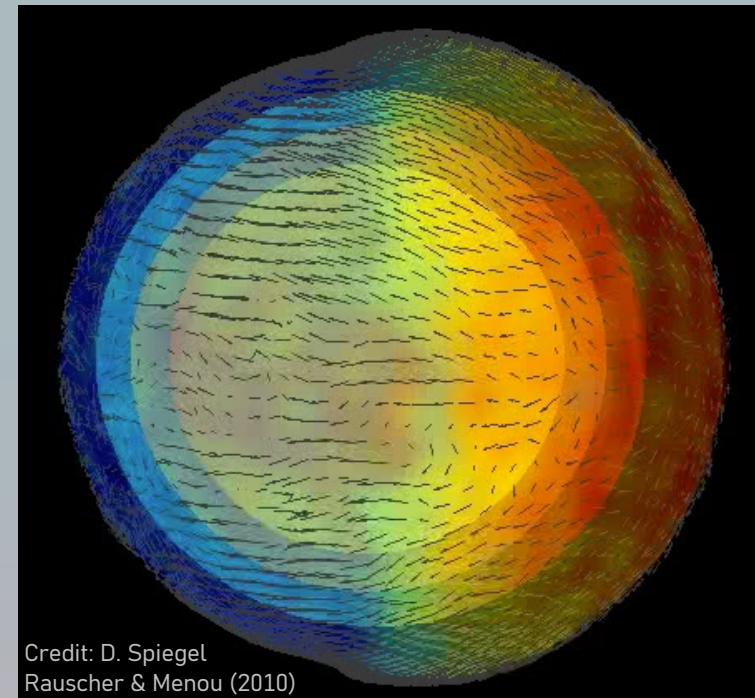


Mapping the 3D Structure of Exoplanet Atmospheres using Transit Spectroscopy

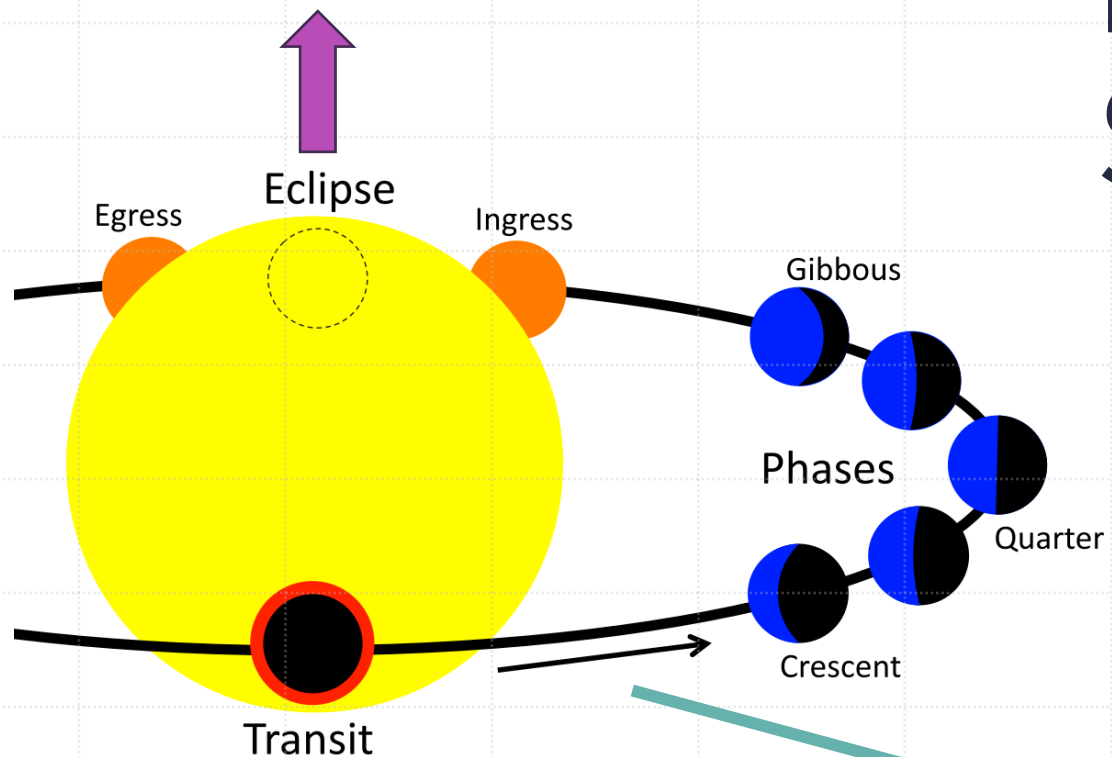


Credit: D. Spiegel
Rauscher & Menou (2010)

Emily Rauscher (she/her)
University of Michigan

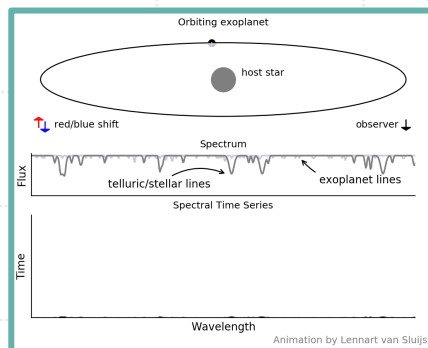
Methods of Transit Spectroscopy

Eclipse mapping
3D structure of dayside



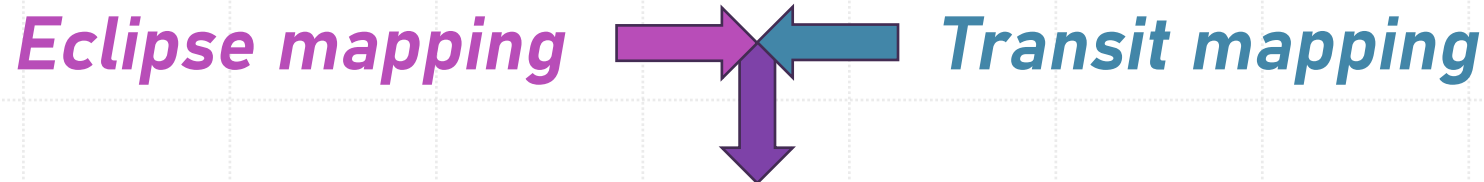
Orbital (rotational) phase curves
2D structure in longitude and pressure

Phase-dependent high-resolution spectroscopy
2D structure in longitude and pressure



Transit mapping
3D structure of terminator

The geometries are different, but both techniques share the same basics

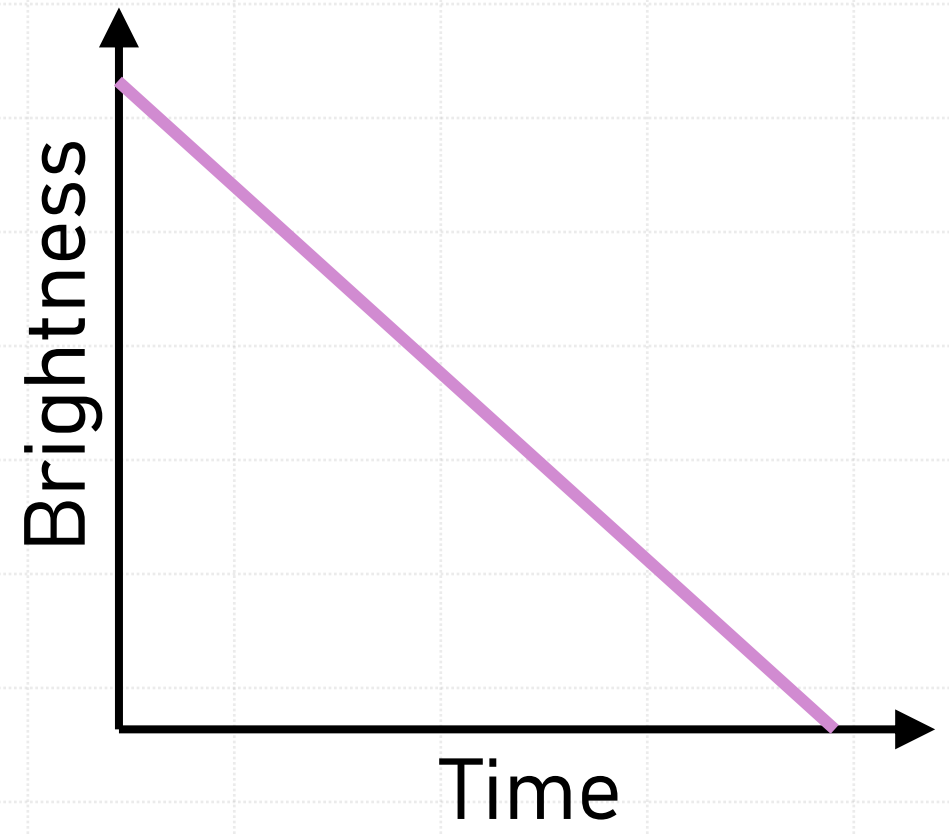
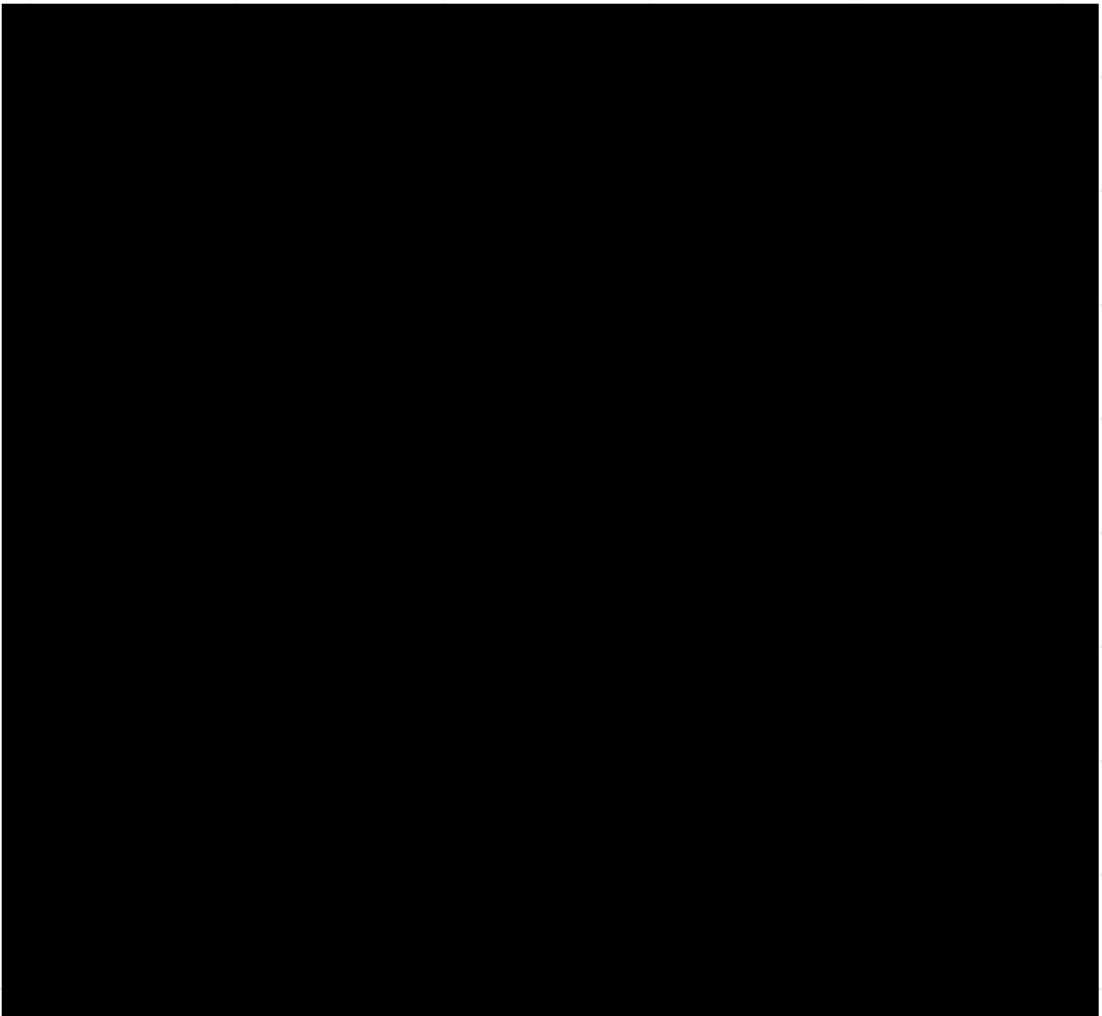


- How to access 3D info:
 - Latitude and longitude come from the shape of the light curve
 - Depth into the atmosphere comes from spectral differences
- Methods to extract 3D info:
 - Model-independent
 - Model-informed

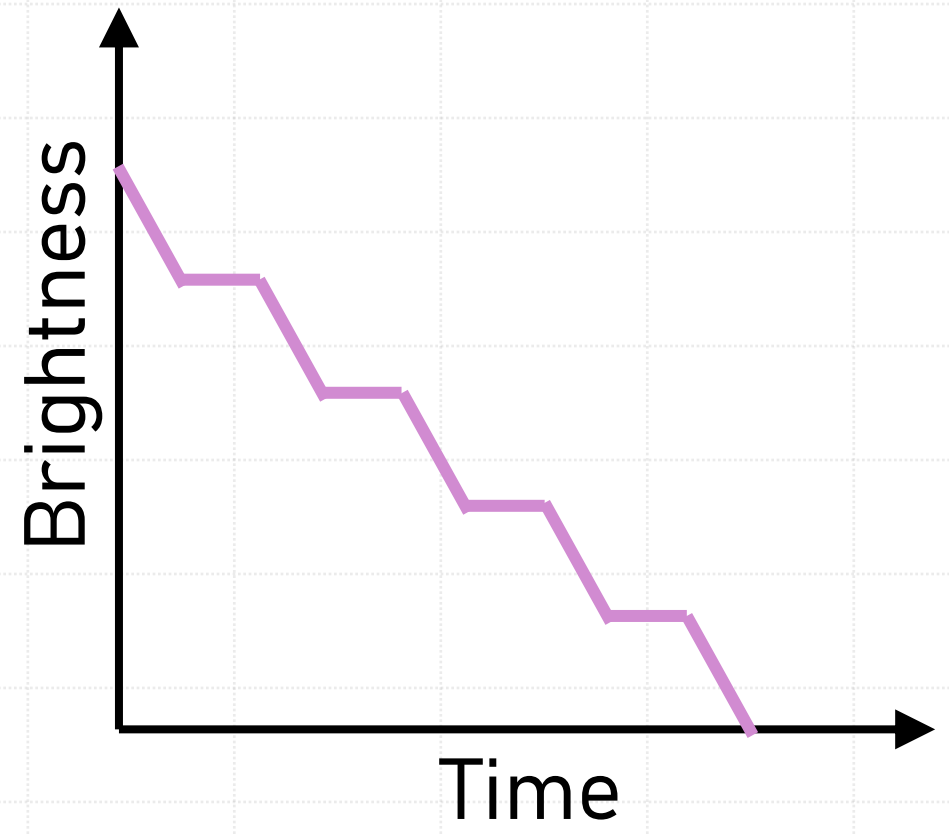
Basic concepts of 3D mapping

1. The 3D info comes from the shape and wavelength-dependence of the light curve
2. Extracting that info requires applying assumptions

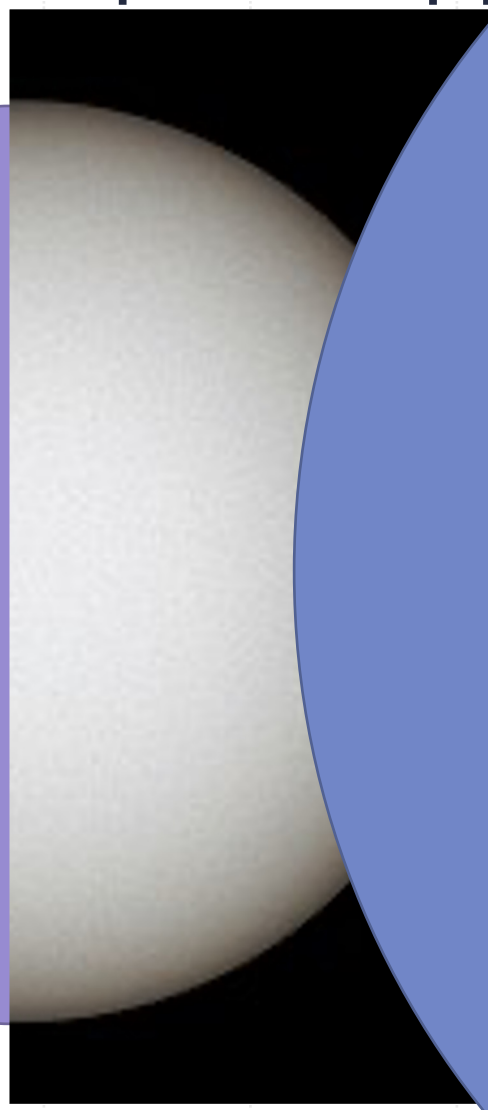
Eclipse mapping: a cartoon example



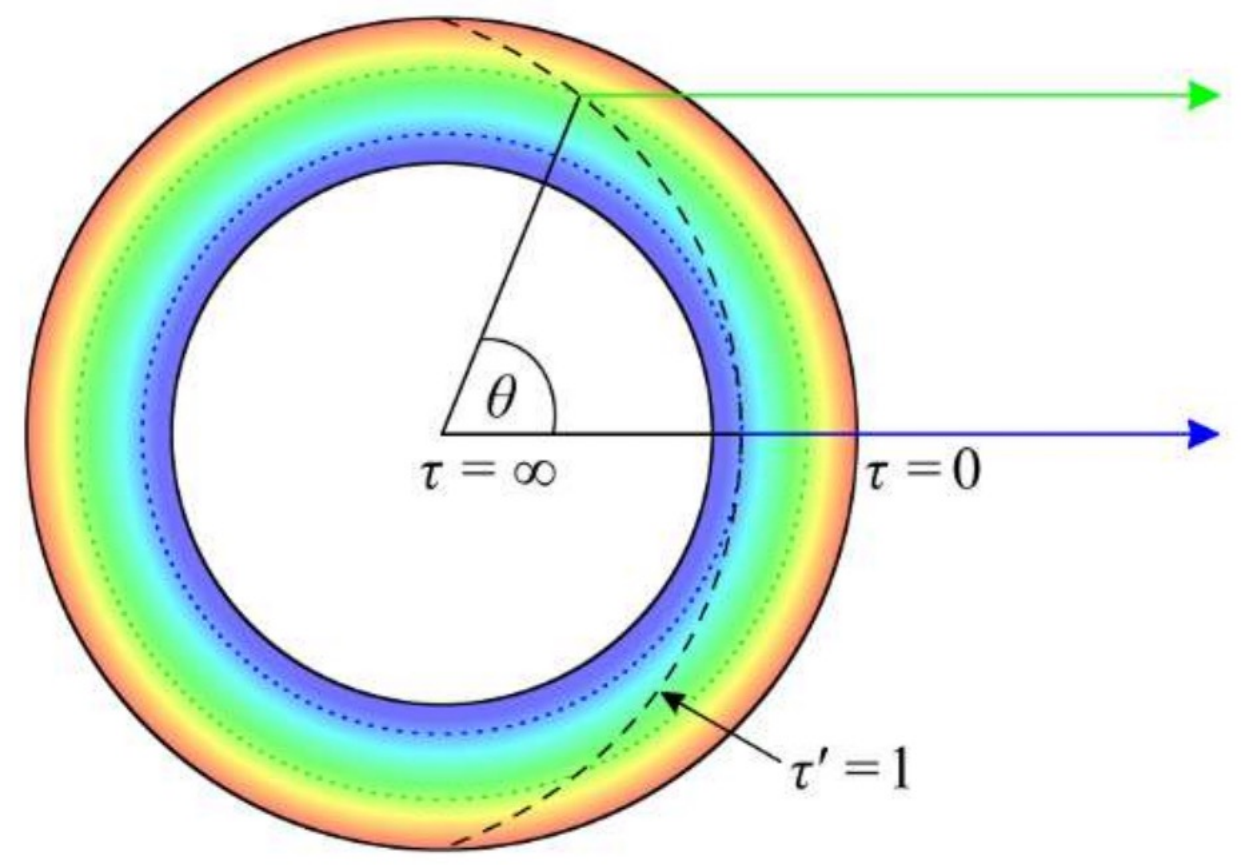
Eclipse mapping: a cartoon example



Eclipse mapping



- How to access 3D info:
 - Latitude and longitude come from the shape of the light curve
 - Depth into the atmosphere comes from spectral differences



