

# Transmission Spectroscopy

Hannah Wakeford  
(She/her)

Associate Professor in Astrophysics  
University of Bristol



UK Research  
and Innovation

Horizon Europe Funding

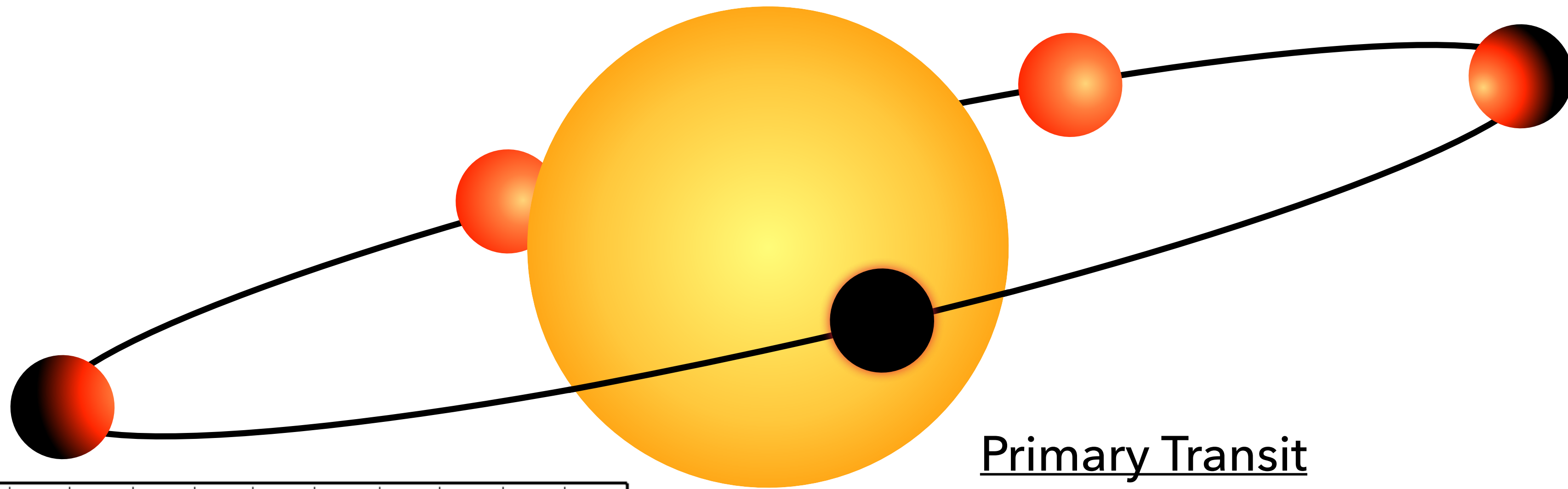


Image compilation: HRWakeford



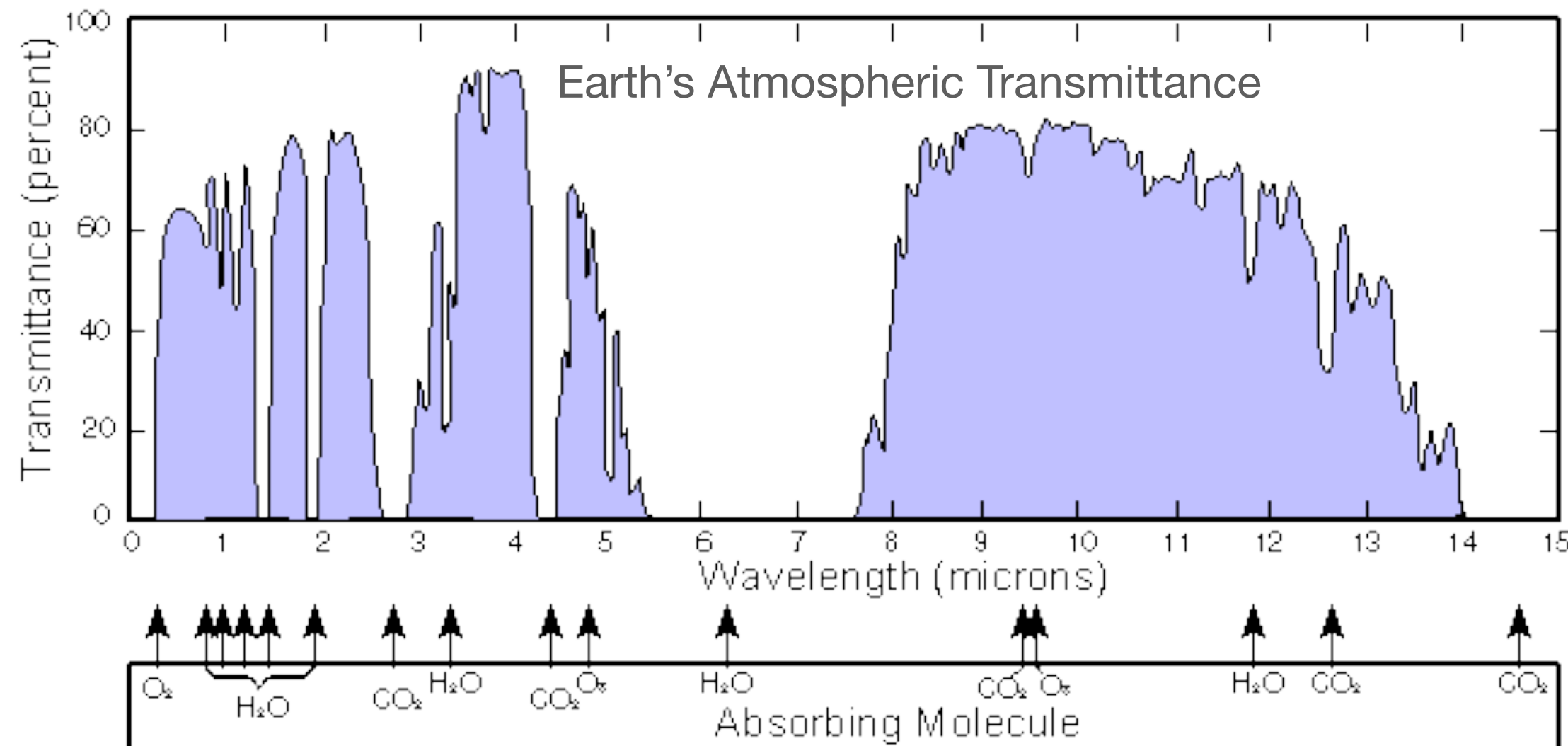
# Transmission Spectroscopy

Measure of atmospheric absorption and transmission during transit



## Primary Transit

The planet passes in front of the star  
Absorption (transmission) through the planets atmosphere can be measured by the change in area blocked



