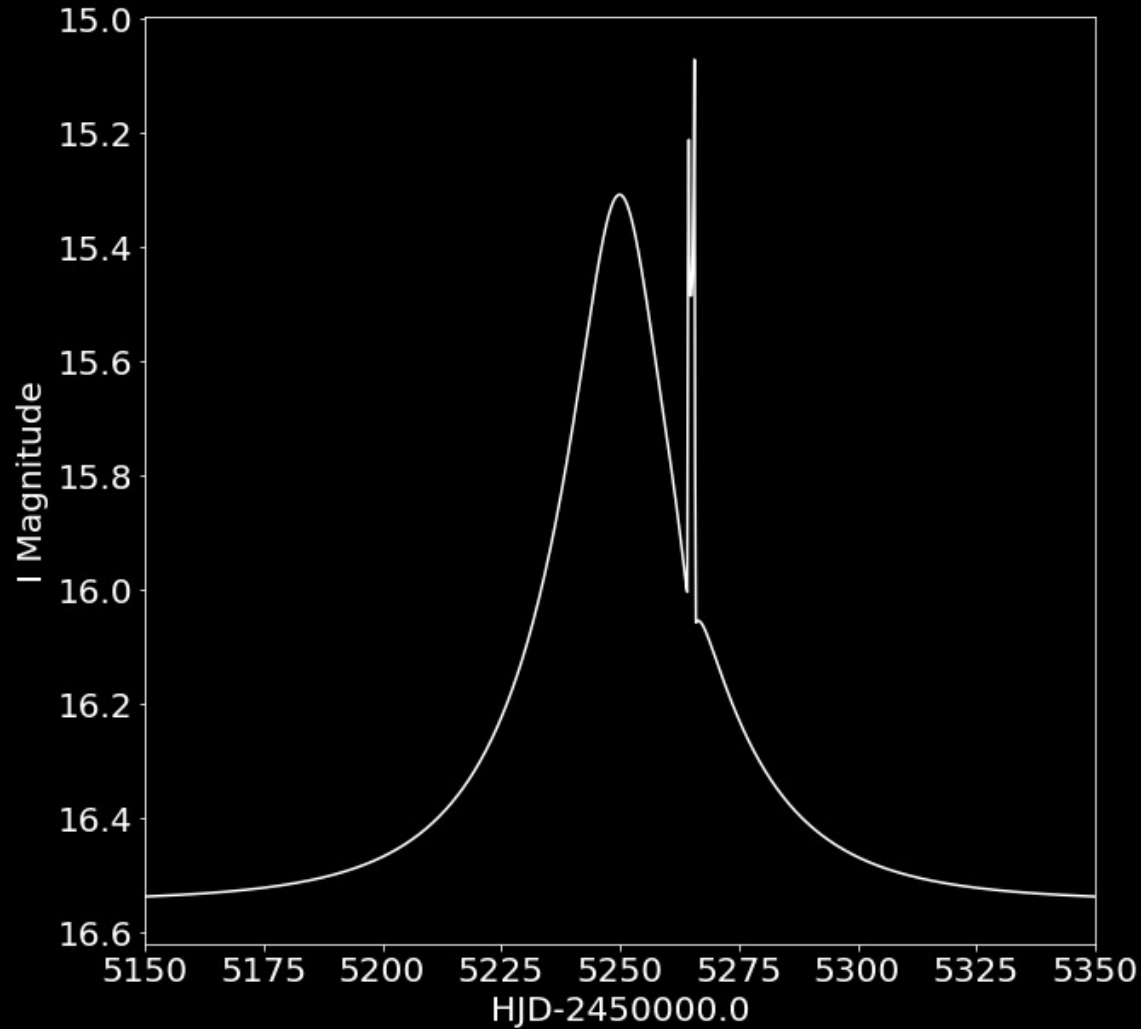
Classification:  
*Binary star event*

Reason:  
Clear anomaly  
 $t_{anomaly} \sim 20days$

# Lightcurve Challenge



# Lightcurve Challenge



Classification:

*Star + planet candidate*

Reason:

Mostly symmetrical

$t_{anomaly} \sim 1 \text{ day}$