Eclipse mapping: a more complex example

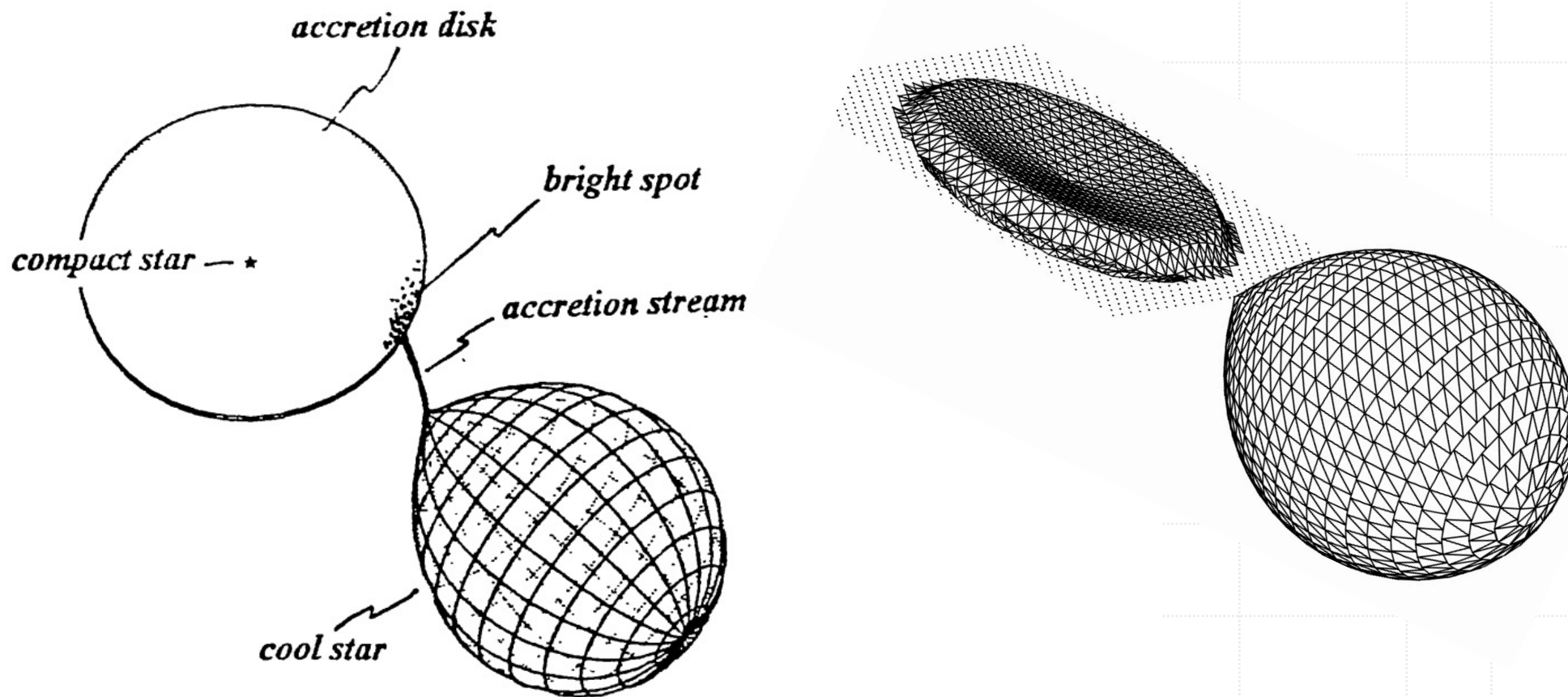
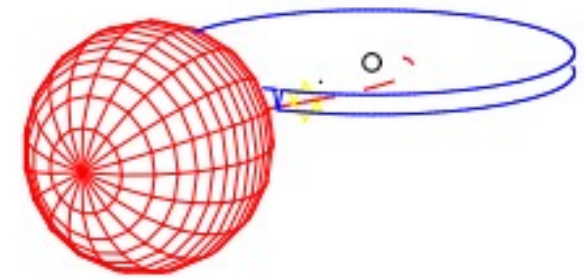
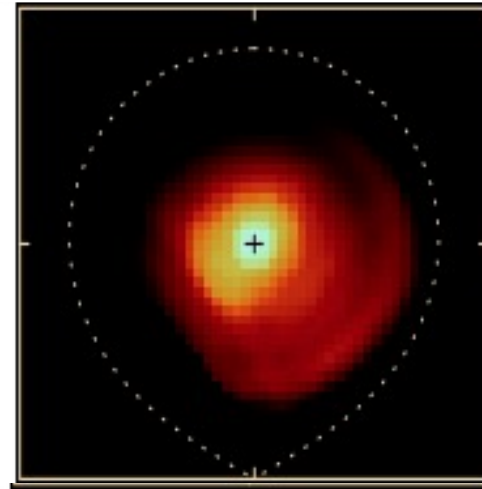
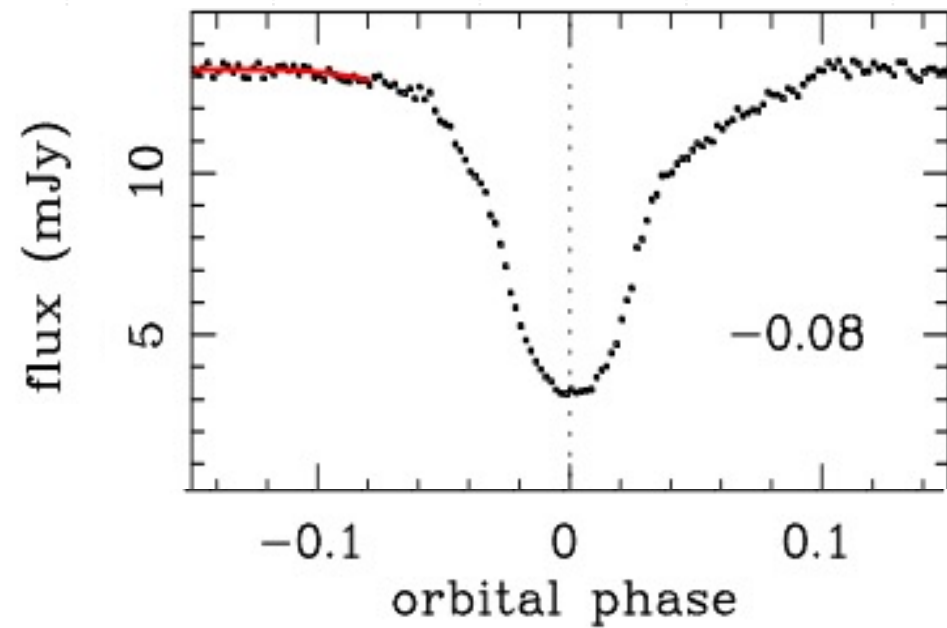
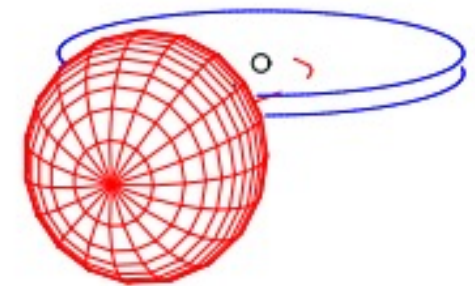
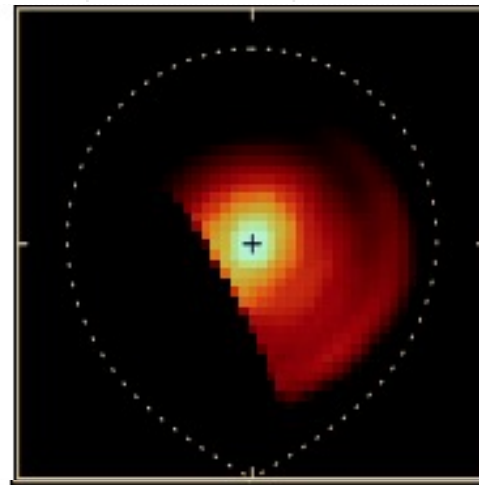
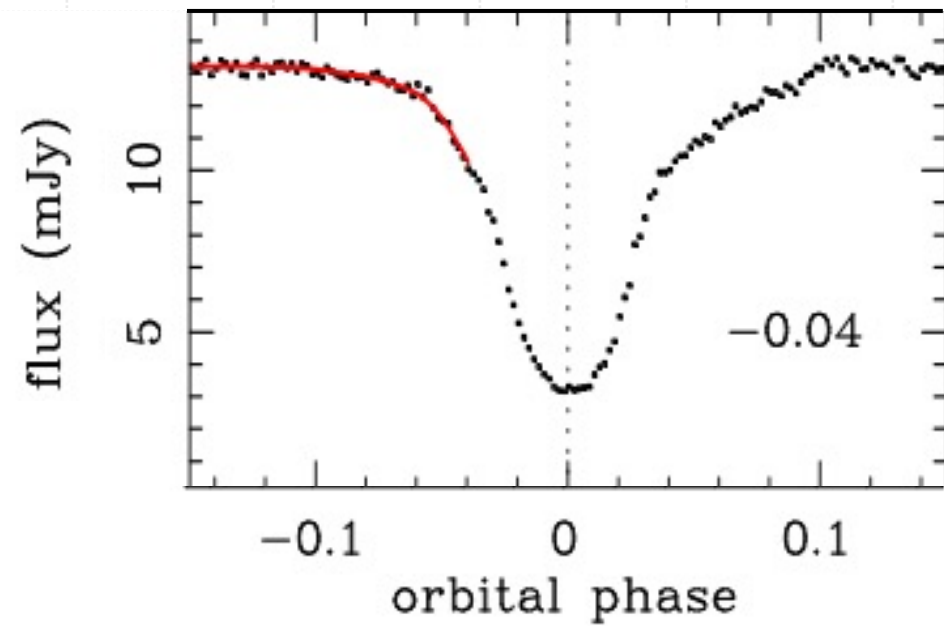


Figure 1. Representation of a cataclysmic variable star with the Roche-lobe filling secondary star, the accretion disk, and the compact white dwarf indicated.

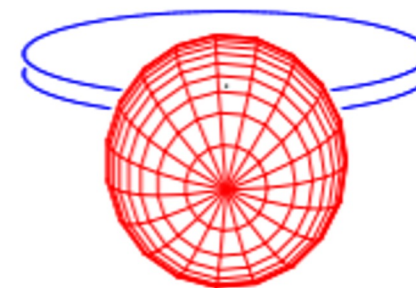
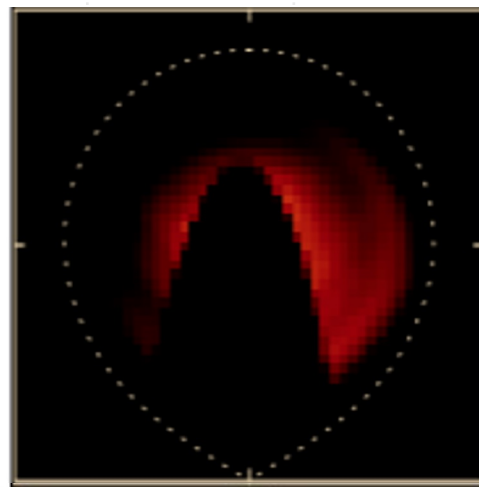
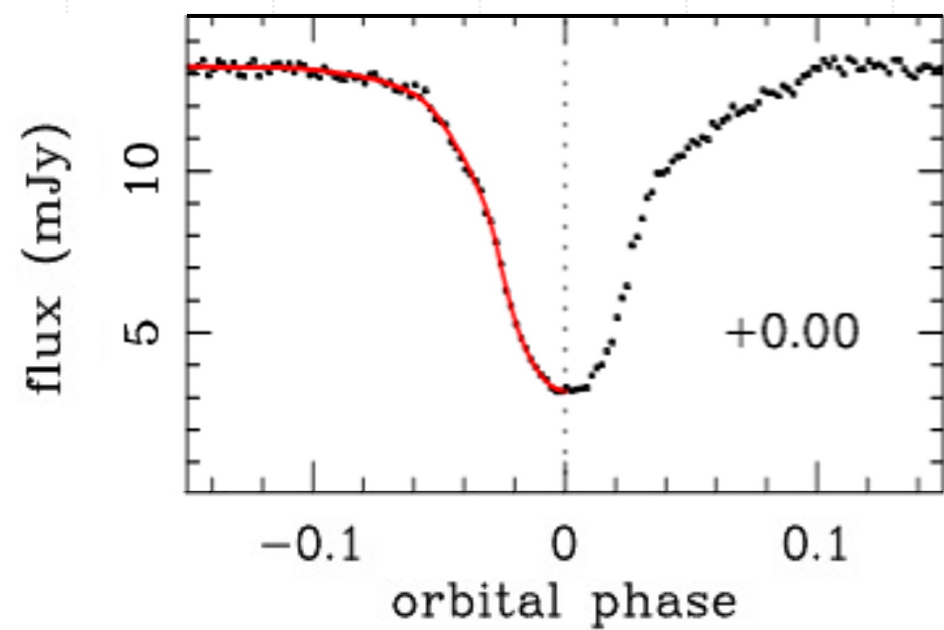
Eclipse mapping: a more complex example



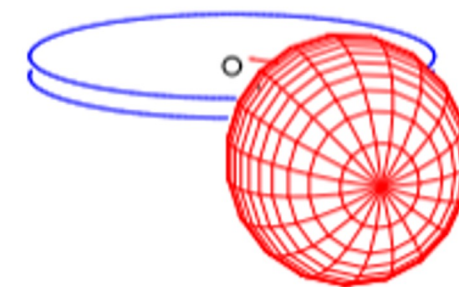
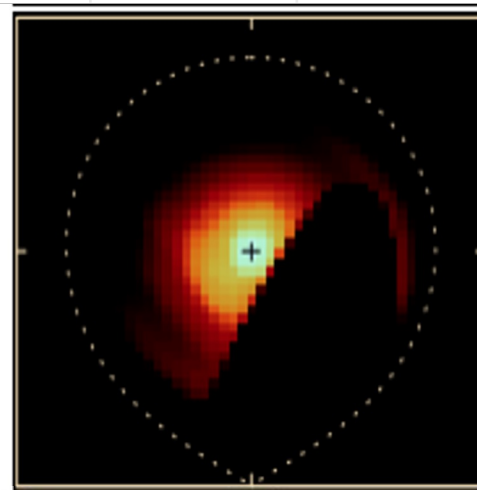
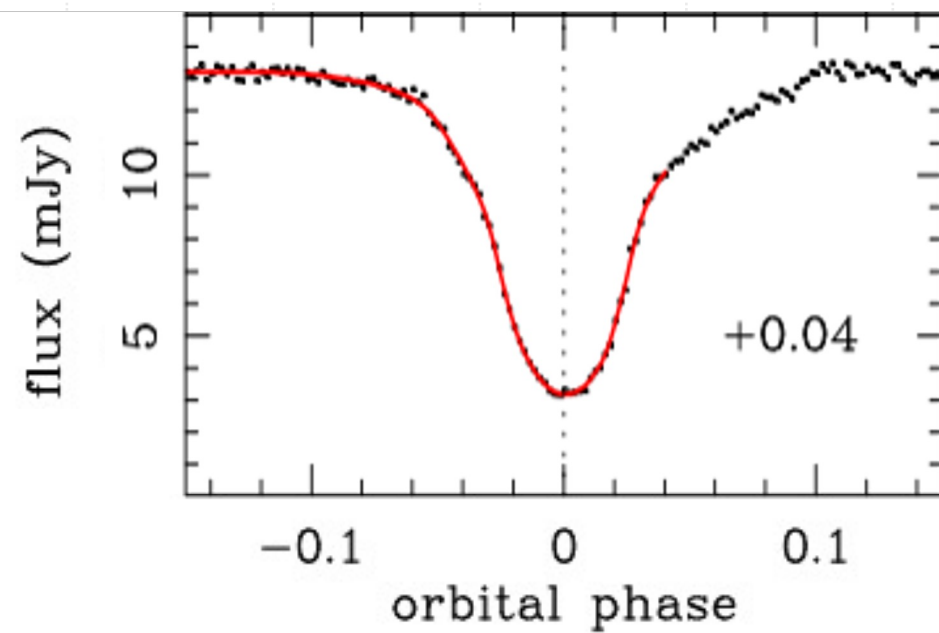
Eclipse mapping: a more complex example



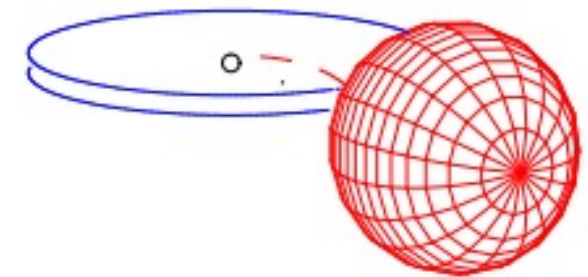
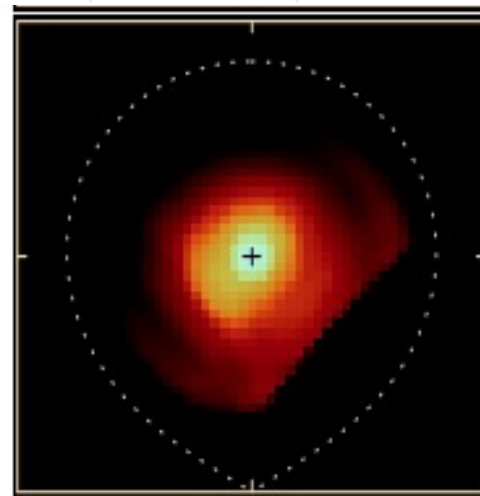
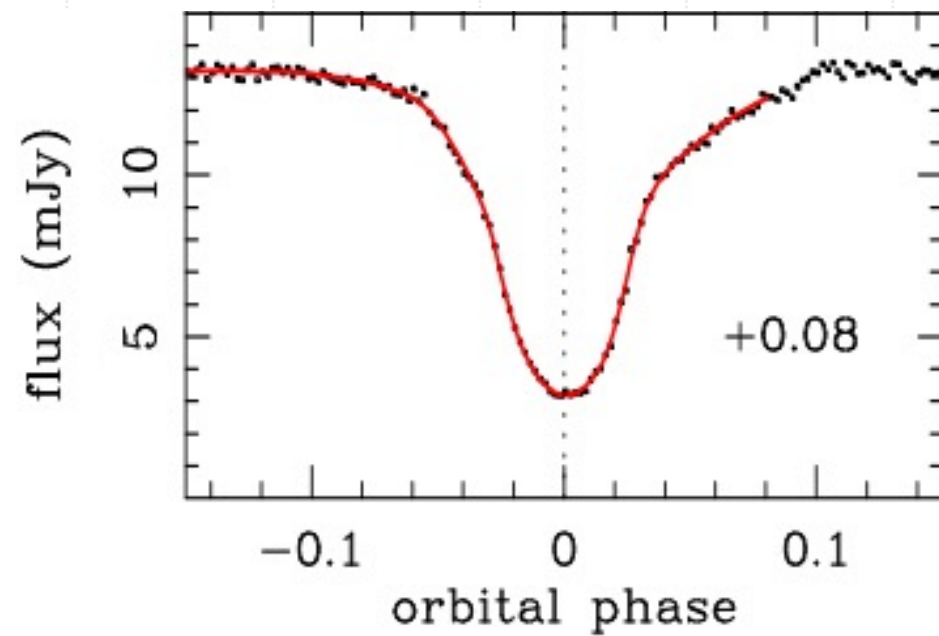
Eclipse mapping: a more complex example



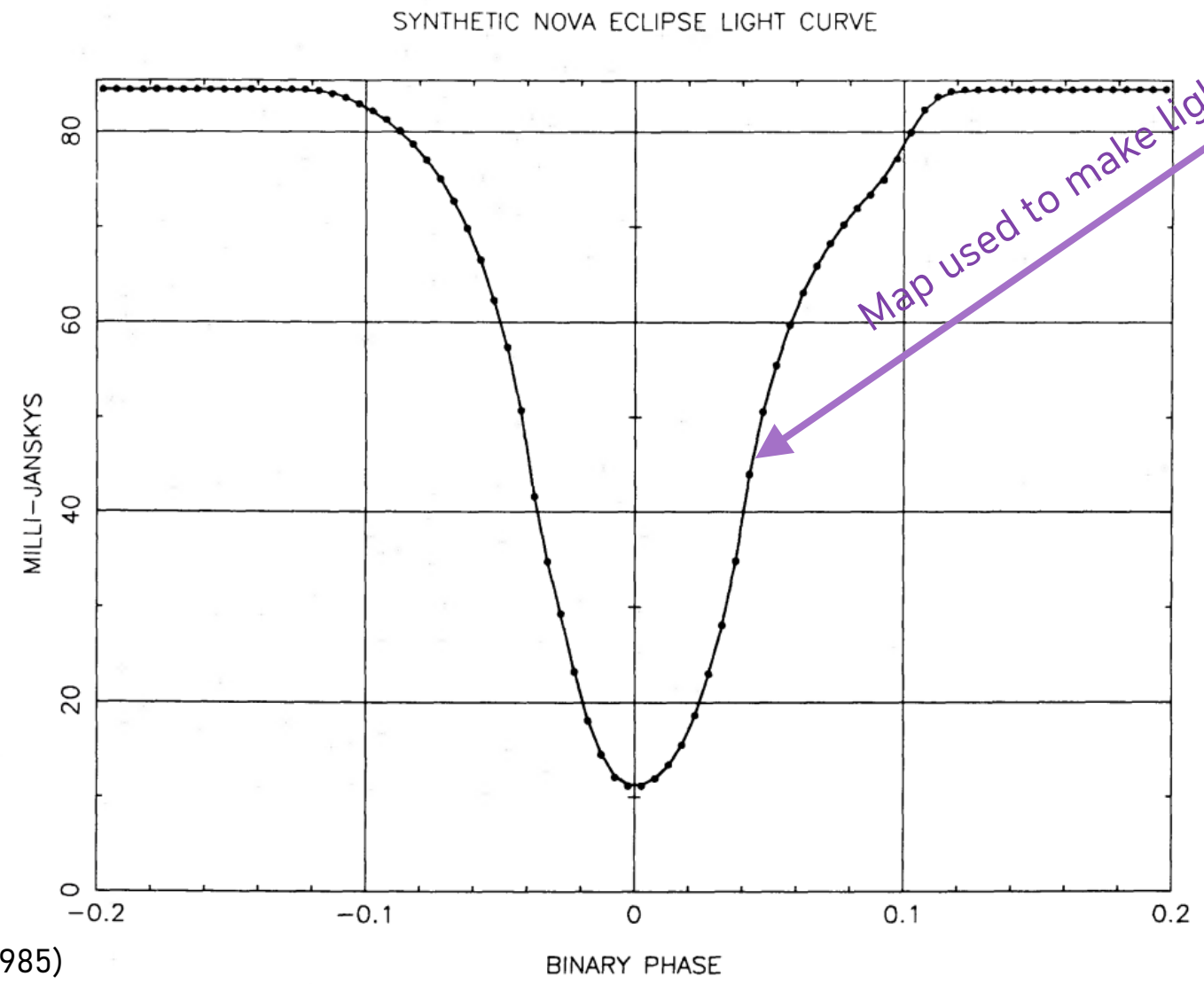
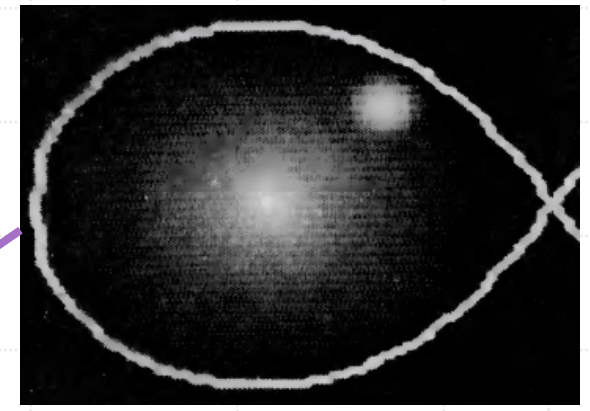
Eclipse mapping: a more complex example