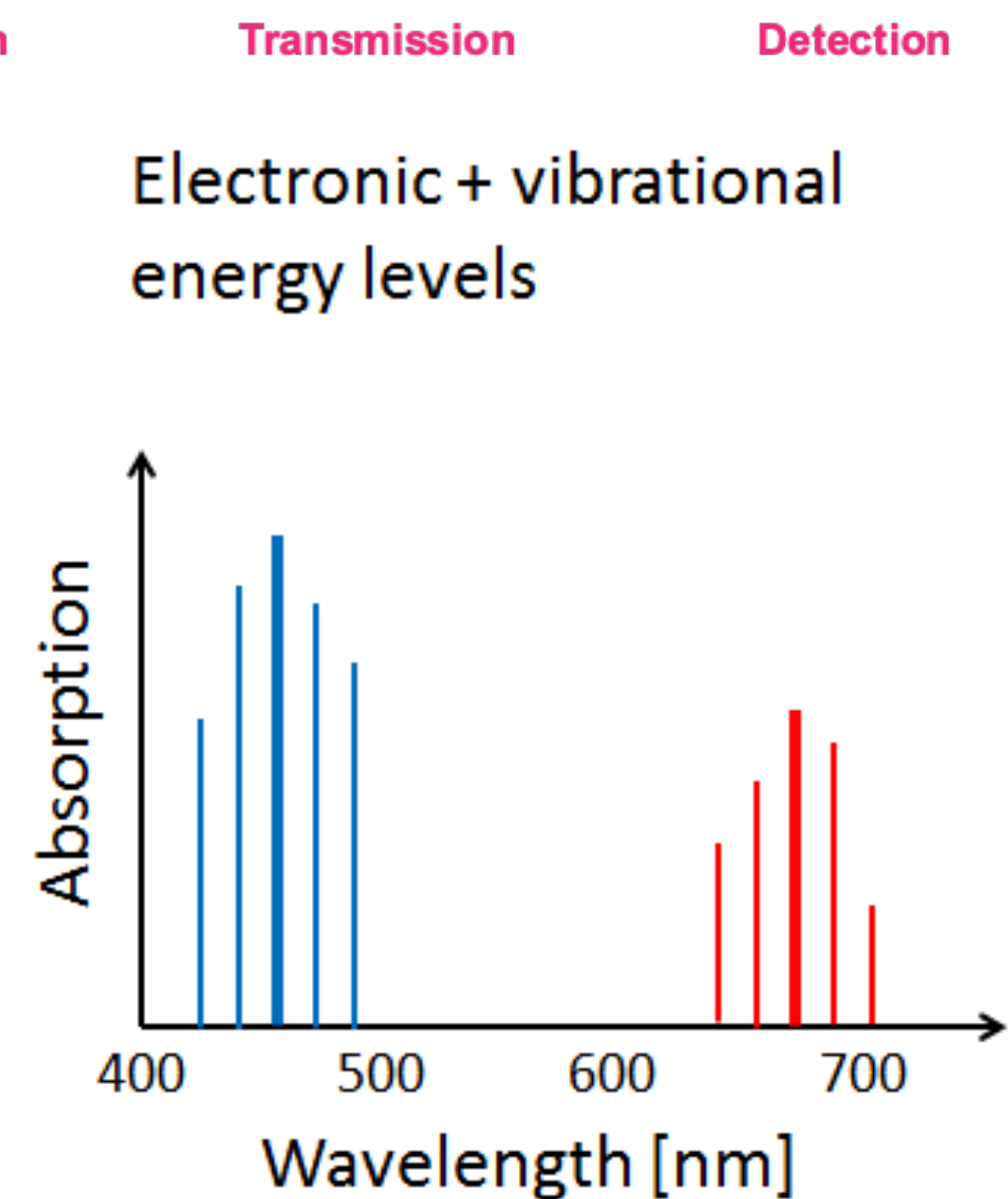
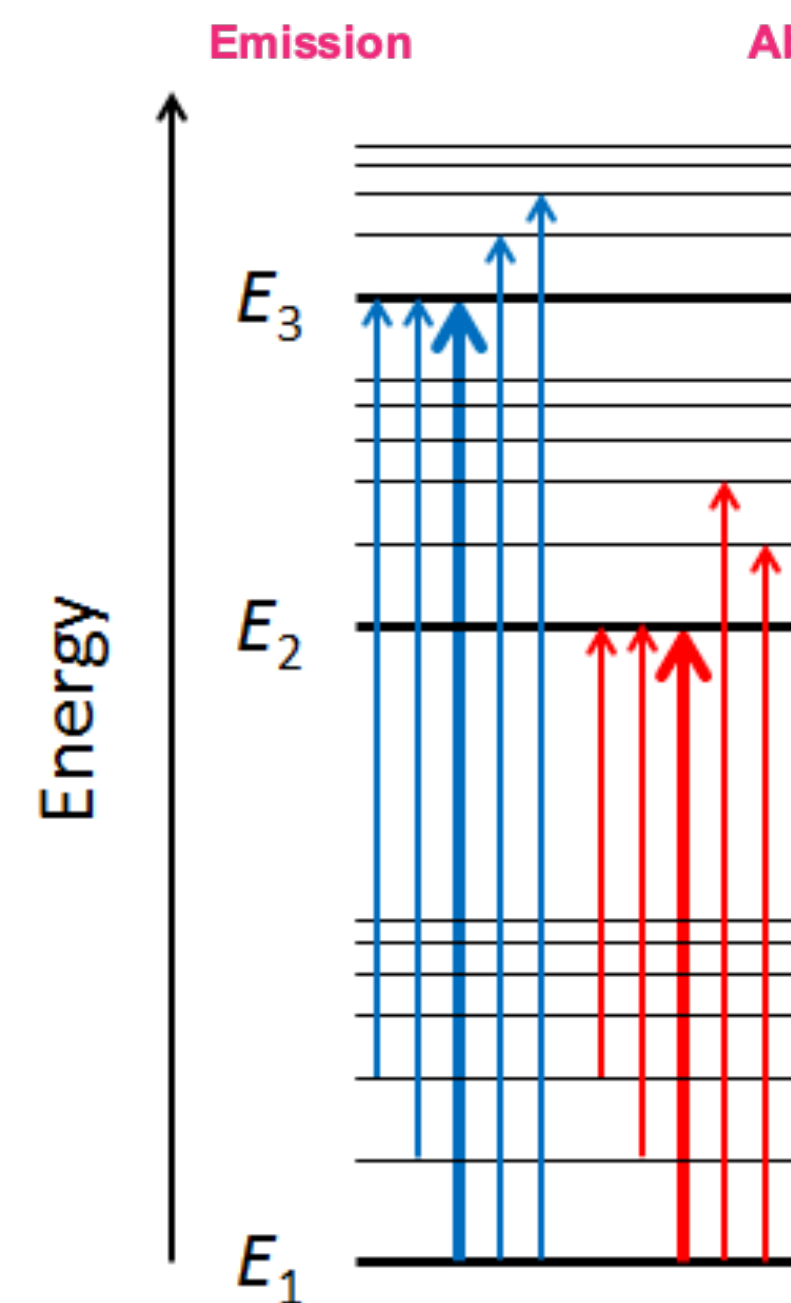
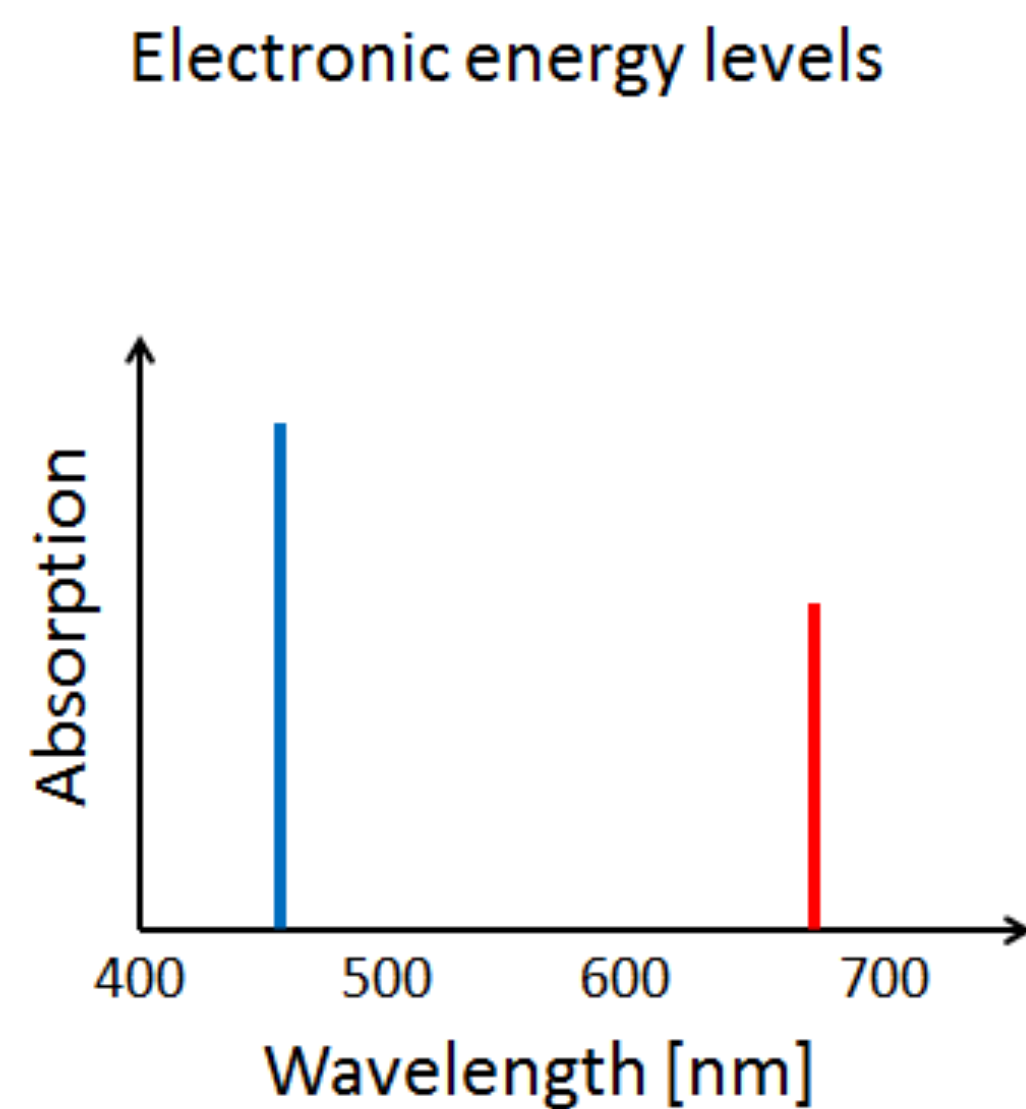
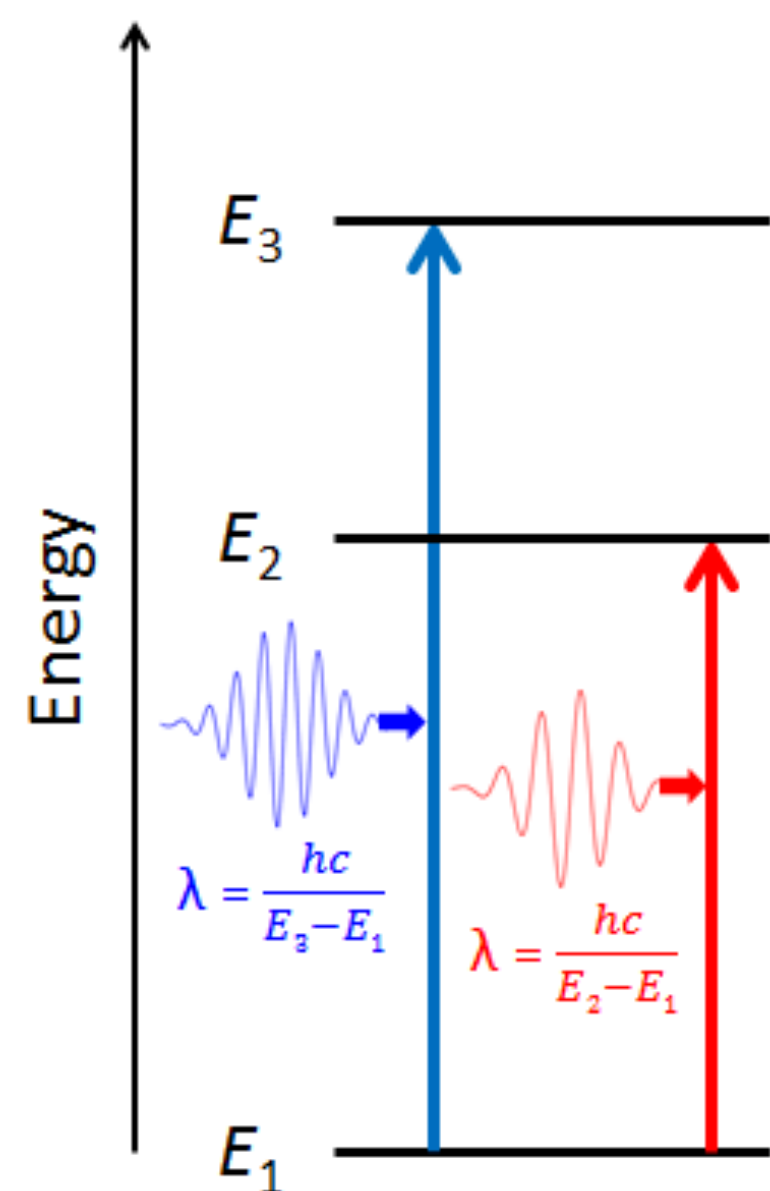
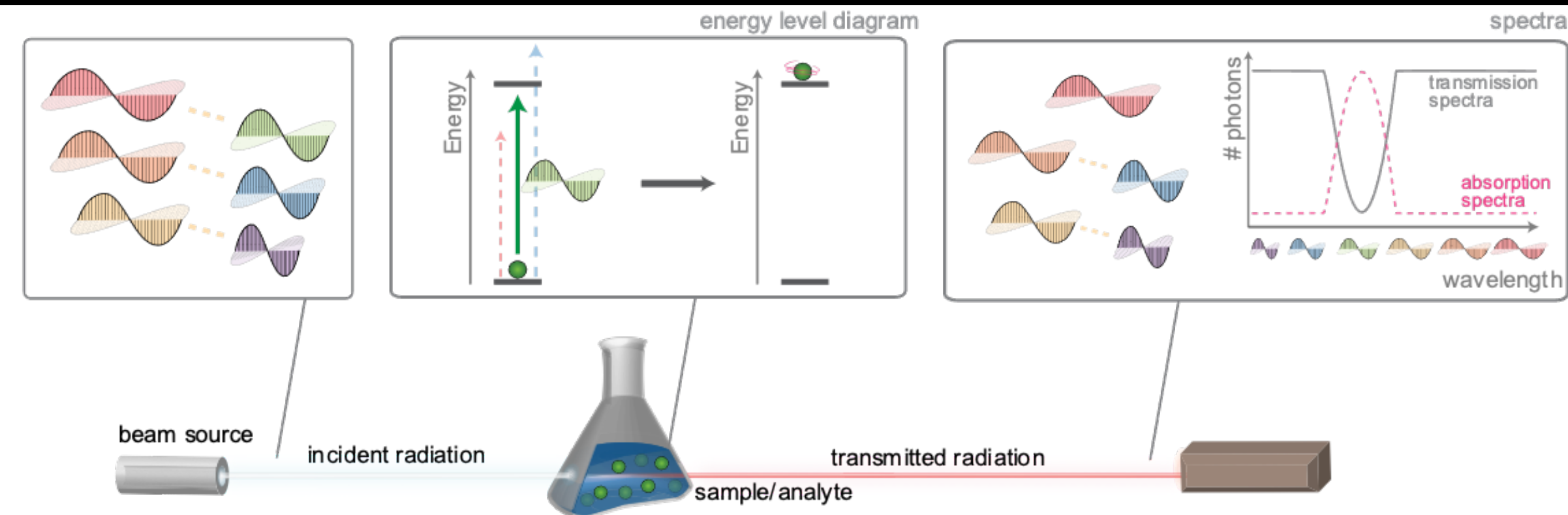