Eclipse mapping: a more complex example

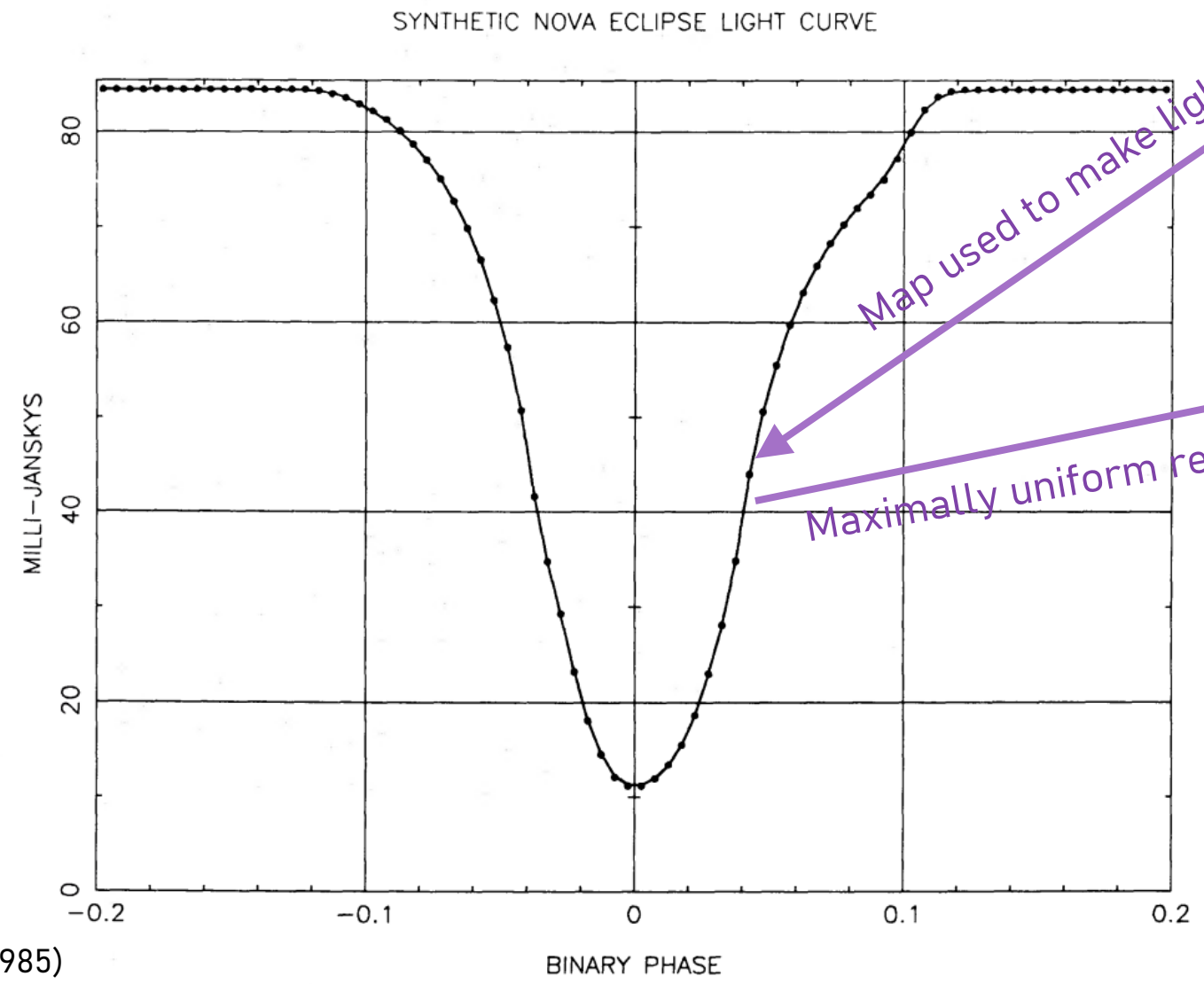


Nuances in creating eclipse maps



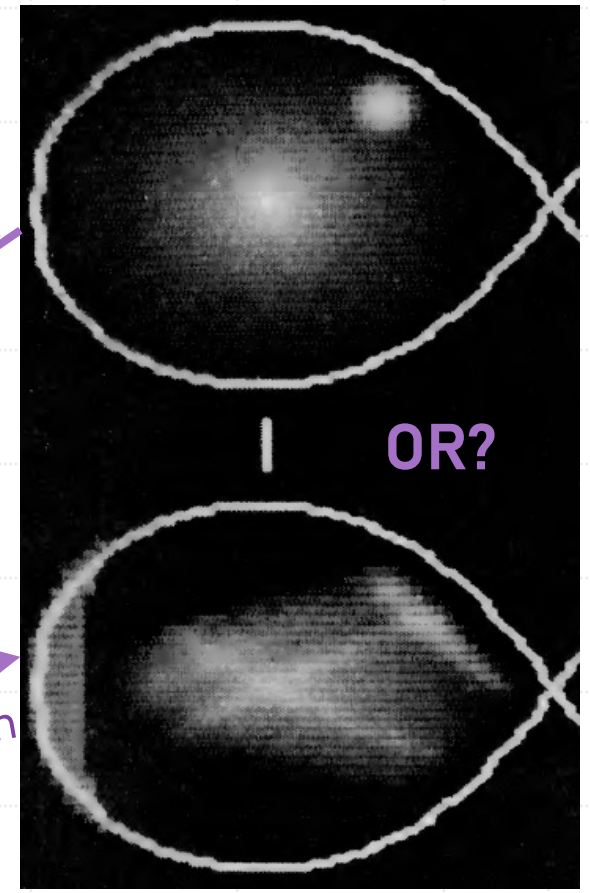
Horne (1985)

Nuances in creating eclipse maps



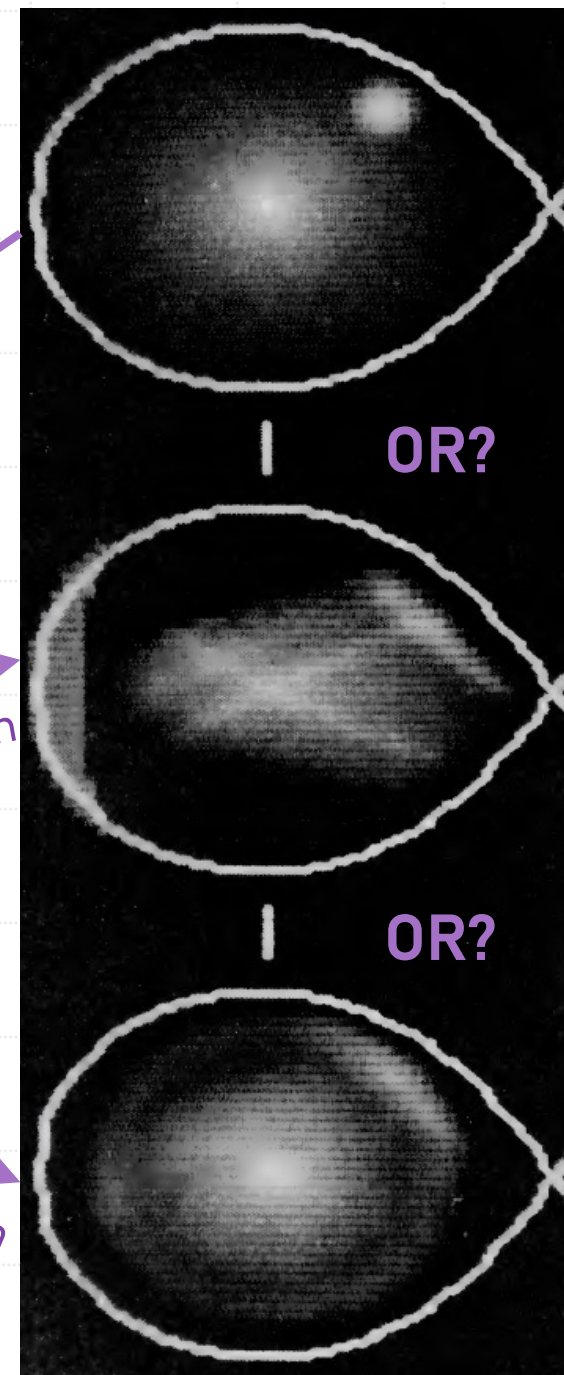
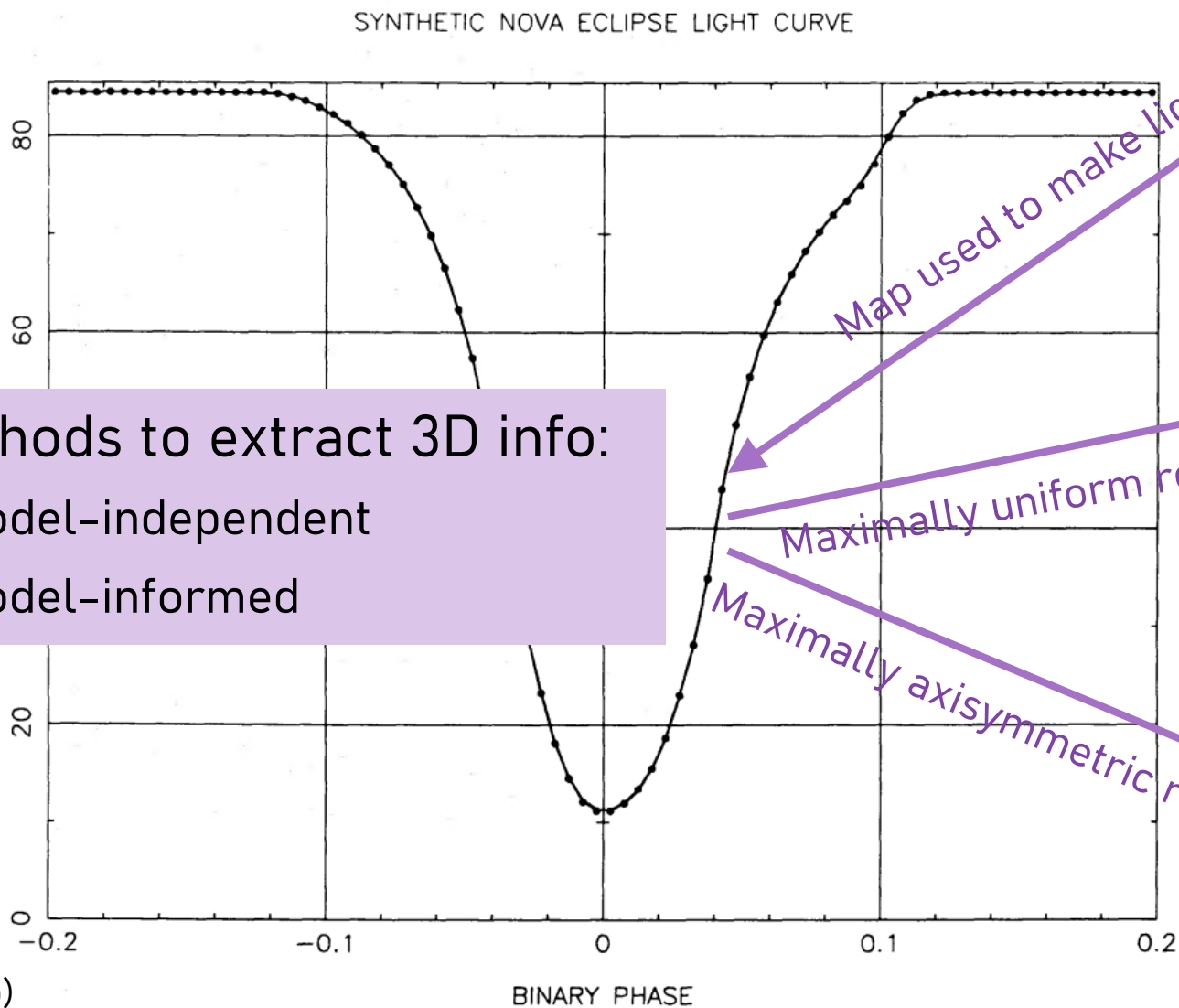
Map used to make light curve

Maximally uniform reconstruction

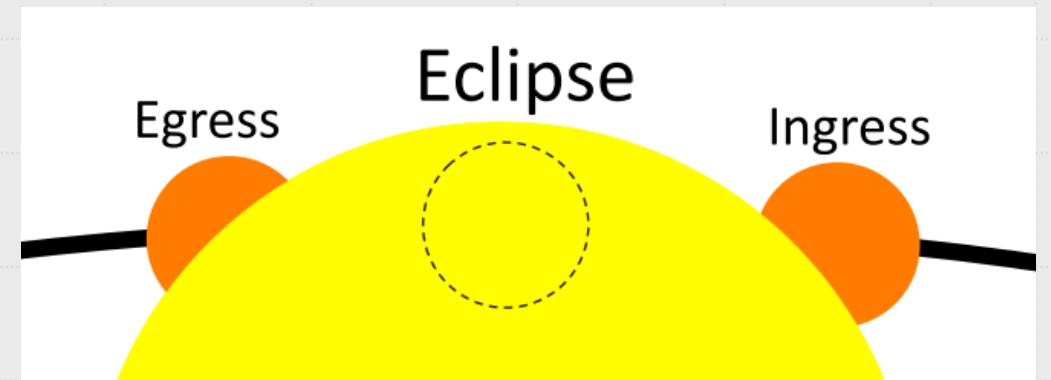


Nuances in creating eclipse maps

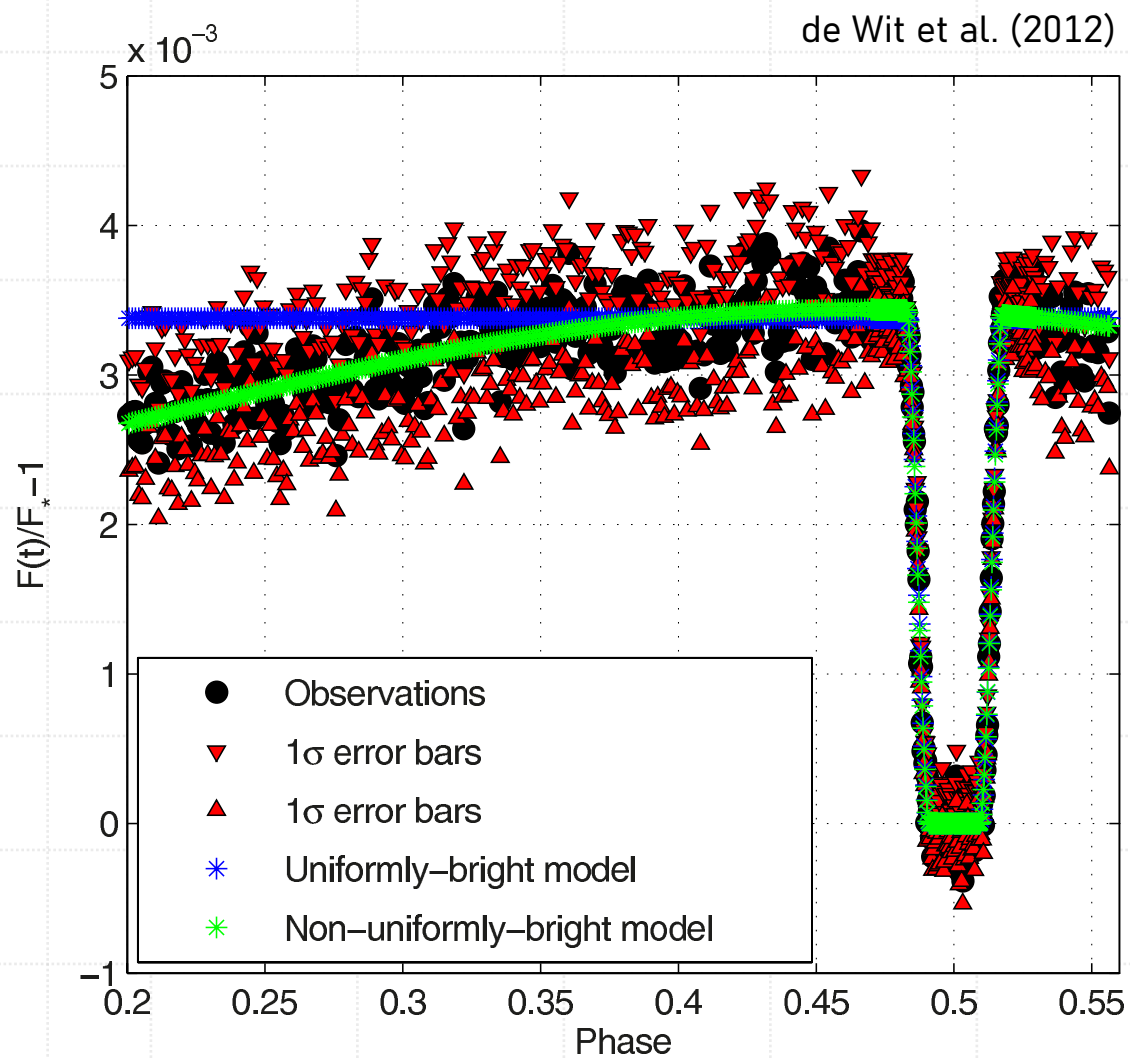
- Methods to extract 3D info:
 - Model-independent
 - Model-informed