# Absorption and Energy Levels



The process where photons are transformed into internal energy

On a quantum mechanical level, a molecule can only absorb or emit energy of wavelength  $\lambda$  if it has energy levels separated by a transition energy





# Photon Energies Tell You About Absorption Properties



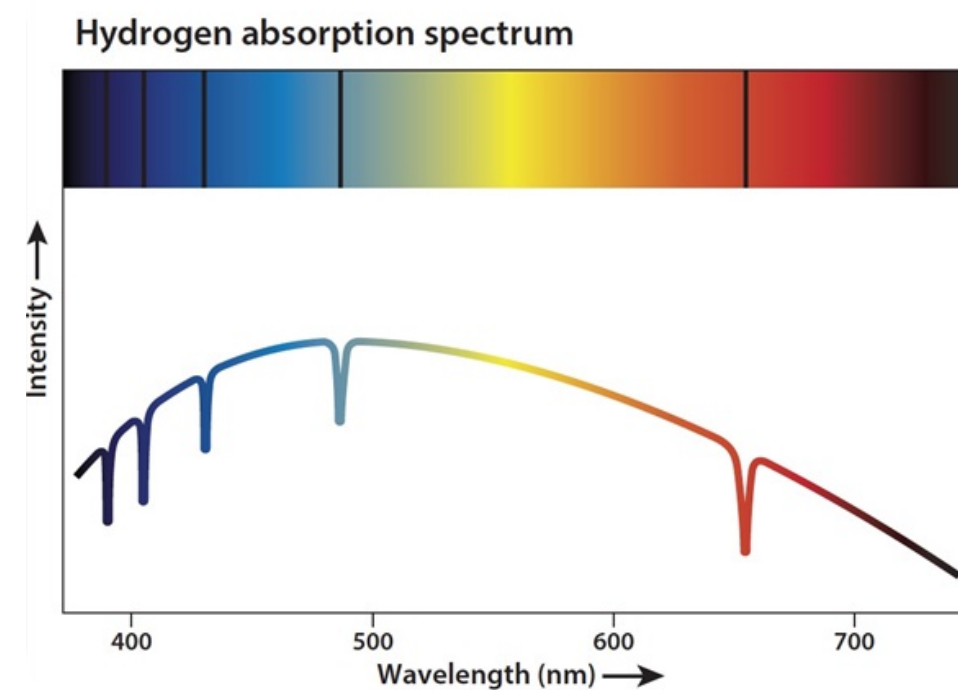
Different energy scales in atoms and molecules correspond to different processes