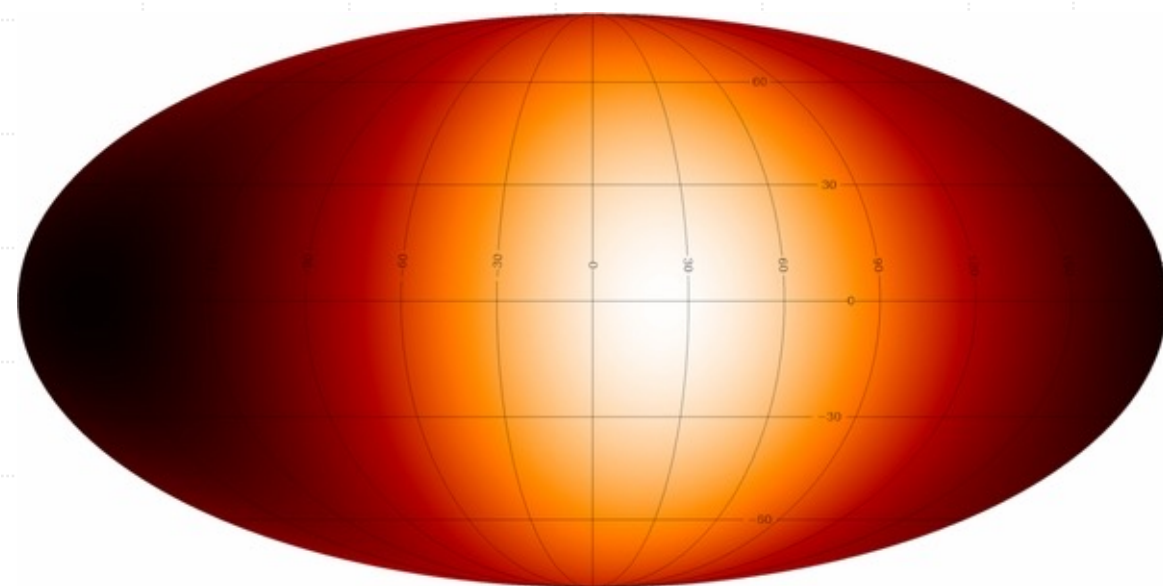
Eclipse mapping



The first (and only) *Spitzer* eclipse map

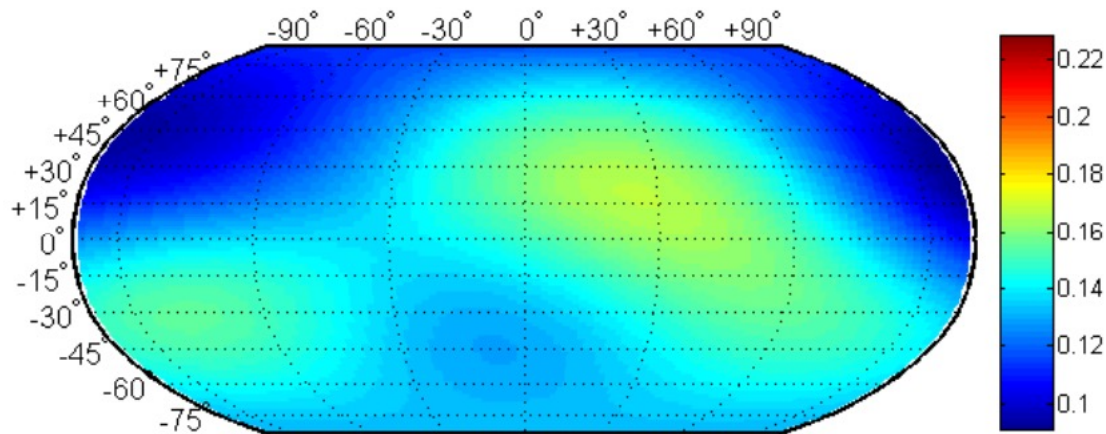
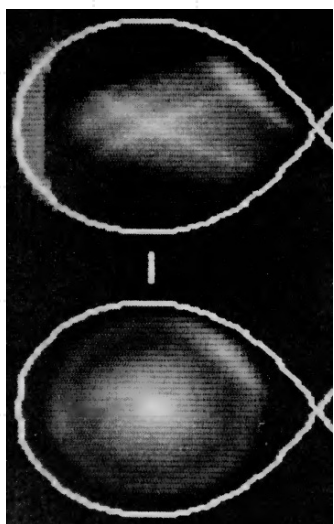


Majeau et al. (2012)



See also Williams et al. (2006); Rauscher et al. (2007)

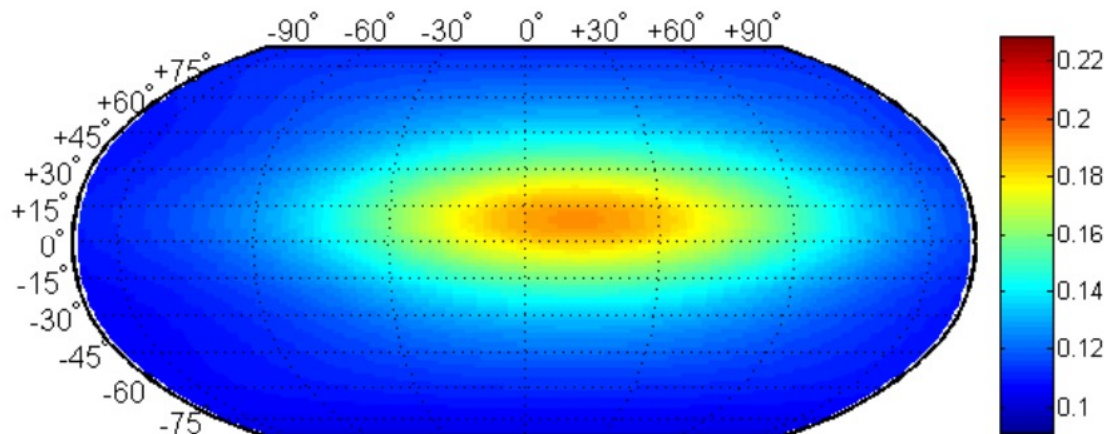
... but it's complicated ... what's the right map to use?



$$\Gamma_{SH,3}(\phi, \theta) = \sum_{l=0}^3 I_l Y_l^0(\phi - \Delta\phi_l, \theta - \Delta\theta_l),$$

Spherical harmonics

OR?

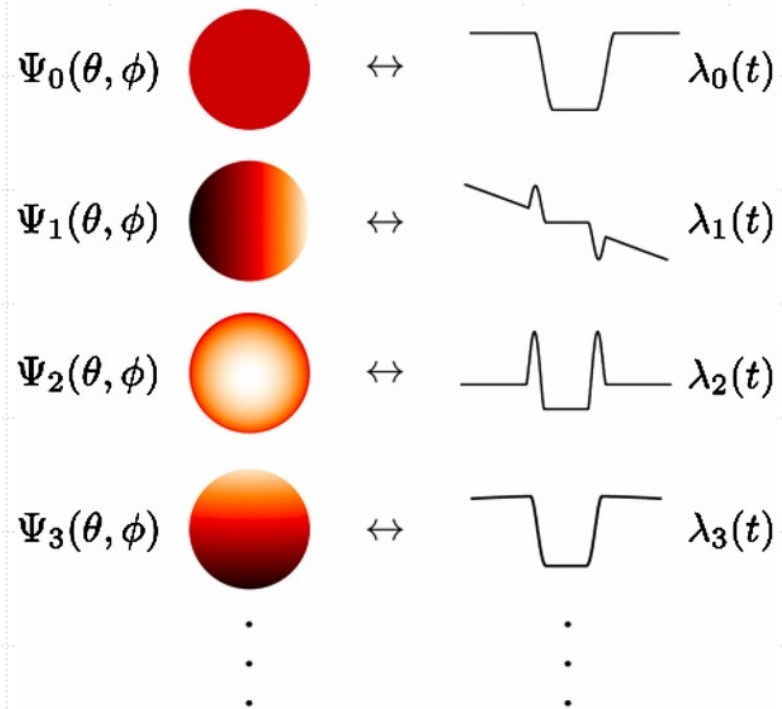


A physical assumption about how the planet should look

$$\Gamma_2(\phi, \theta) = \begin{cases} I_1 \cos^\alpha \phi_o \cos^\gamma \theta_o + I_0 & \text{if } \phi_o \geq 0 \\ I_1 \cos^\beta \phi_o \cos^\gamma \theta_o + I_0 & \text{if } \phi_o < 0, \end{cases}$$

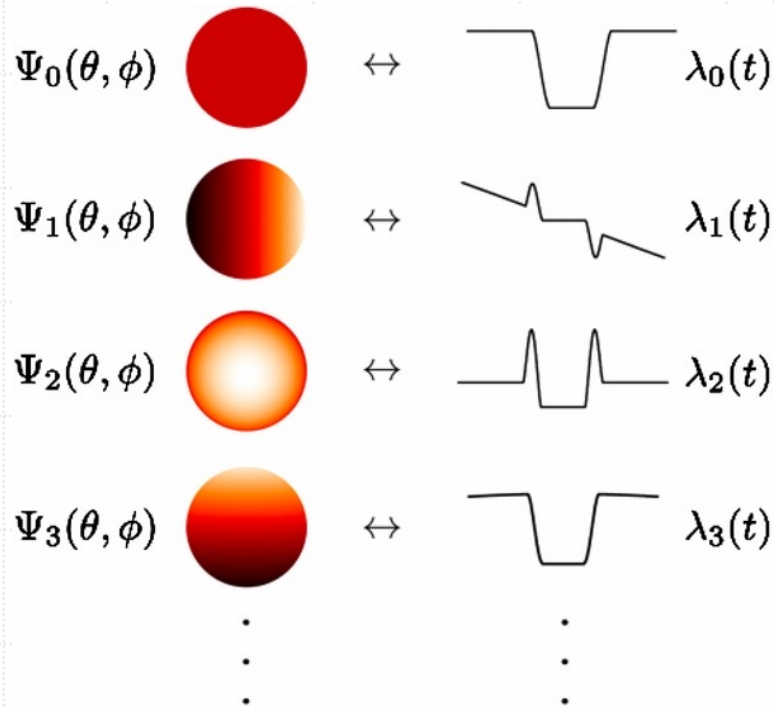
“Eigen-mapping”: a model-independent method

orthogonal
on the planet \leftrightarrow **NOT orthogonal**
in the data



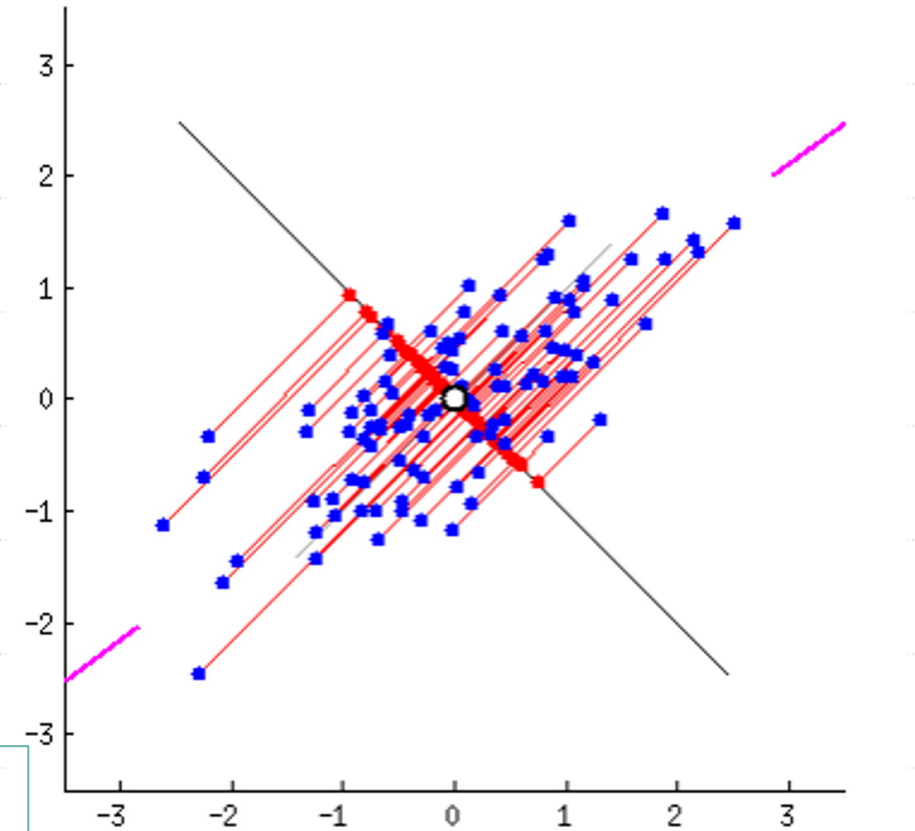
“Eigen-mapping”: a model-independent method

Spherical harmonic light curves, $F_l^m(t)$



Principal
Component
Analysis

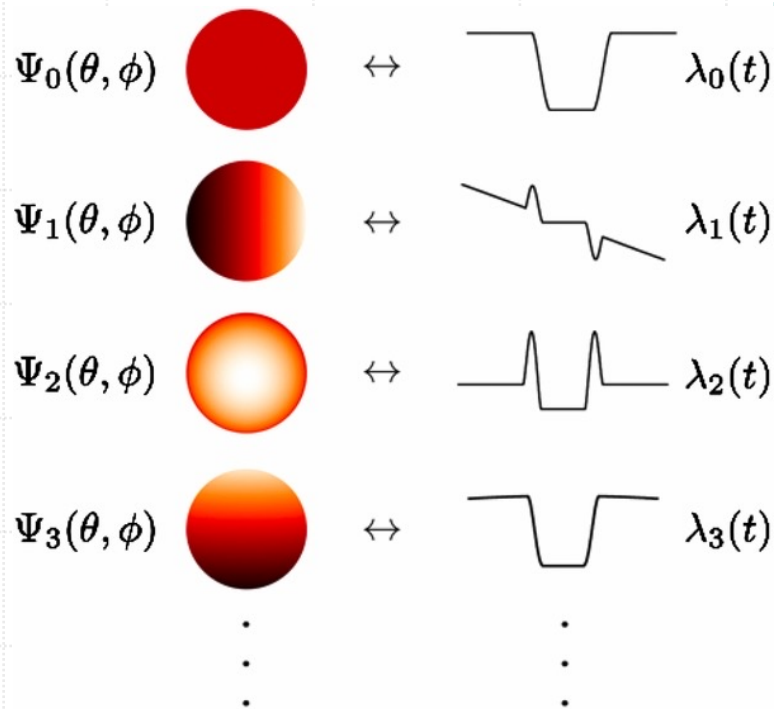
Identifies orthogonal
and maximally
informative light curves



From: <https://medium.com/analytics-vidhya>

“Eigen-mapping”: a model-independent method

Spherical harmonic light curves, $F_l^m(t)$

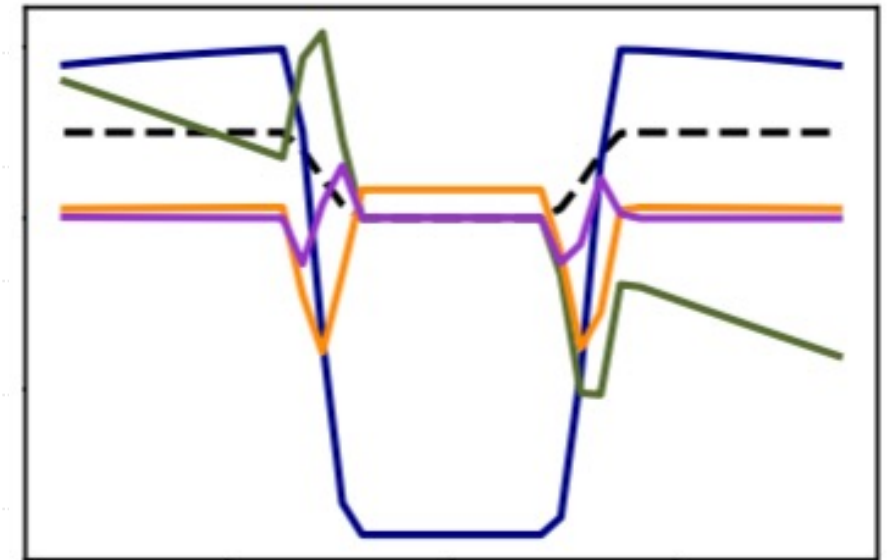


Majeau et al. (2012)

$\lambda_{n,l,m}$

Principal
Component
Analysis

“Eigen-curves”, $E_n(t)$

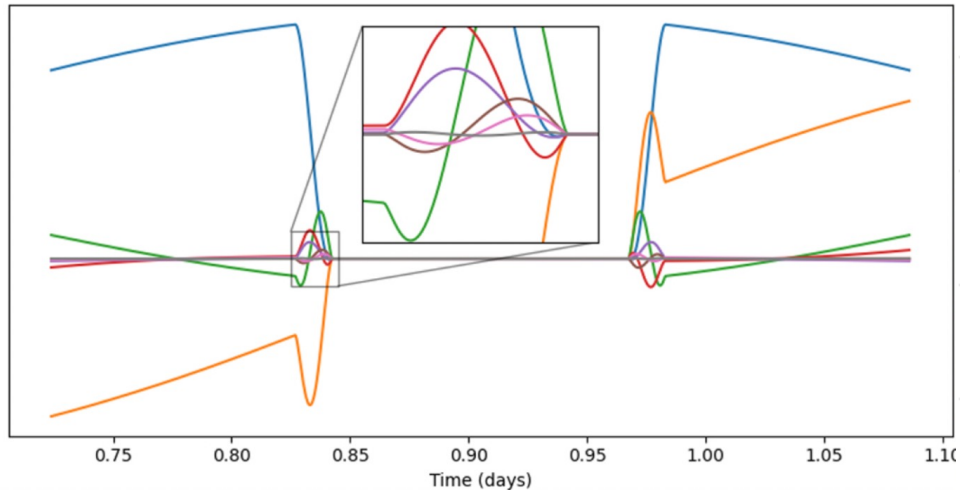


$$E_n(t) = \sum_{l=1}^{l_{\max}} \sum_{m=0}^{\pm l} \lambda_{n,l,m} F_l^m(t)$$

Rauscher et al. (2018)