Electron motion:

$$\Delta E \sim 1000 \text{ eV} - 1 \text{ eV}$$

$$\lambda \sim 1 \text{ nm} - 1 \mu\text{m}$$

UV - Optical

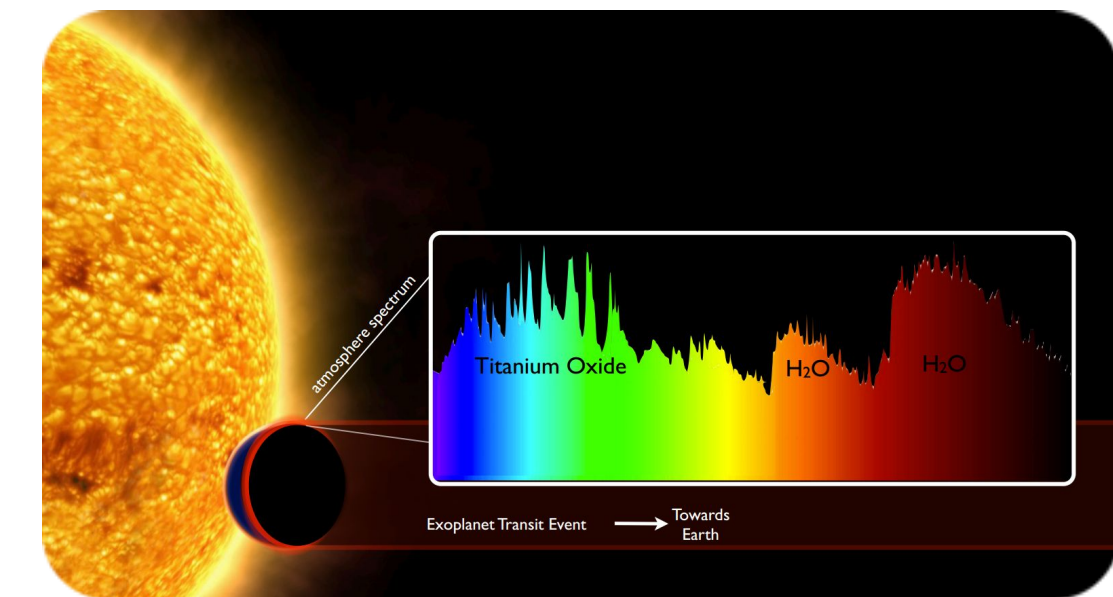


Ro-vibrational overtones:

$$\Delta E \sim 1 \text{ eV} - 100 \text{ meV}$$

$$\lambda \sim 1 \mu\text{m} - 10 \mu\text{m}$$

Near- to Mid-IR

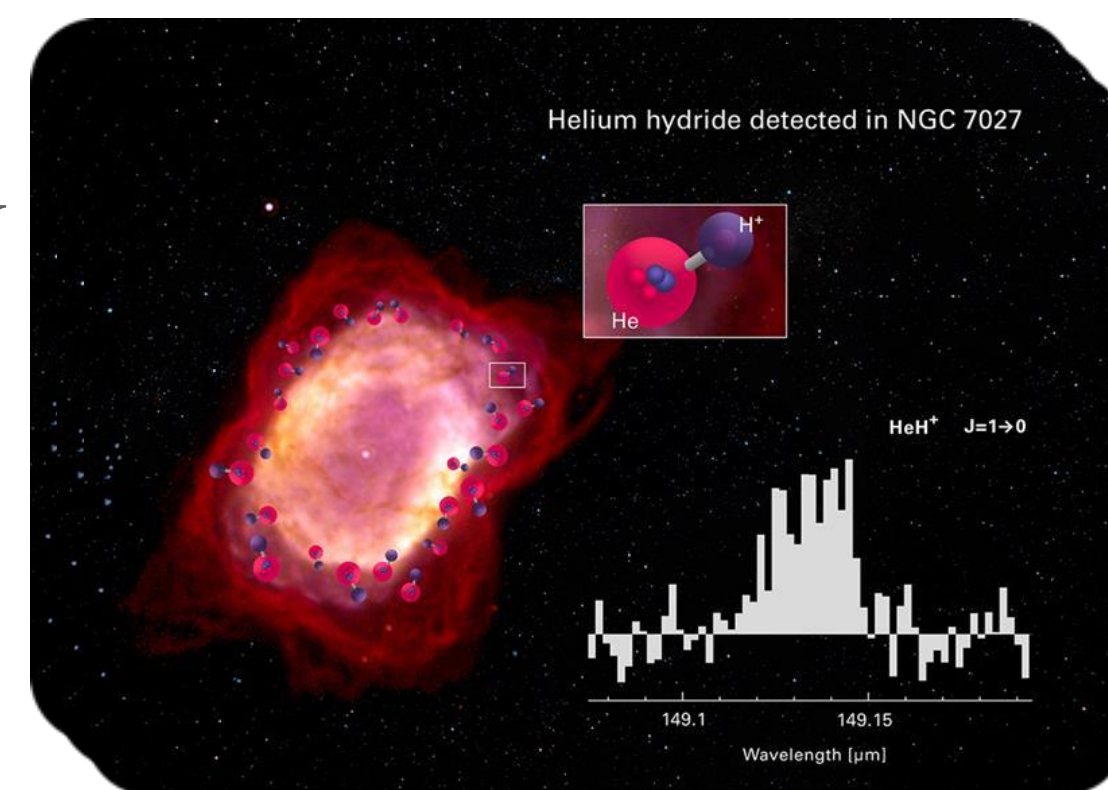


Molecular Vibration:

$$\Delta E \sim 100 \text{ meV} - 0.1 \text{ meV}$$

$$\lambda \sim 10 \mu\text{m} - 1 \text{ cm}$$

IR - sub-mm & radio

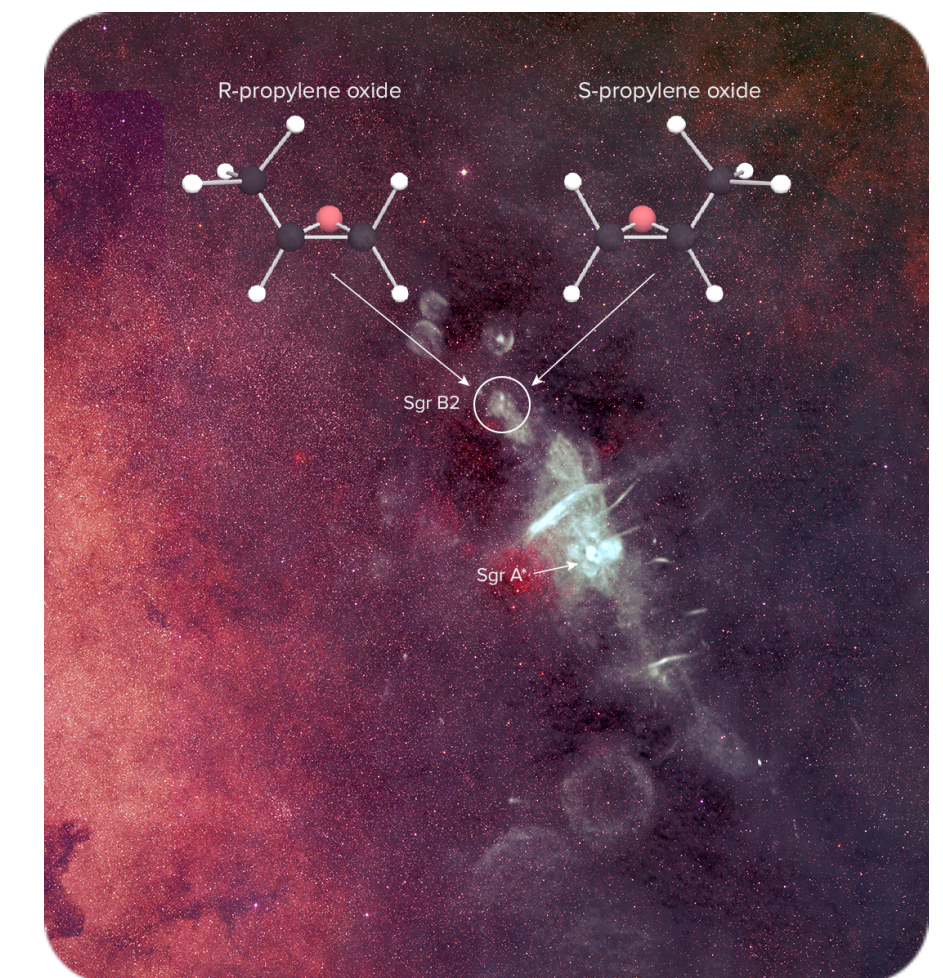


Molecular Rotation:

$$\Delta E \sim 0.01 \text{ meV}$$

$$\lambda \sim 10 \text{ cm}$$

Radio

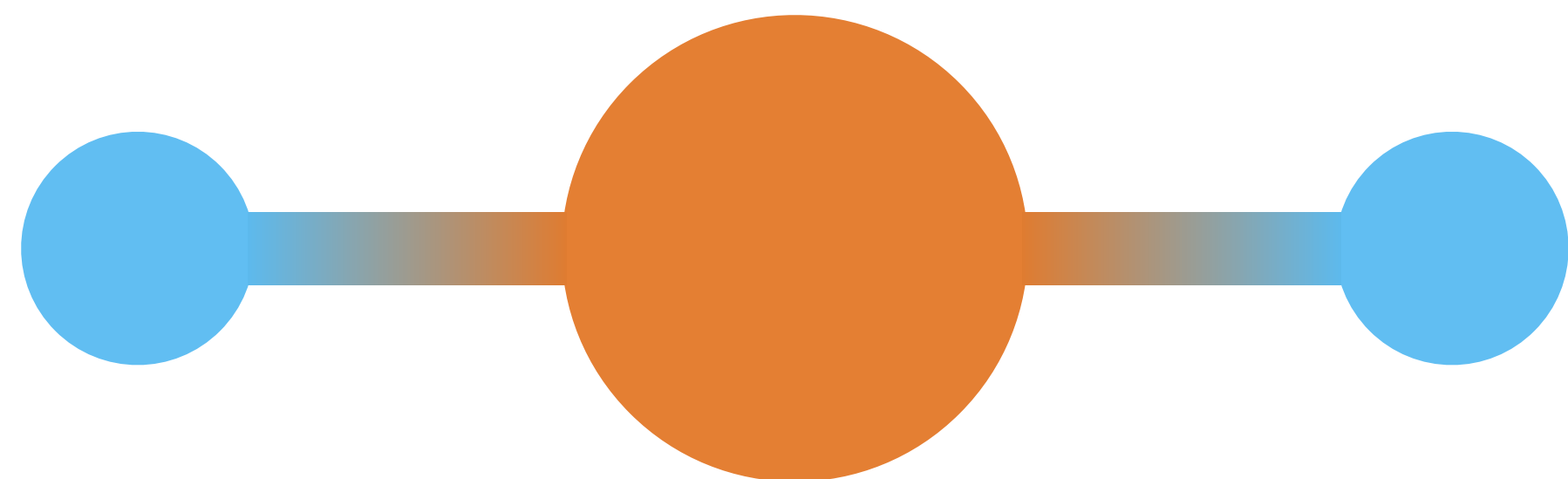




# Infrared Absorption



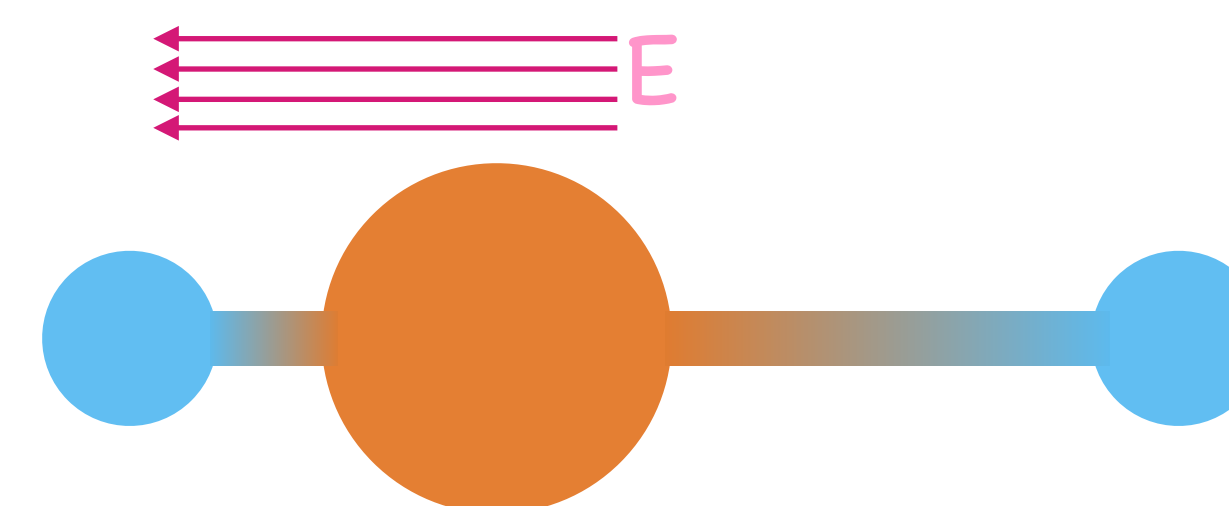
A vibrational mode can only be induced if the molecule has an electric dipole



Electric dipole = structural separation of +ve and -ve charges

Molecules with a pronounced dipole moment will absorb in the infrared

- \* The wavelength of infrared radiation has a wavelength larger than a typical molecule
- \* As far as the molecule is concerned, the electric field of the IR radiation represents a uniform external field.
- \* Within this field all positive charges are pushed in one direction and all the negative charges are pushed in the opposite direction.
- \* This motion produces a fluctuation on the dipole moment which is how the IR radiation induces a vibration.