“Eigen-mapping”: a model-independent method

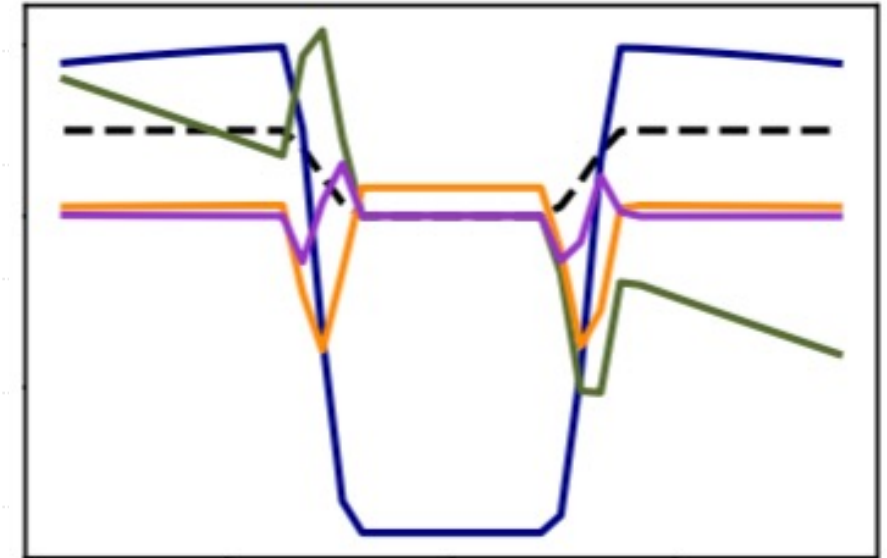
“Eigen-maps”, $Z_n(\theta, \phi)$



Challener & Rauscher (2022)
ThERESA code available on github

$\lambda_{n,l,m}$

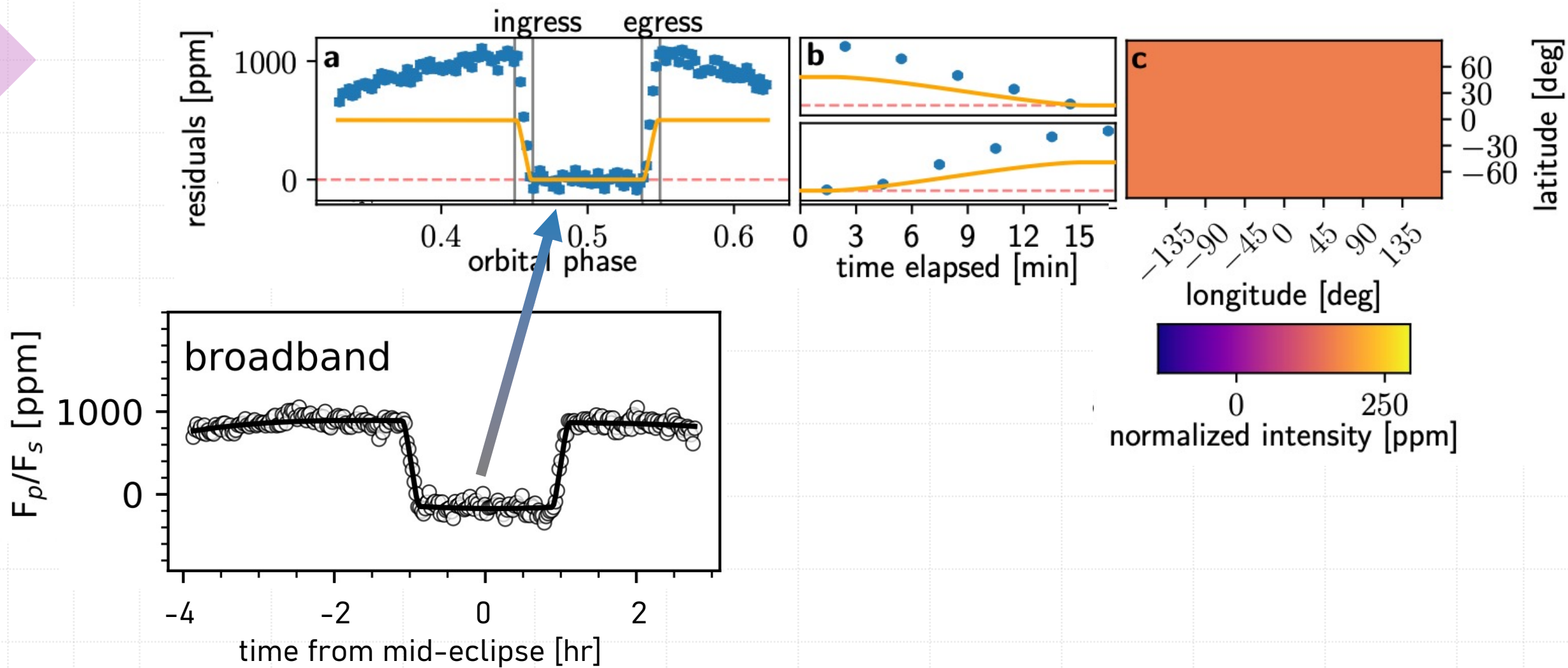
“Eigen-curves”, $E_n(t)$



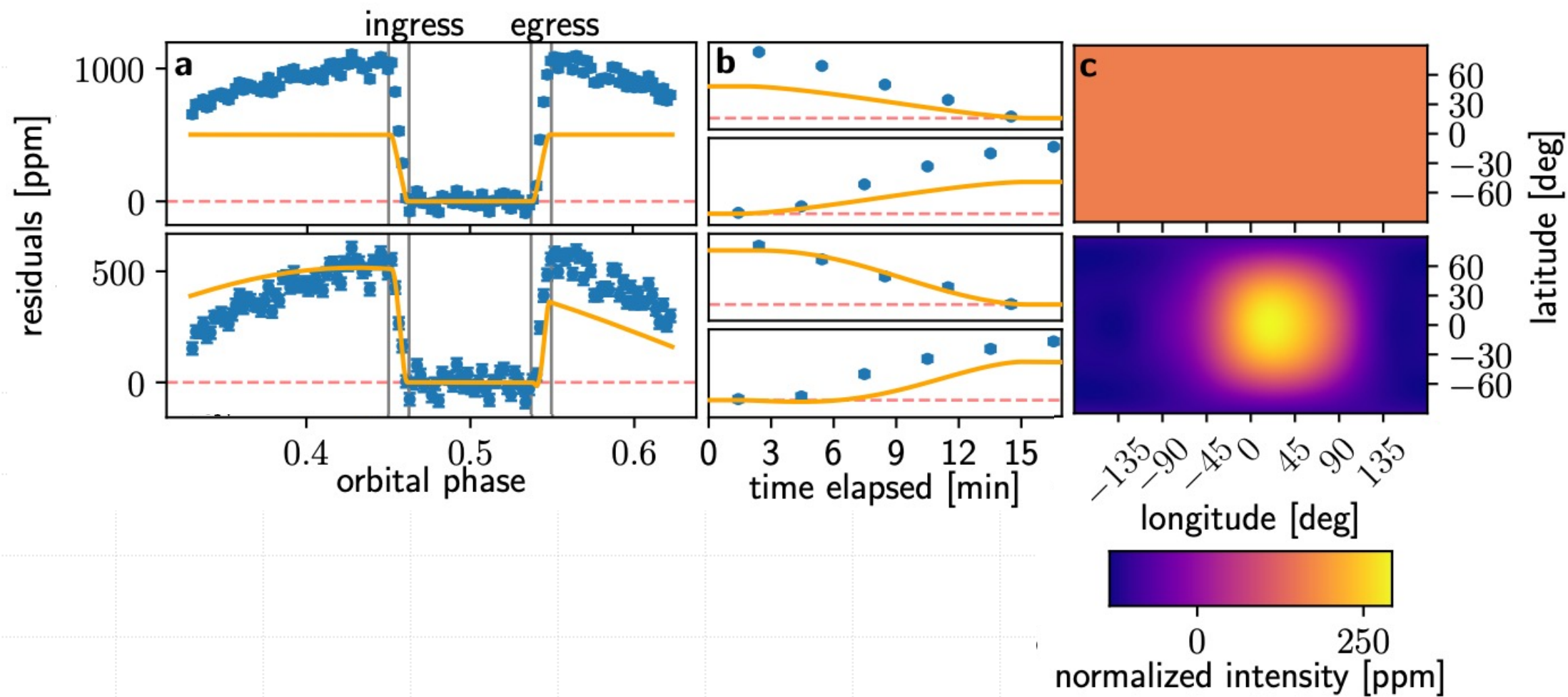
$$Z_n(\theta, \phi) = \sum_{l=1}^{l_{\max}} \sum_{m=0}^{\pm l} \lambda_{n,l,m} Y_l^m(\theta, \phi)$$

Rauscher et al. (2018)

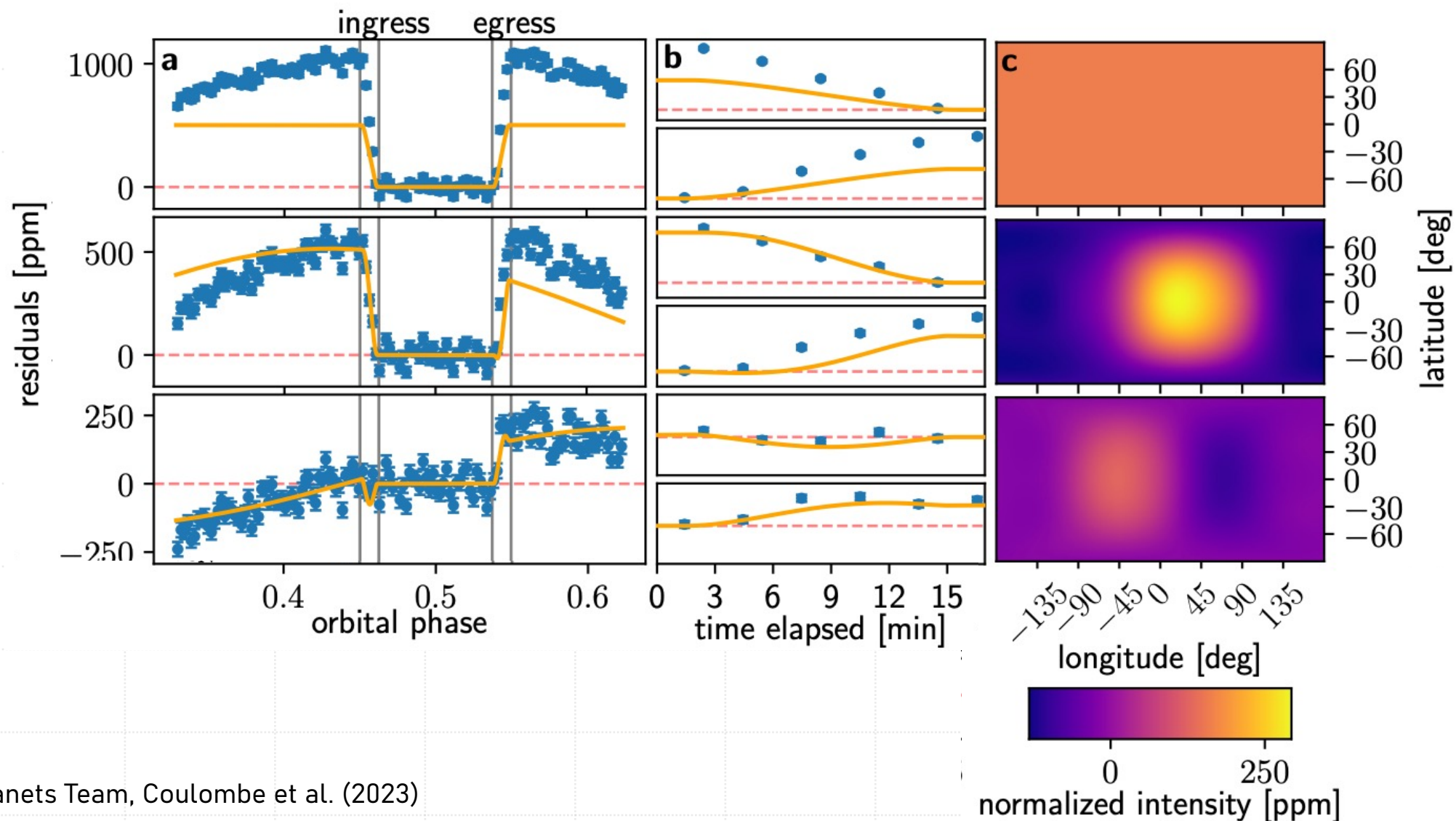
The *first* eclipse map with JWST!



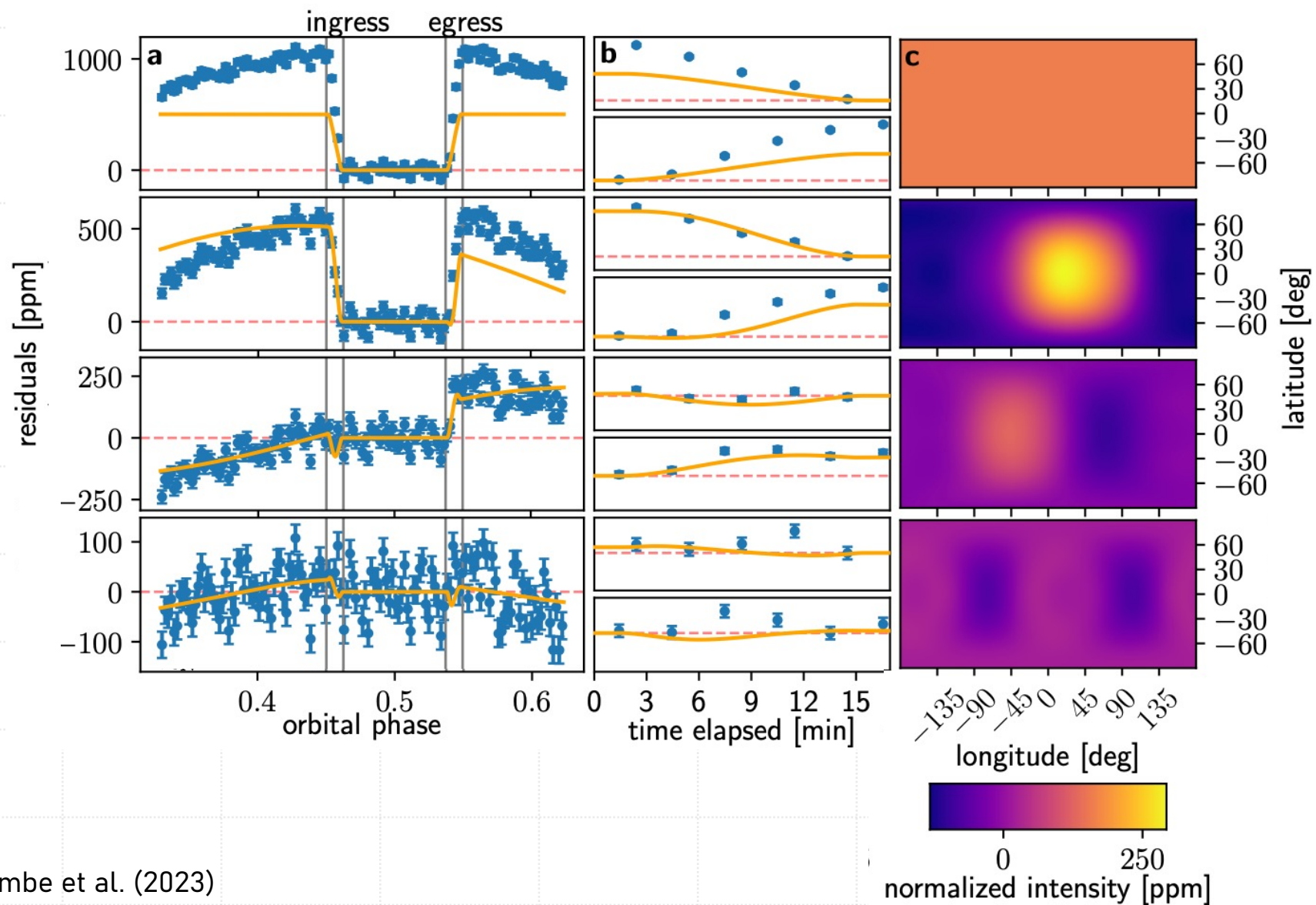
The *first* eclipse map with JWST!



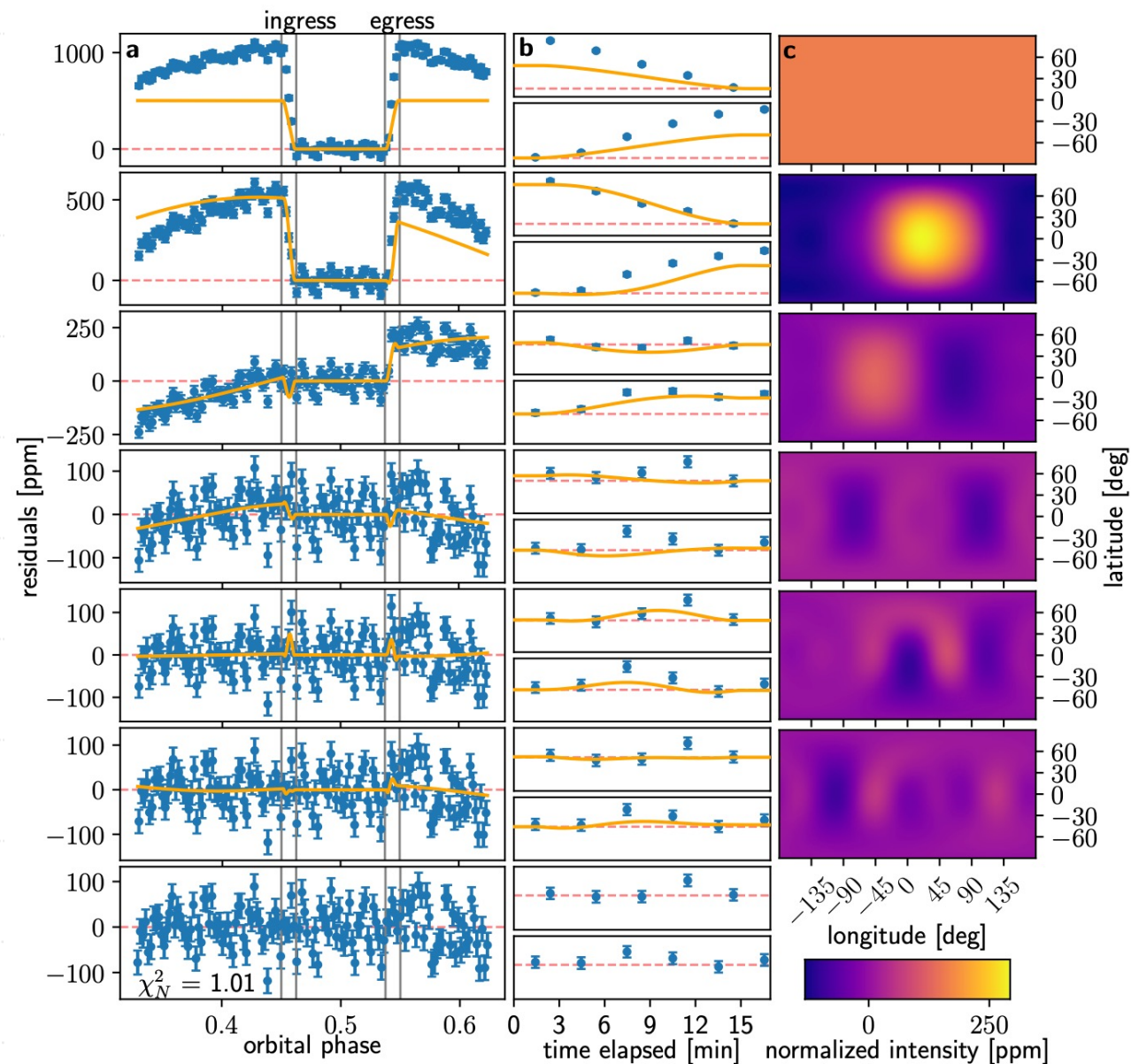
The *first* eclipse map with JWST!



The *first* eclipse map with JWST!

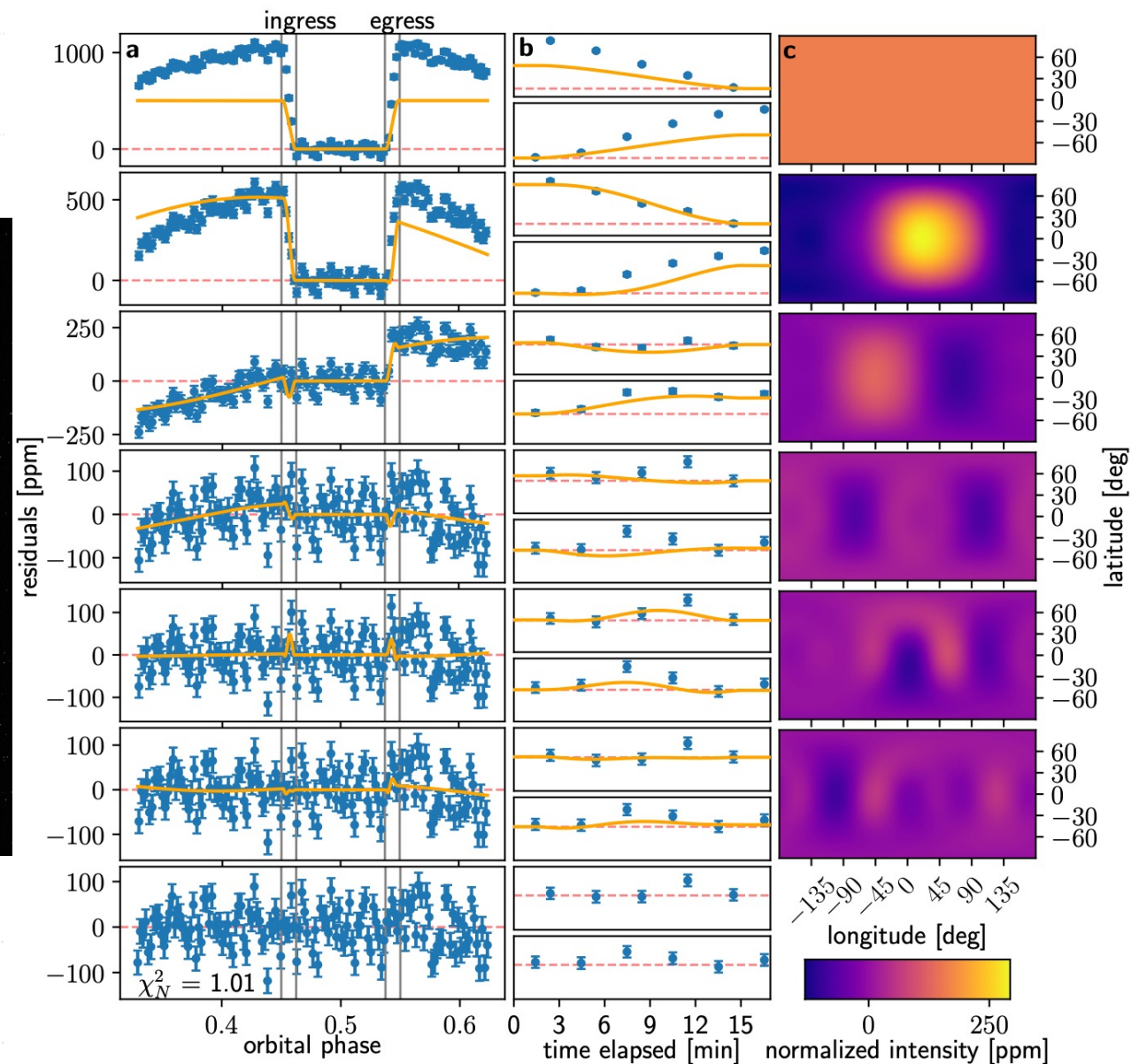


The *first* eclipse map with JWST!



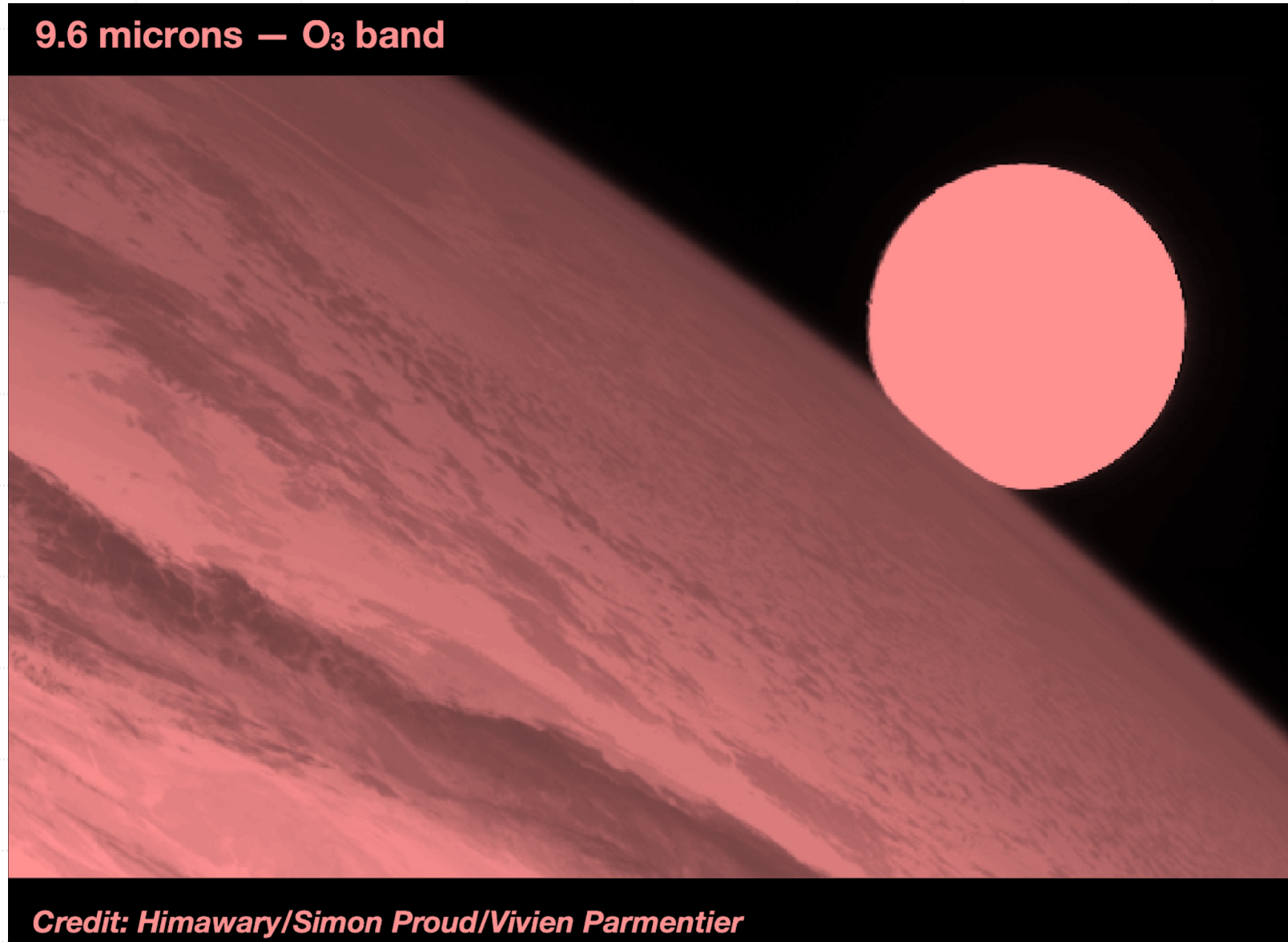
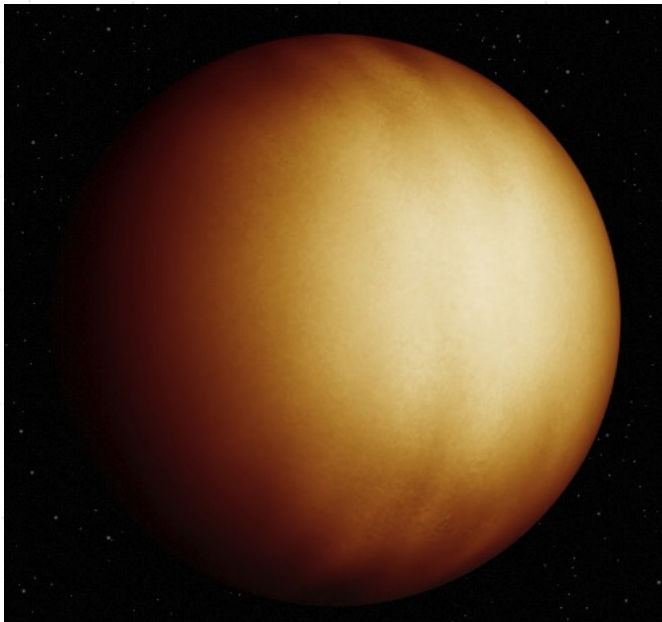
The *first* eclipse map with JWST!

Credit: NASA/JPL-Caltech (K. Miller/IPAC)



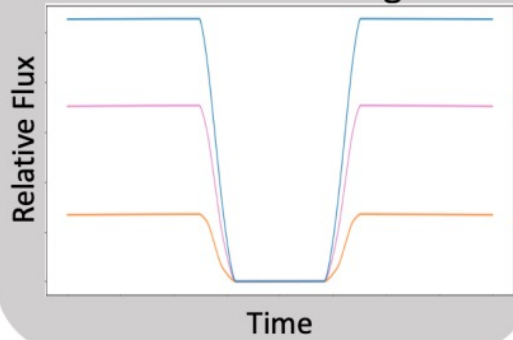
But what about a 3D map?

Thermal emission comes from different layers in the atmosphere

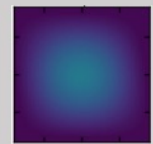
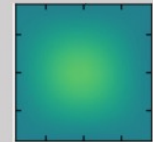
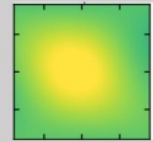


3D Eclipse Mapping Methods:

1. Eclipse light curve at each wavelength

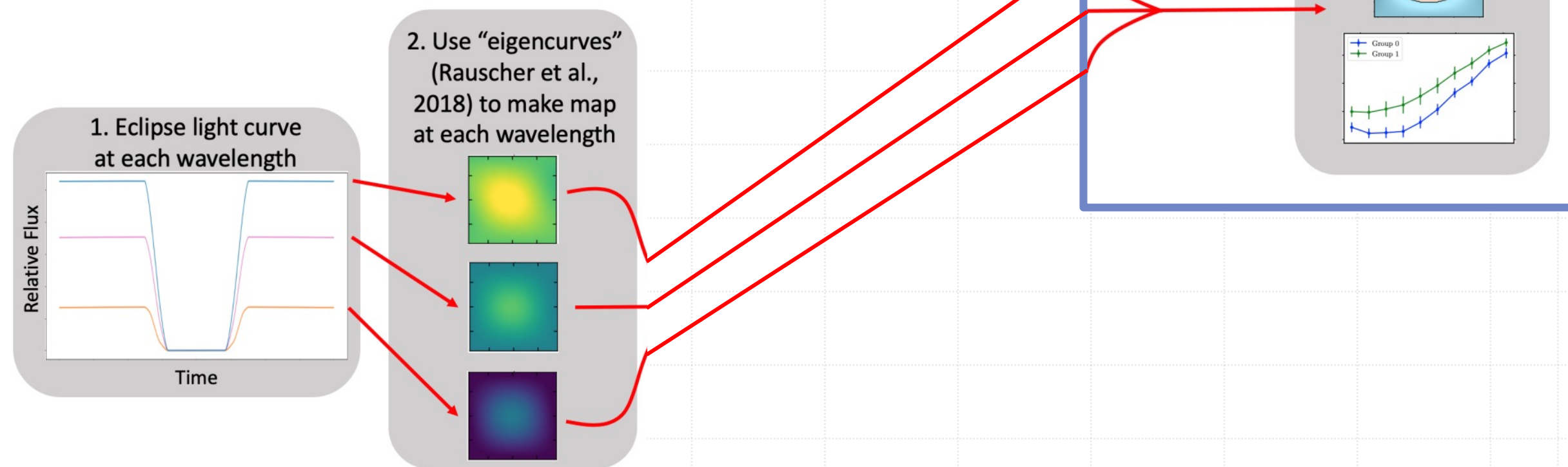


2. Use "eigencurves" (Rauscher et al., 2018) to make map at each wavelength



3D Eclipse Mapping Methods:

Model-independent spectral-spatial groups



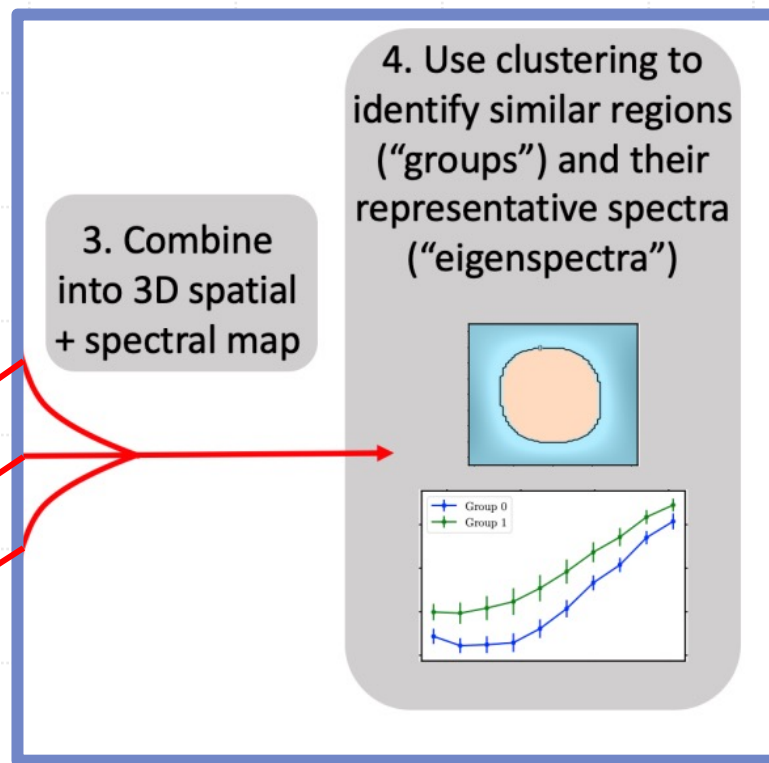
3D Eclipse Mapping Methods: Model-independent spectral-spatial groups

OR

Temperature-pressure parameterization

Stay tuned!

- 3D map of WASP-18b
- More maps:
 - WASP-43b
 - GTO/GO targets
- More techniques
 - parameterizations linking temperature structure to physics
 - what parts of a map we *can't* see (null space)

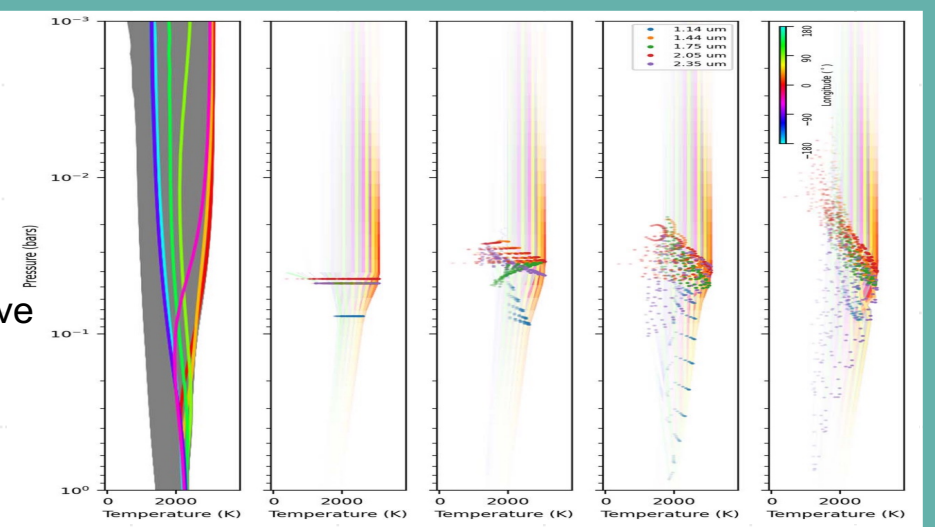


Relative Flux

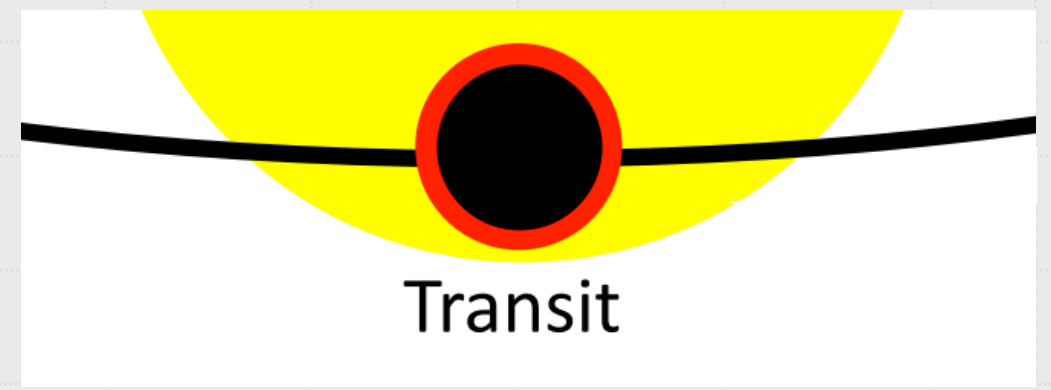


3. Place temperature maps at different pressures

4. Use radiative transfer to match measured spectra

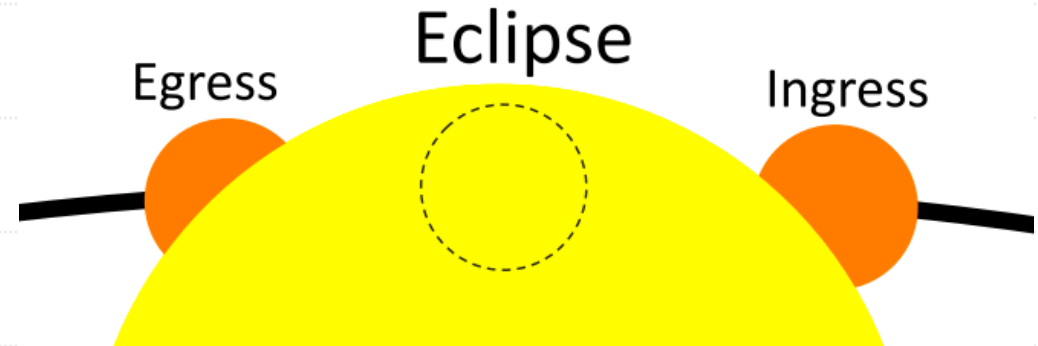
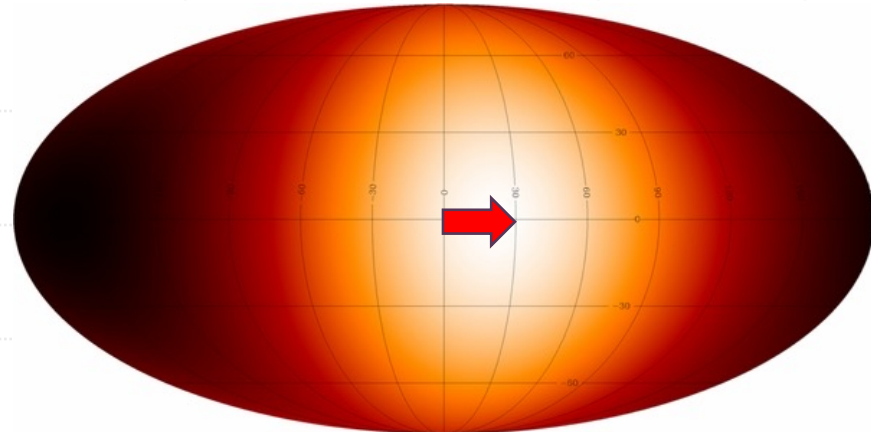


Transit mapping



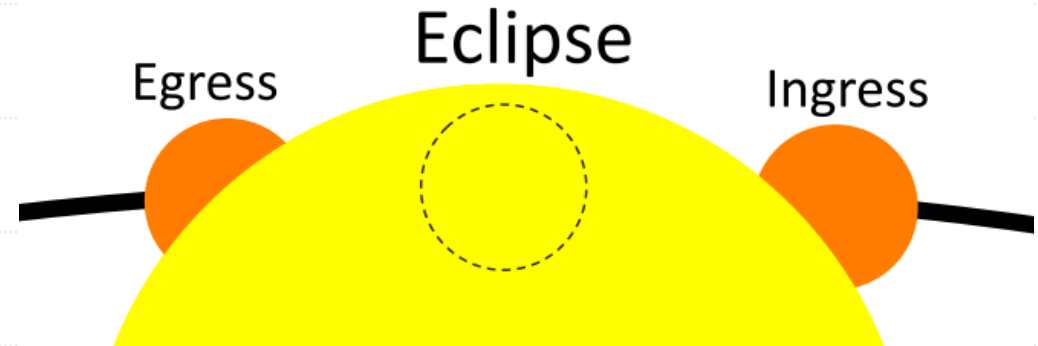
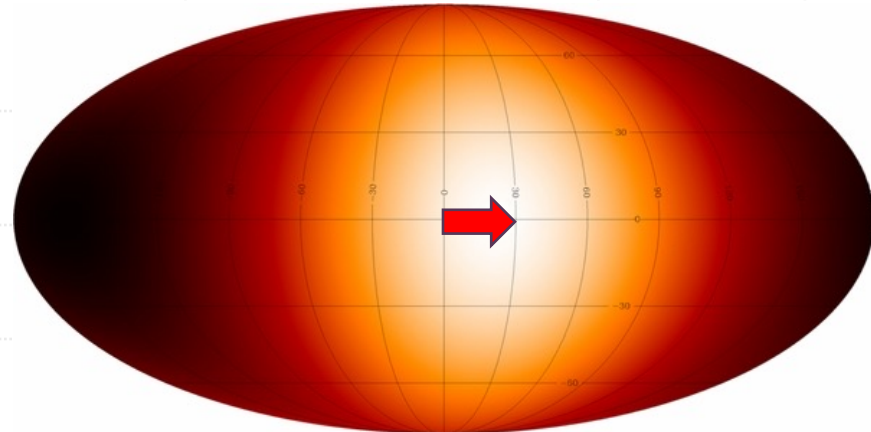
How spatial structure shows up in transit

Dayside facing us

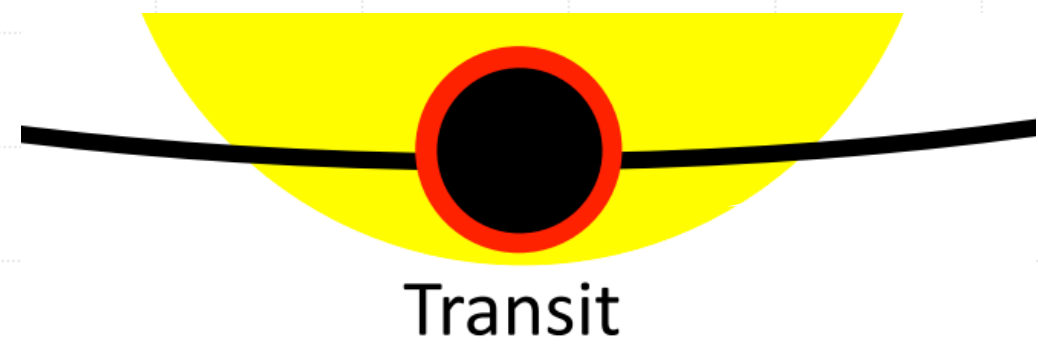
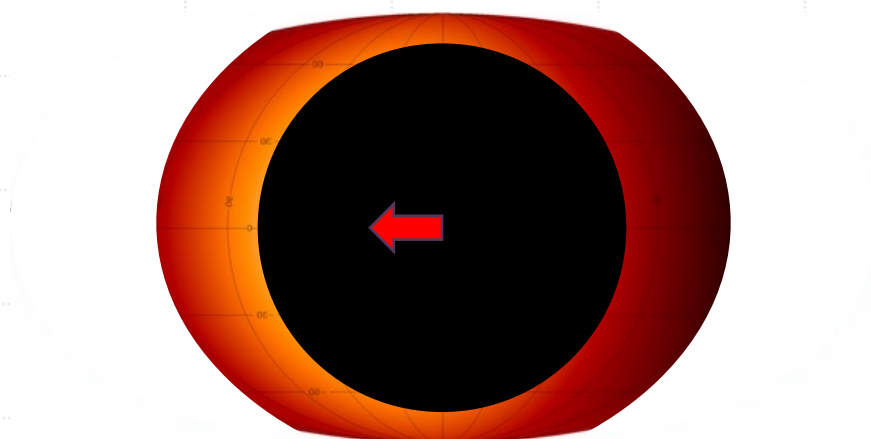