# Absorption in the Earth's Atmosphere



The size of the atmosphere looks different at different wavelengths



*Credit: Himawary/Simon Proud/Vivien Parmentier*

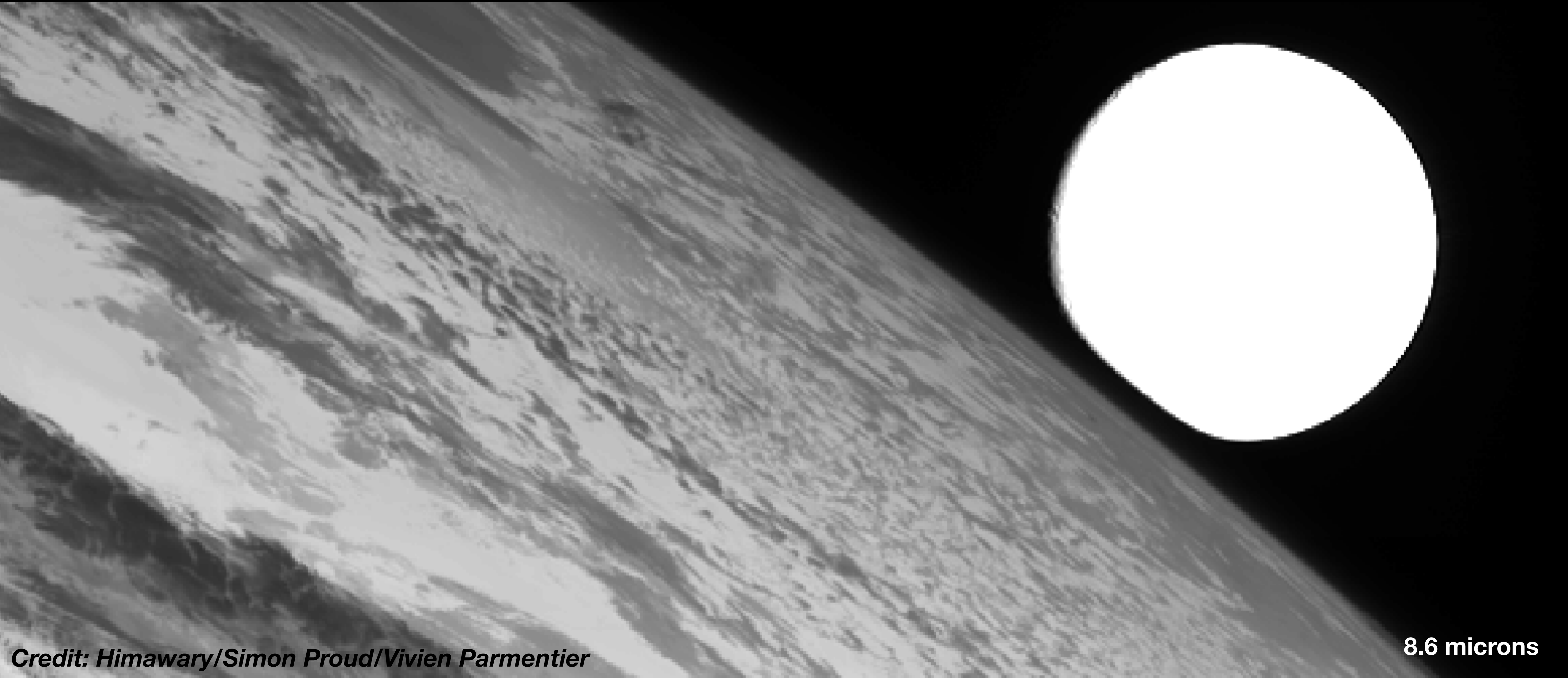
Real color



# Absorption in the Earth's Atmosphere



The size of the atmosphere looks different at different wavelengths



8.6 microns

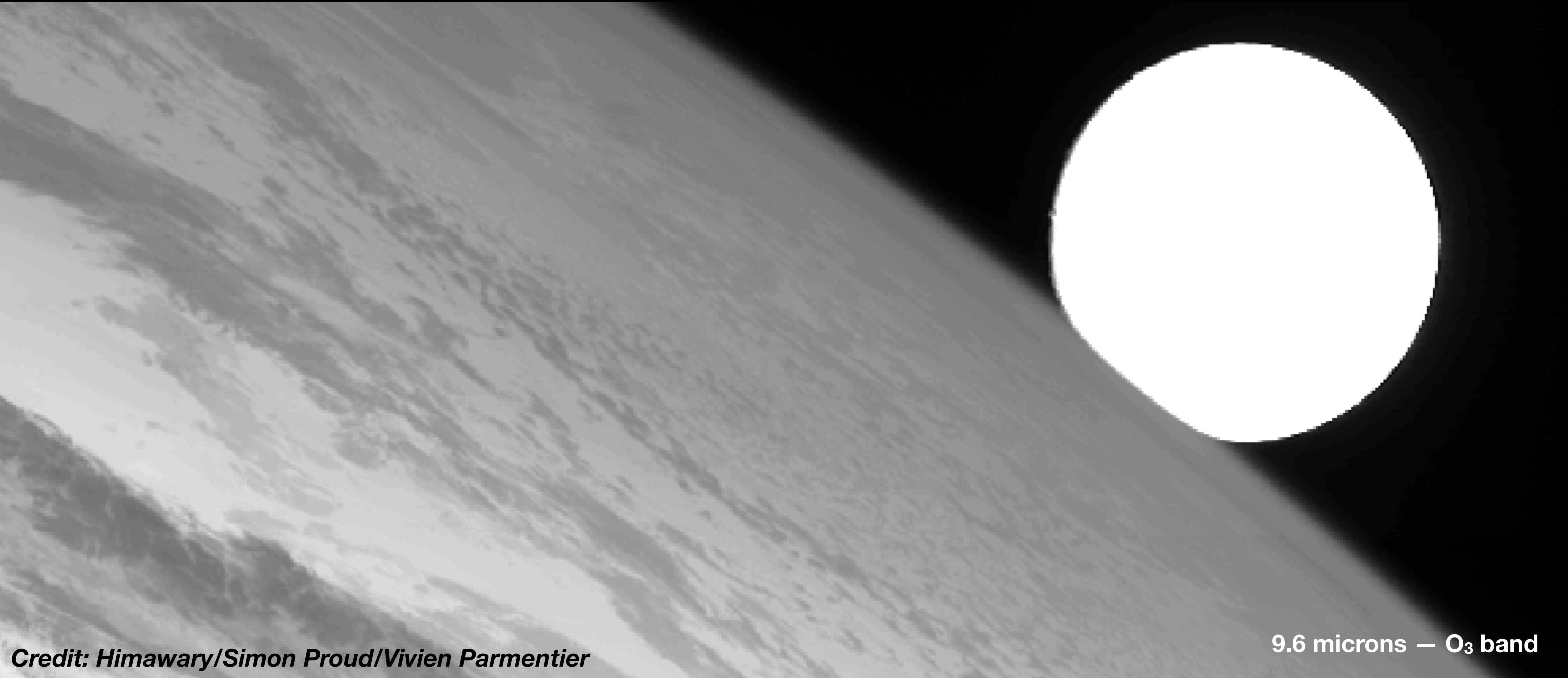
*Credit: Himawary/Simon Proud/Vivien Parmentier*