How spatial structure shows up in transit

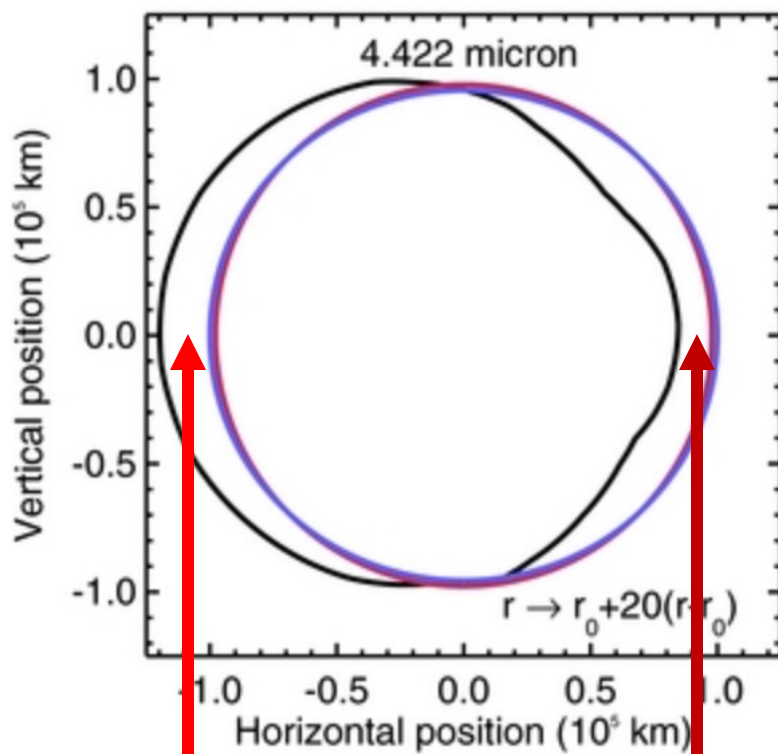
Dayside facing us



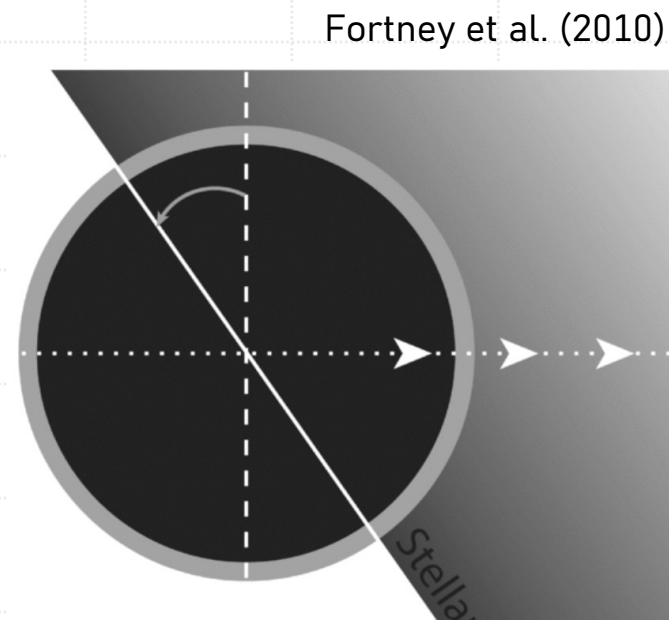
Nightside facing us



How spatial structure shows up in transit



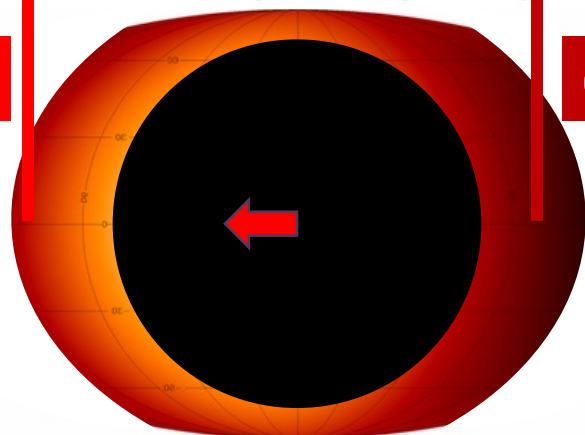
Dobbs-Dixon et al. (2012)



Fortney et al. (2010)

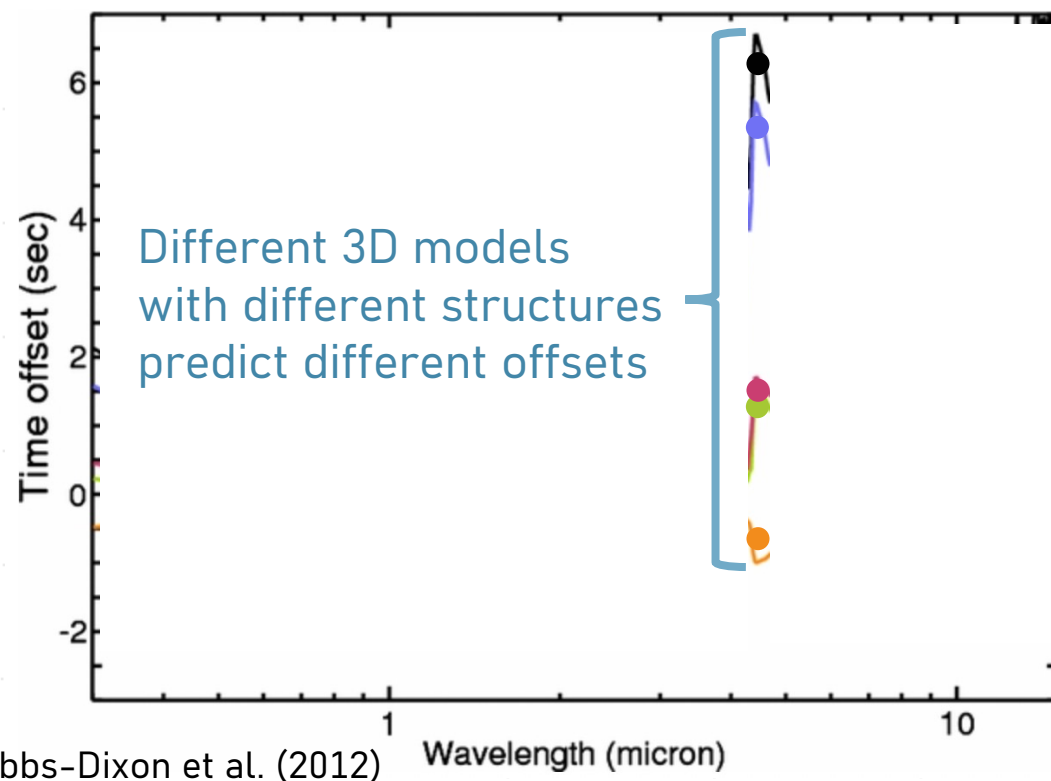
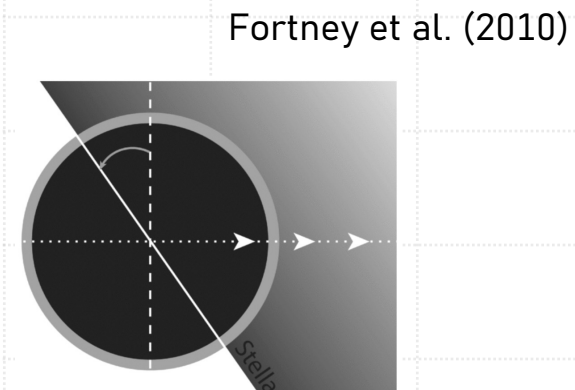
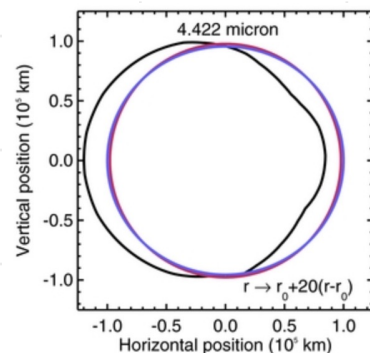
hotter = puffier

cooler = compact

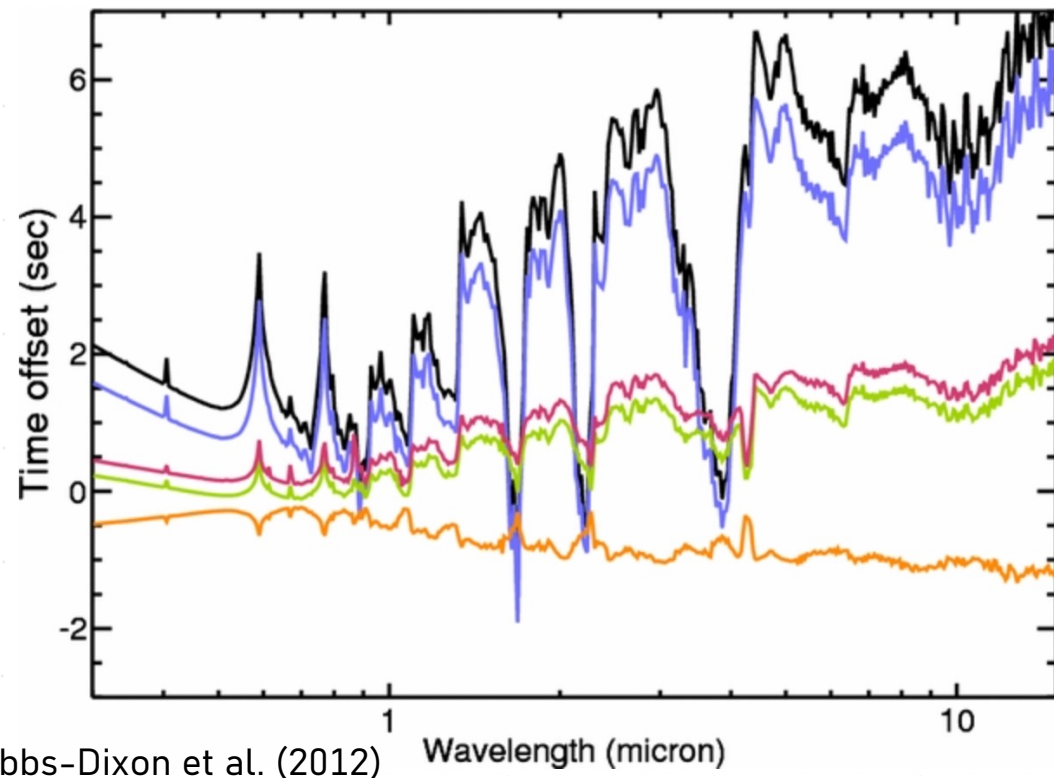
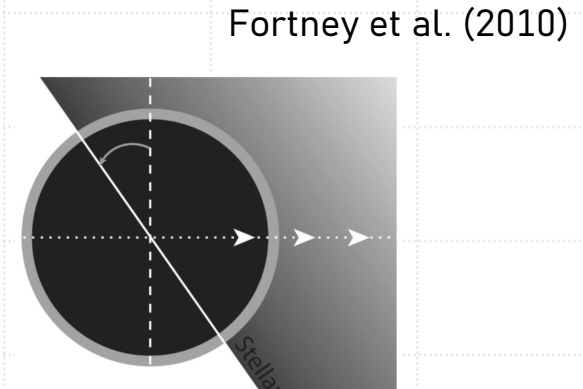
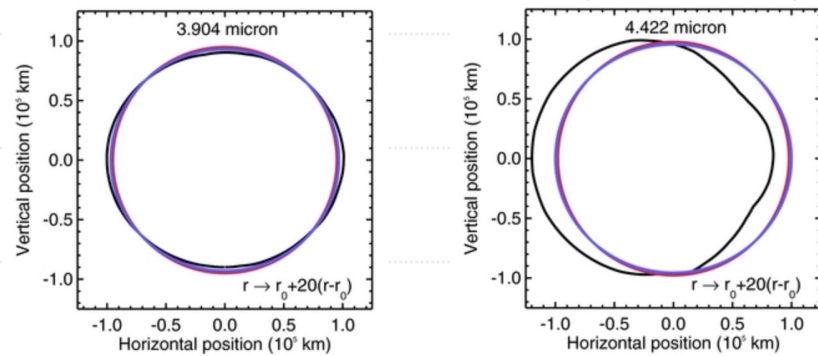


Leading and Trailing terminators
≠
Eastern and Western terminators

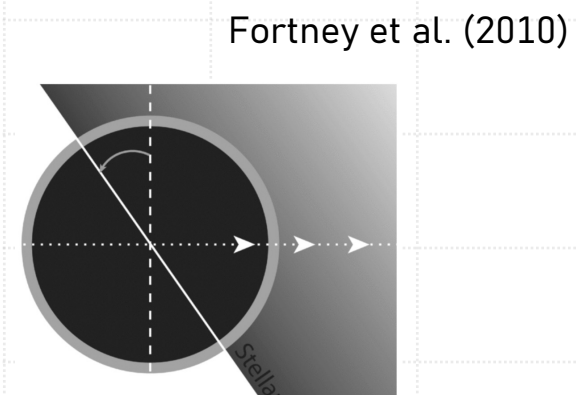
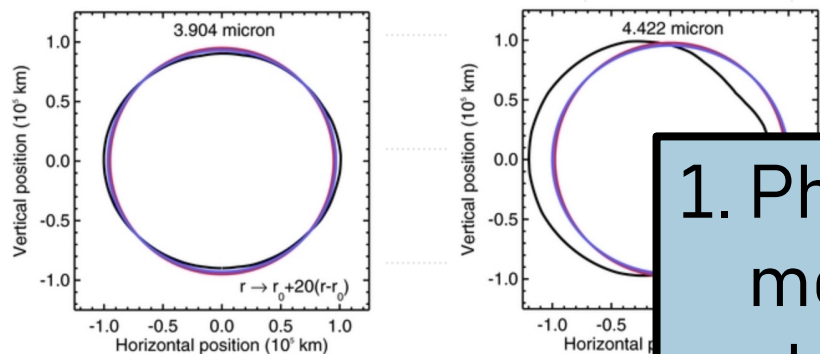
How spatial structure shows up in transit



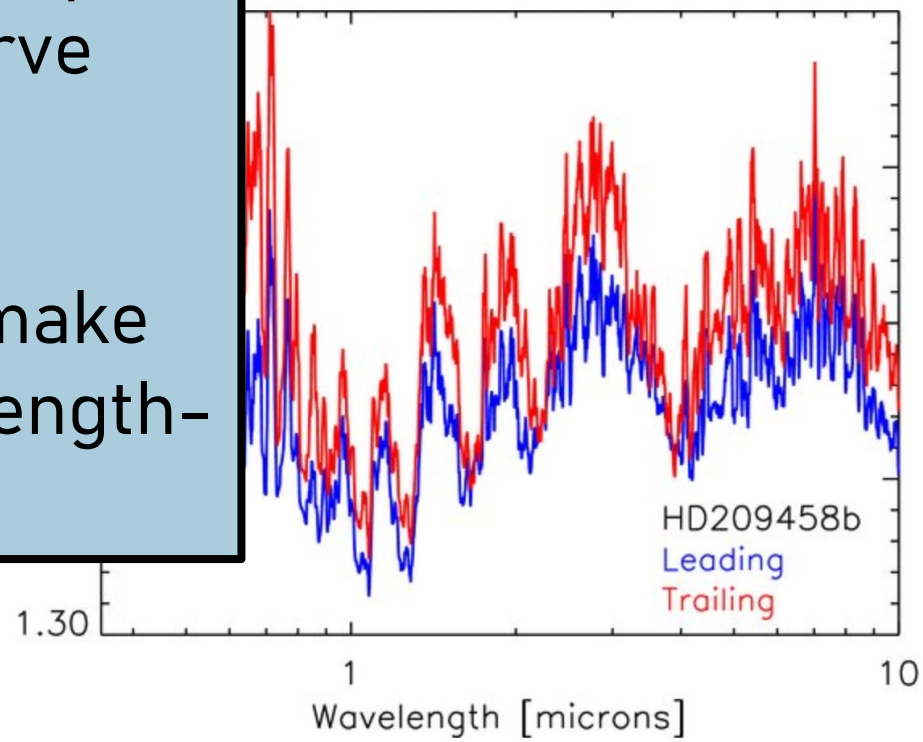
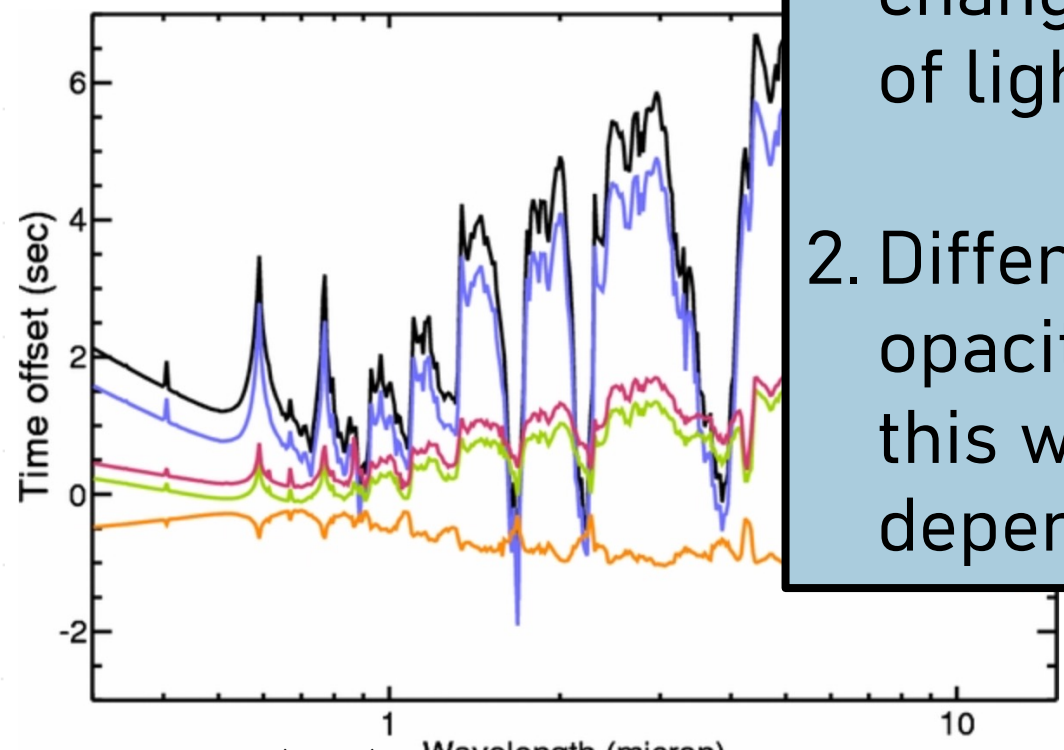
How spatial structure shows up in transit



How spatial structure shows up in transit



1. Physical morphology changes shape of light curve
2. Differing opacities make this wavelength-dependent



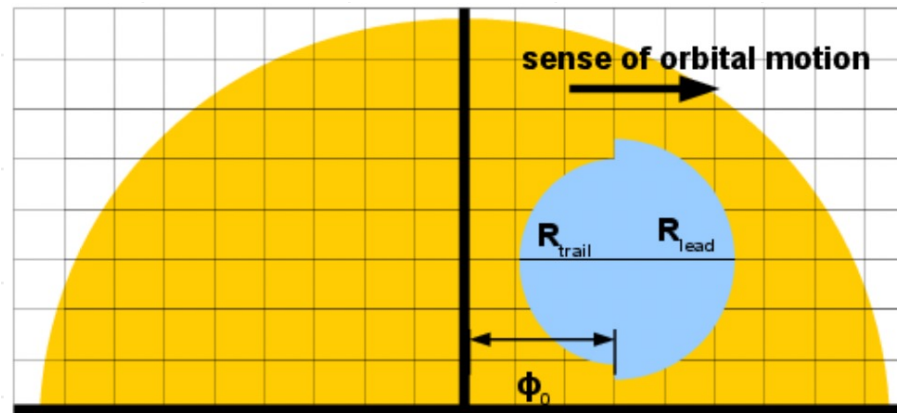
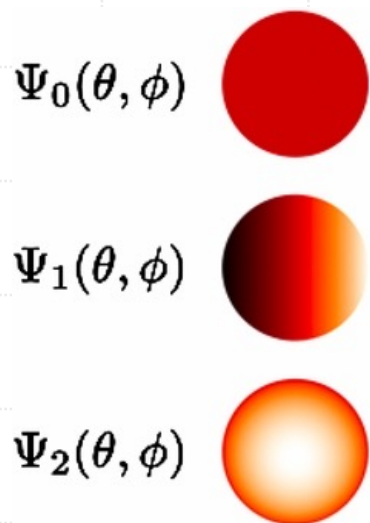
Dobbs-Dixon et al. (2012)

HD209458b

Leading
Trailing

How do we measure 3D structure in transit?