# Absorption in the Earth's Atmosphere



The size of the atmosphere looks different at different wavelengths



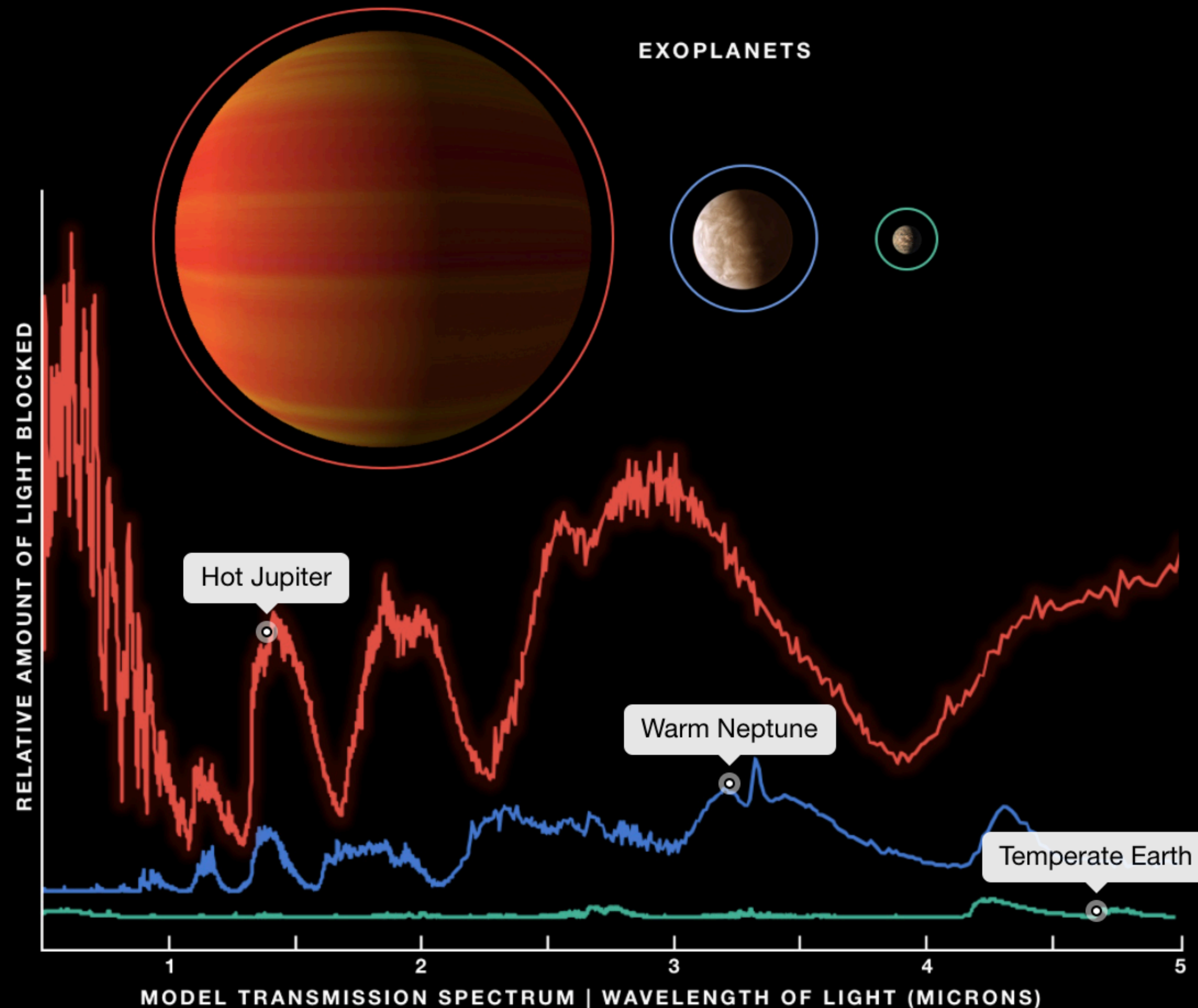
9.6 microns — O<sub>3</sub> band

*Credit: Himawary/Simon Proud/Vivien Parmentier*



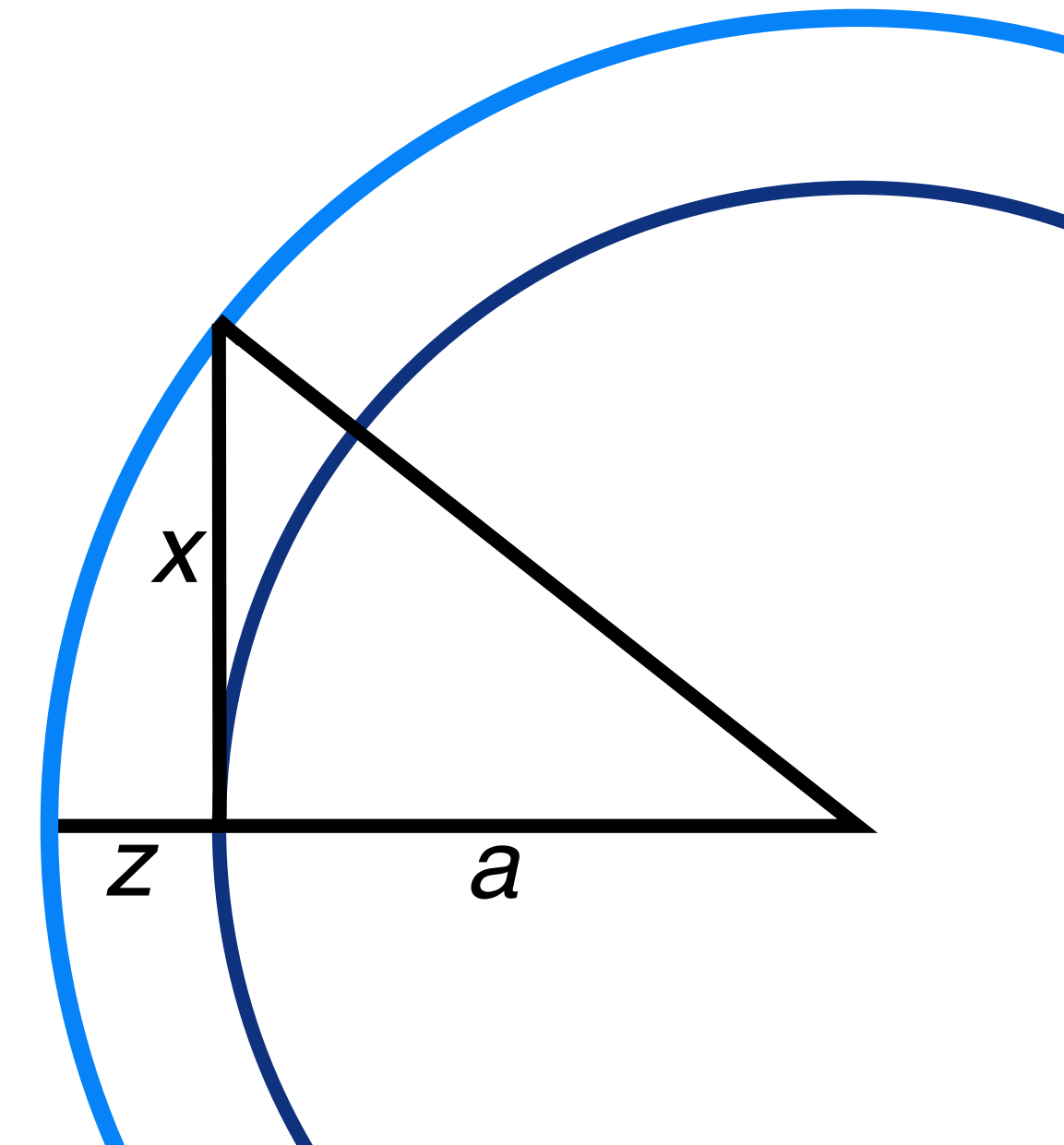
# Predicting the Size of Atmospheric Features

The more atmosphere, the more signal transmitted



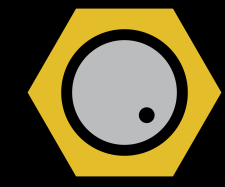
- The larger the atmosphere the easier the measurement will be.
- The larger the cross section of the molecule the larger the impact on the spectrum for small amounts

The slant geometry measured in transit often increases absorption significance by over 30x

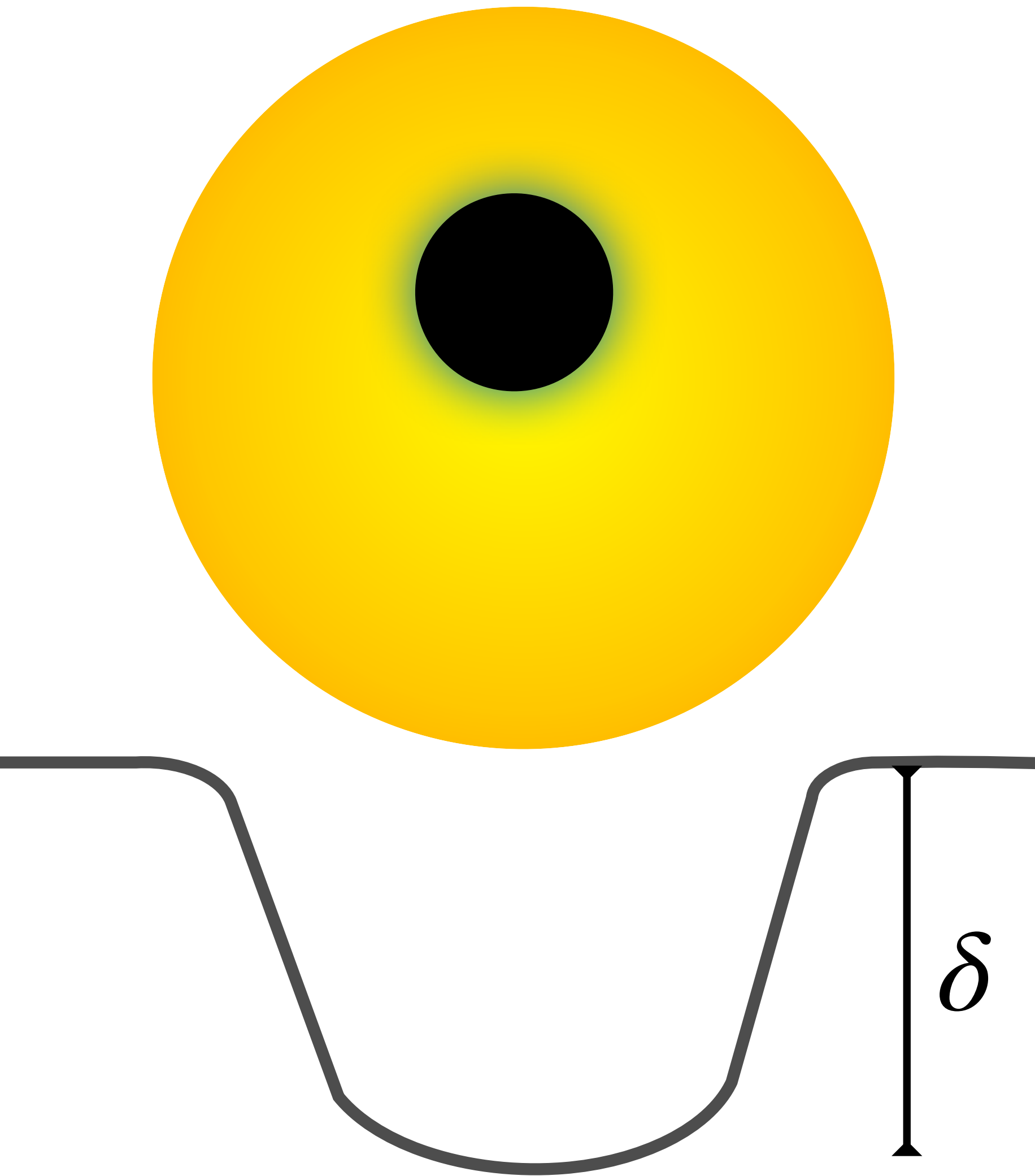




# Measured Transit Depth



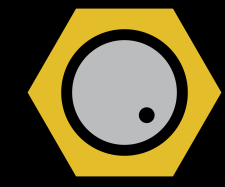
The atmosphere adds a more area blocked by the planet