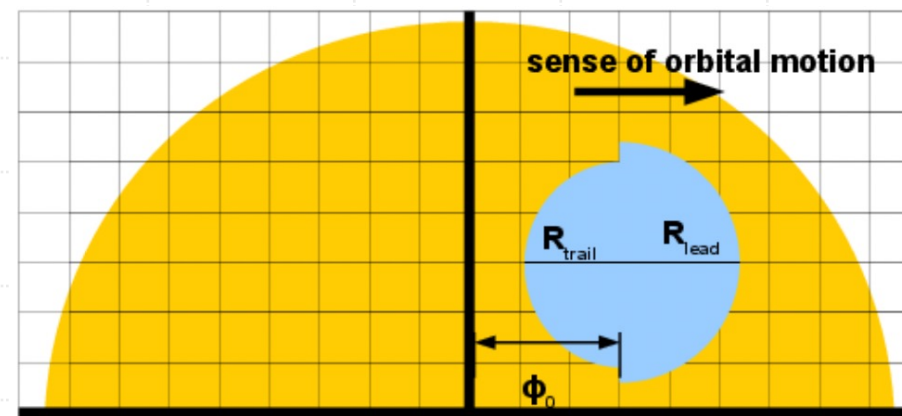
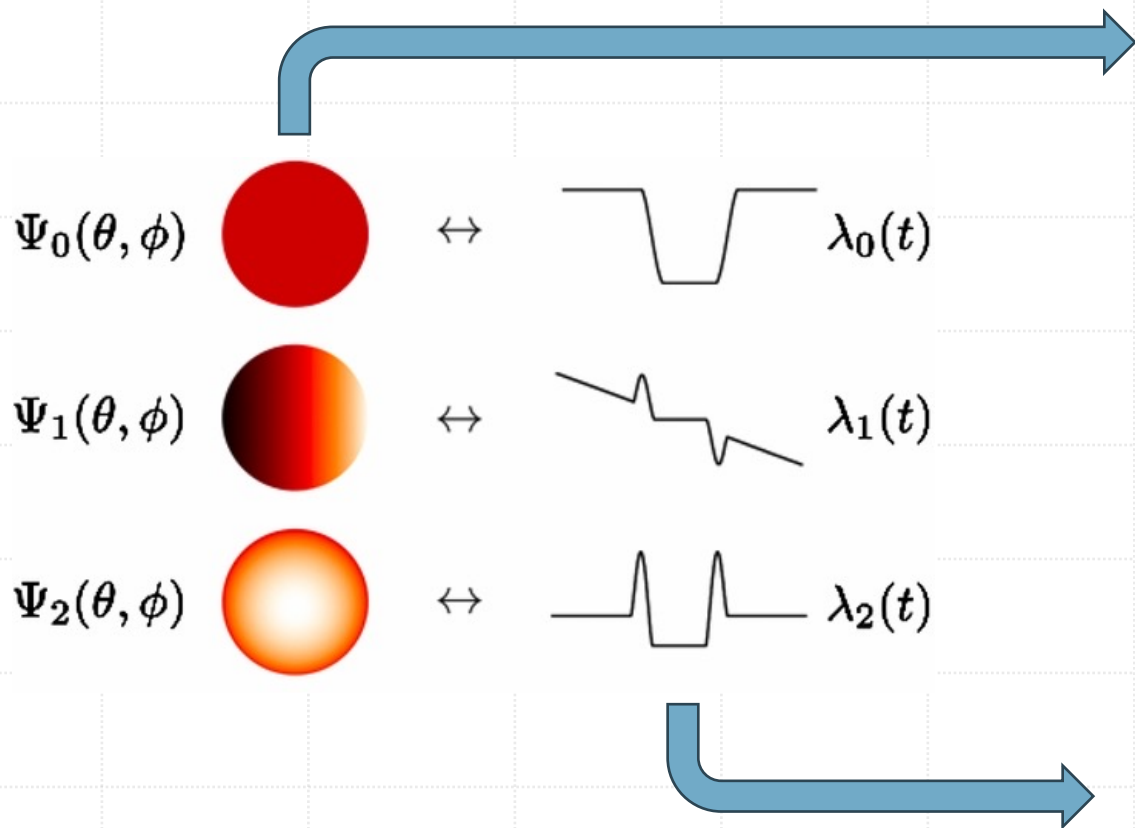
Instead of brightness variations,
there are effective radius variations



von Paris et al. (2016)

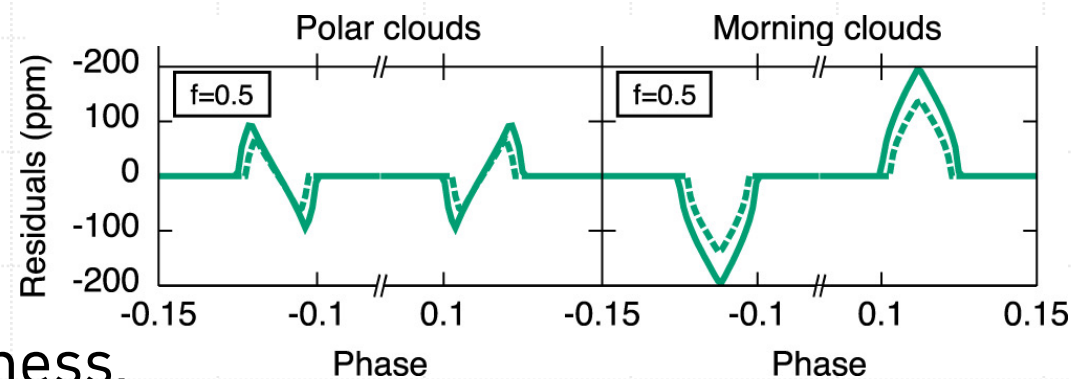
How do we measure 3D structure in transit?

Instead of brightness variations,
there are effective radius variations



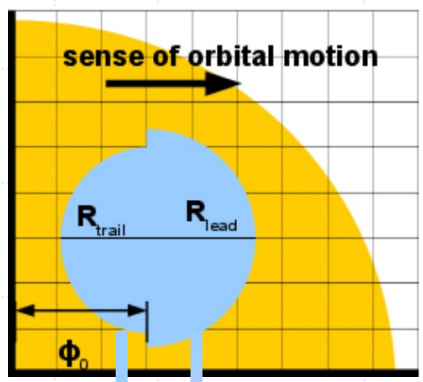
von Paris et al. (2016)

Instead of deviations from uniform brightness,
there are deviations from uniform radius

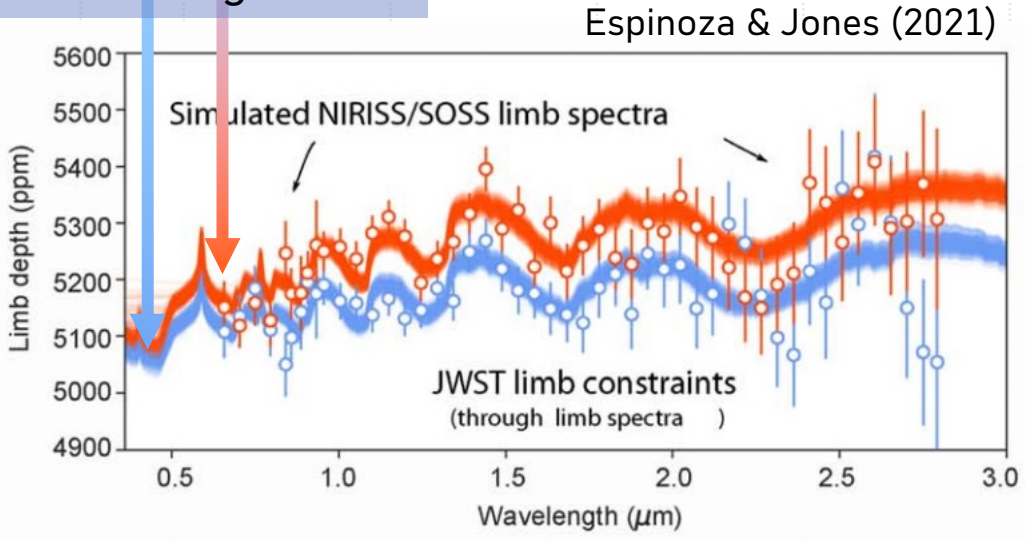


Line & Parmentier (2016)

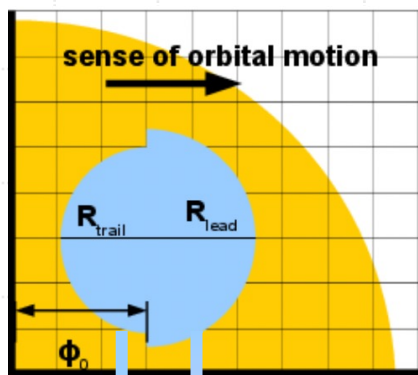
3D Transit Mapping Methods: Model-independent



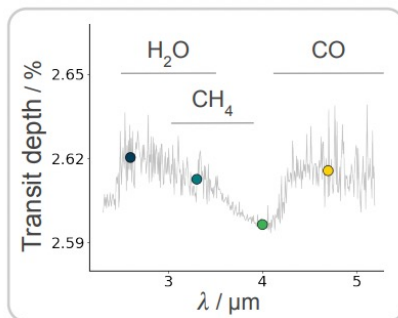
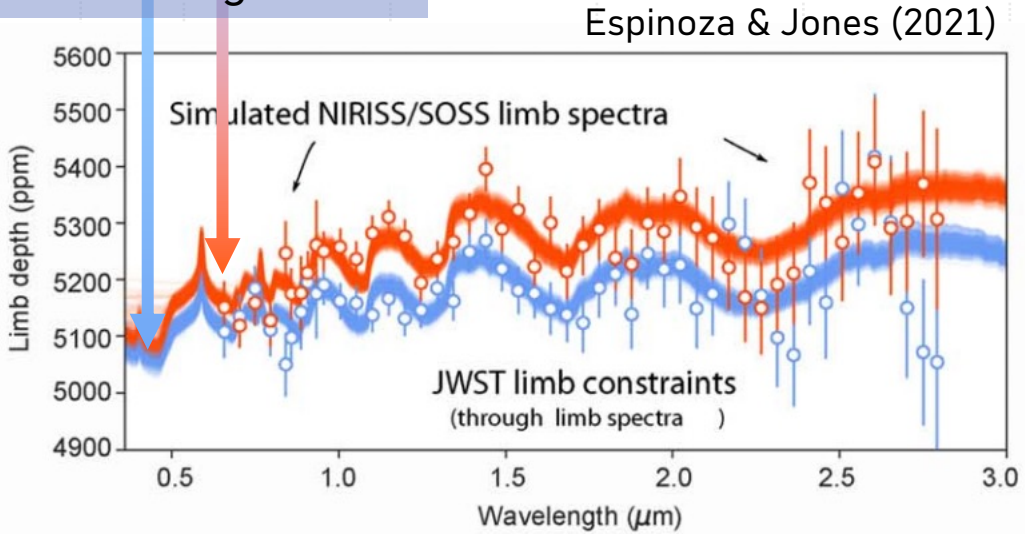
Fit $R_p(\lambda)$ for leading and trailing limbs



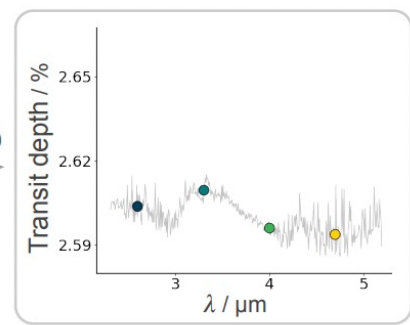
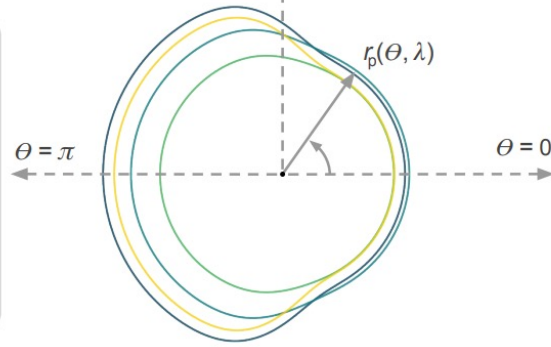
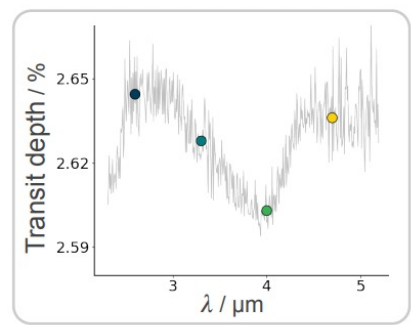
3D Transit Mapping Methods: Model-independent



Fit $R_p(\lambda)$ for leading and trailing limbs



Fit $R_p(\theta, \lambda)$ with Fourier series
Get atmospheric profiles at all locations

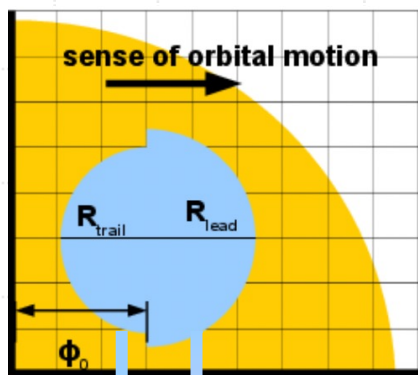


- $r_p(\theta, \lambda = 2.6 \mu\text{m})$
- $r_p(\theta, \lambda = 3.3 \mu\text{m})$
- $r_p(\theta, \lambda = 4.0 \mu\text{m})$
- $r_p(\theta, \lambda = 4.7 \mu\text{m})$

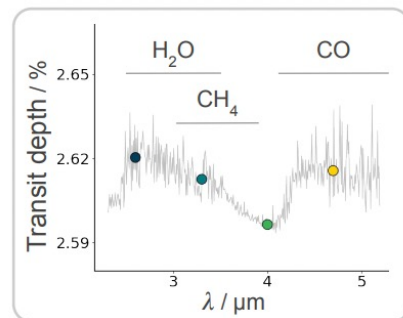
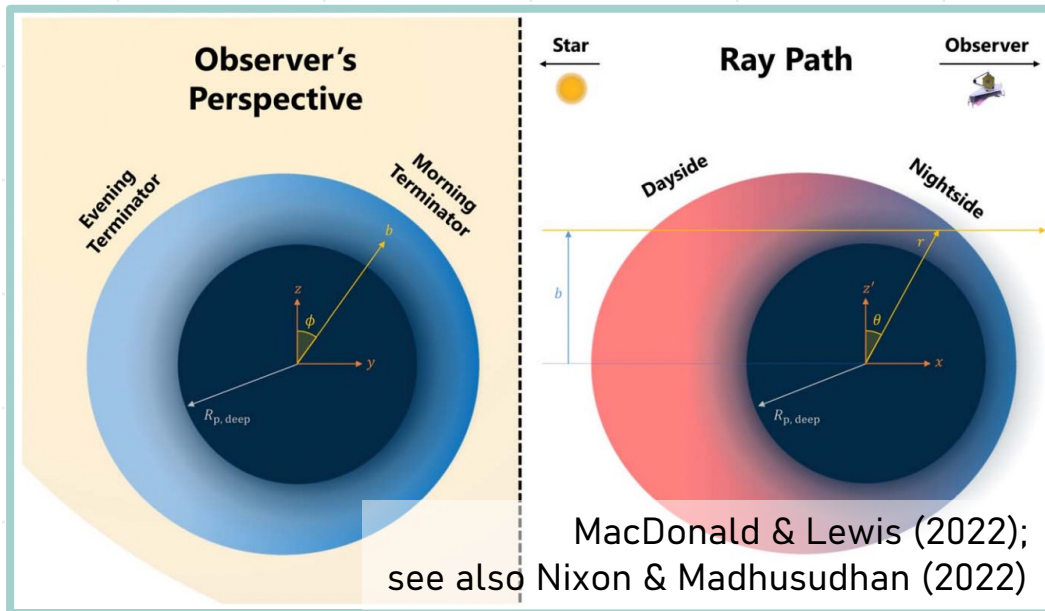
3D Transit Mapping Methods:

Model-independent Parameterized structure

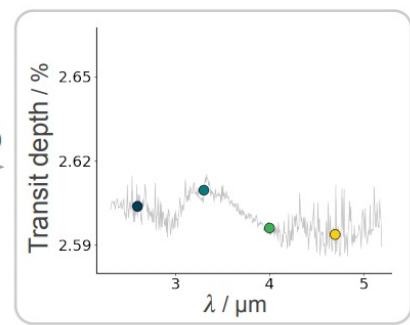
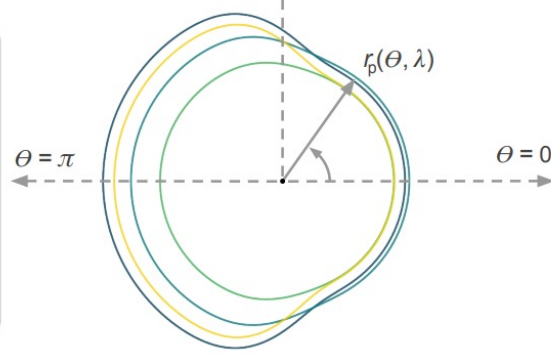
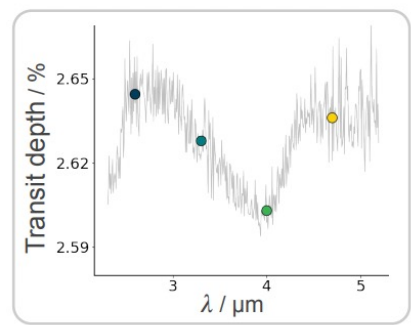
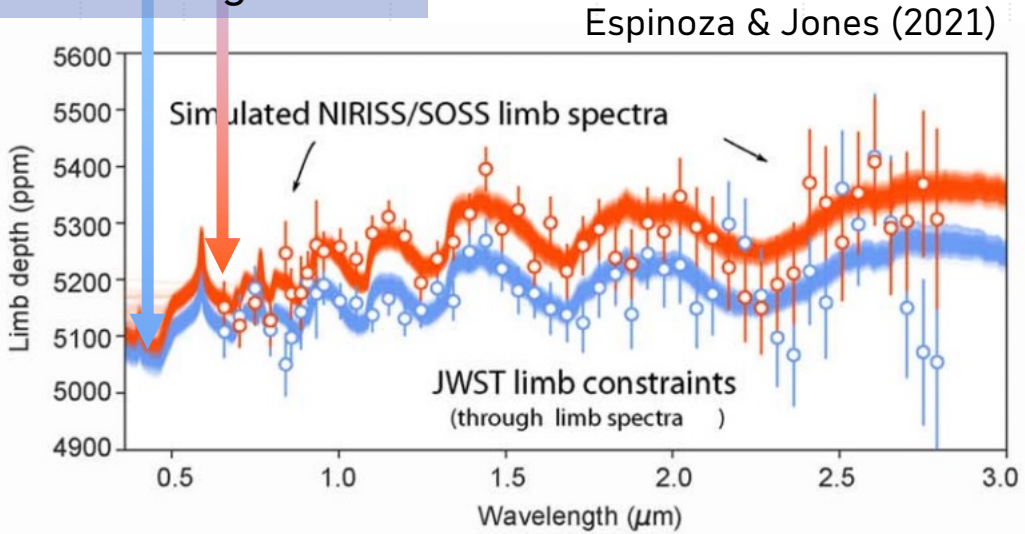
Parameterize 3D atmospheric structure and run retrieval on spectral light curves



Fit $R_p(\lambda)$ for leading and trailing limbs



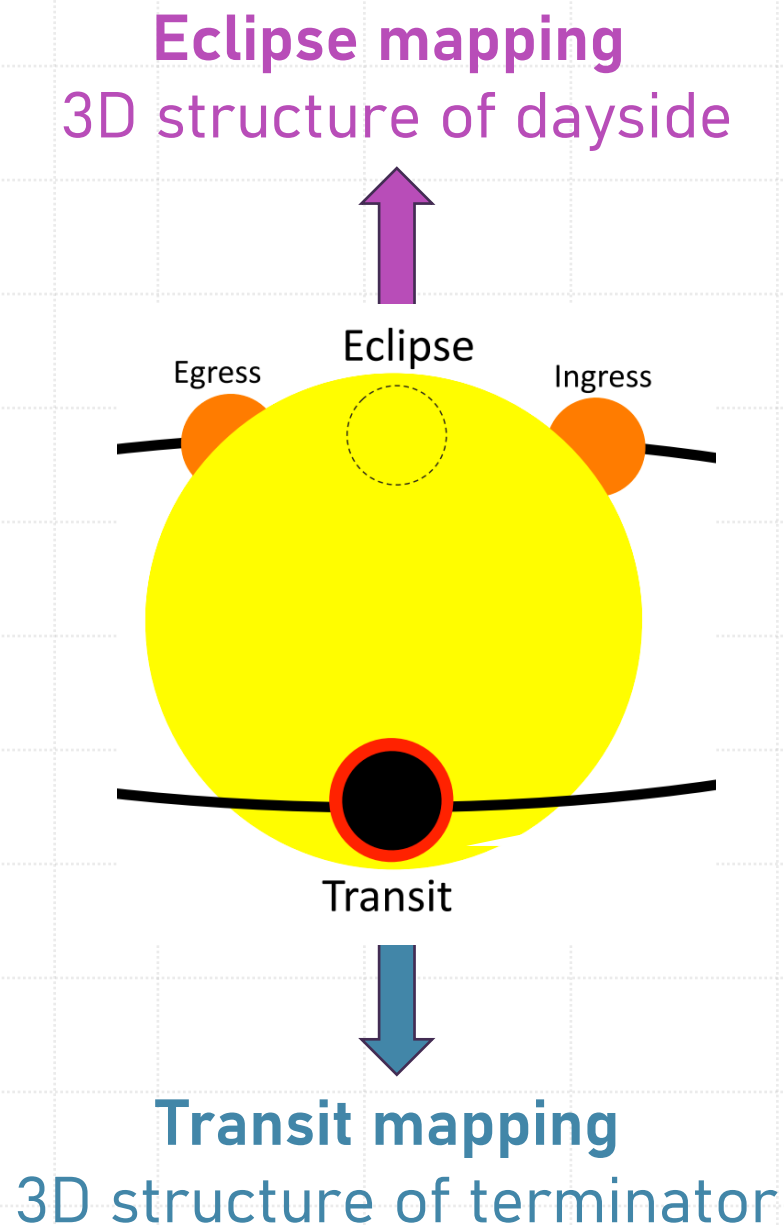
Fit $R_p(\theta, \lambda)$ with Fourier series
Get atmospheric profiles at all locations



- $r_p(\theta, \lambda = 2.6 \mu\text{m})$
- $r_p(\theta, \lambda = 3.3 \mu\text{m})$
- $r_p(\theta, \lambda = 4.0 \mu\text{m})$
- $r_p(\theta, \lambda = 4.7 \mu\text{m})$

Grant & Wakeford (2022)

Mapping the 3D Structure of Exoplanet Atmospheres



- How to access 3D info:
 - Latitude and longitude come from the shape of the light curve
 - Depth into the atmosphere comes from spectral differences
- Methods to extract 3D info:
 - Model-independent
 - Model-informed

With JWST we can measure atmospheres in 3D!