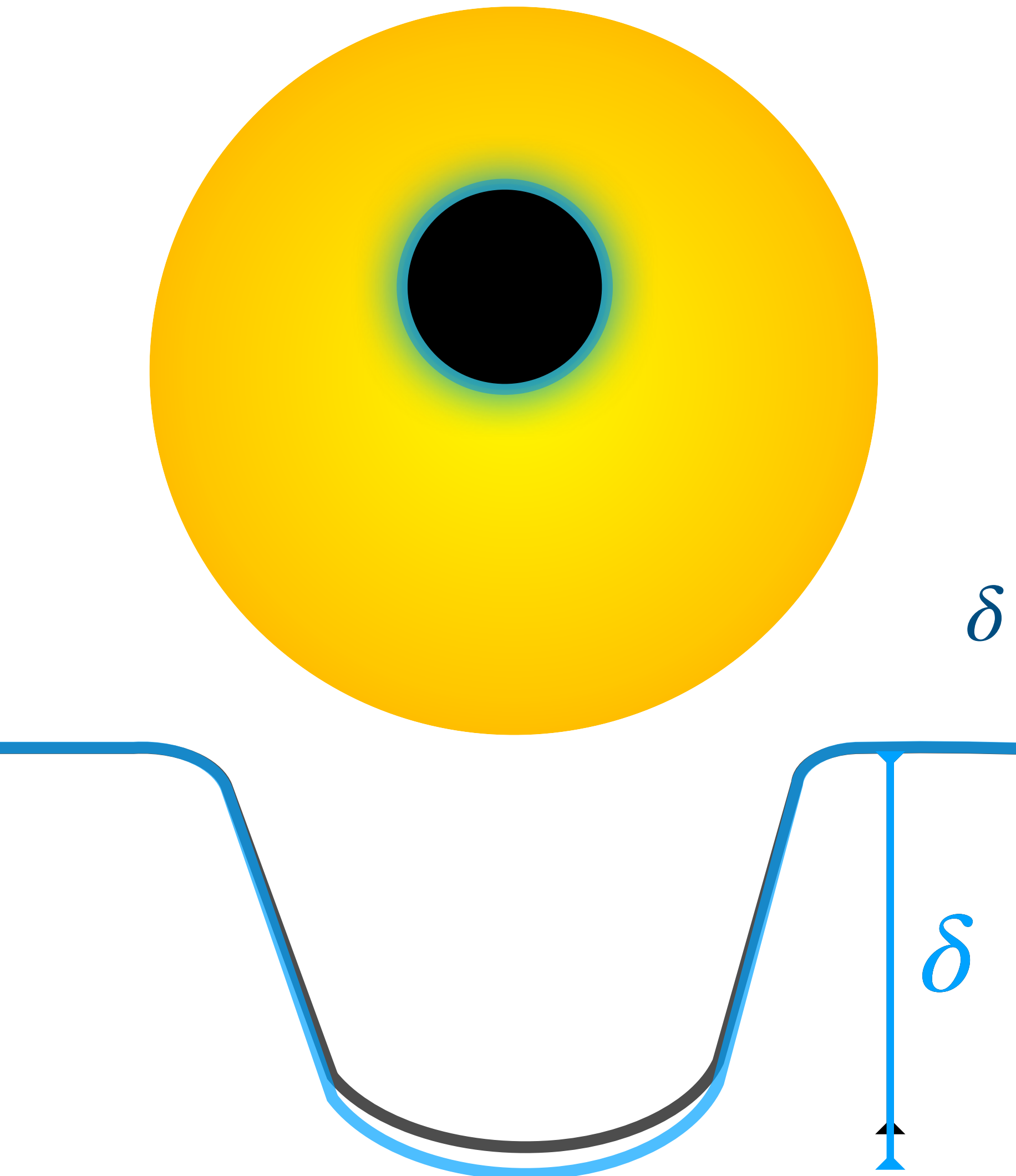
$$\delta = \frac{A_p}{A_*} = \frac{\pi R_p^2}{\pi R_*^2} = \left( \frac{R_p}{R_*} \right)^2$$



# Measured Transit Depth



The atmosphere adds a more area blocked by the planet



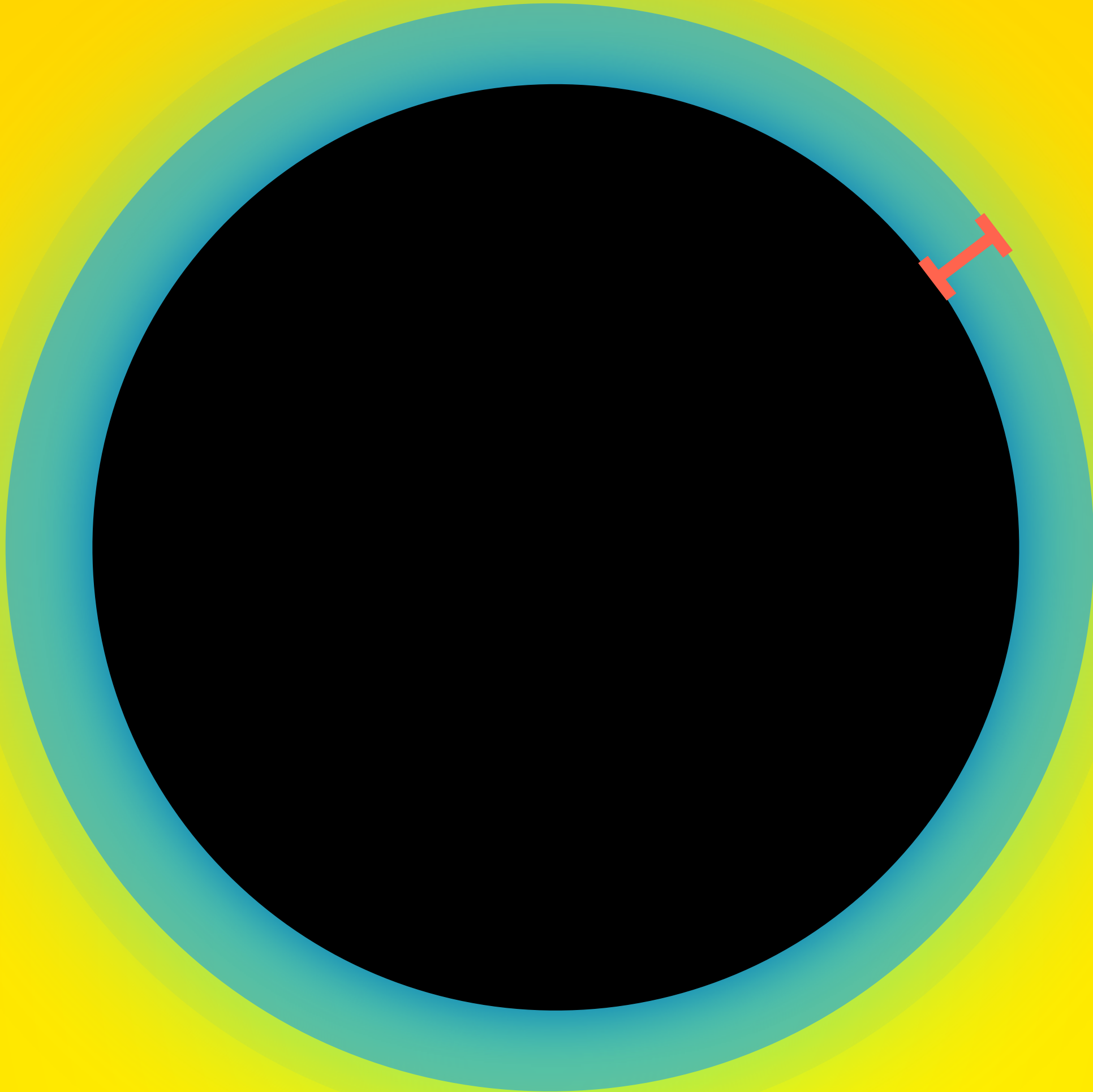
$$\delta = \frac{A_p}{A_*} = \frac{\pi R_p^2}{\pi R_*^2} = \left( \frac{R_p}{R_*} \right)^2$$

$$\delta = \frac{A_p + A_{atm}}{A_*} = \frac{\pi (R_p + H_{atm})^2}{\pi R_*^2} \approx \left( \frac{R_p}{R_*} \right)^2 + \frac{2R_p H_{atm}}{R_*^2}$$



# Atmospheric Scale Height

Height at which pressure decreases by a factor of e (exponent)



The diagram shows a black circle representing a planet, surrounded by a thick, multi-layered atmosphere. The atmosphere is depicted with concentric rings of color, transitioning from dark blue at the surface to light blue, green, and yellow at the top. A red vertical line with horizontal end-caps is drawn on the right side of the planet, indicating the atmospheric scale height H, which is the vertical distance from the surface to the top of the atmosphere.

$$H = \frac{k_B T_{eq}}{\mu g_p}$$

H = Atmospheric Scale Height

$k_B$  = Boltzmann Constant

T = Planetary Temperature

$\mu$  = Atmospheric Mean Molecular Weight

g = planet gravity

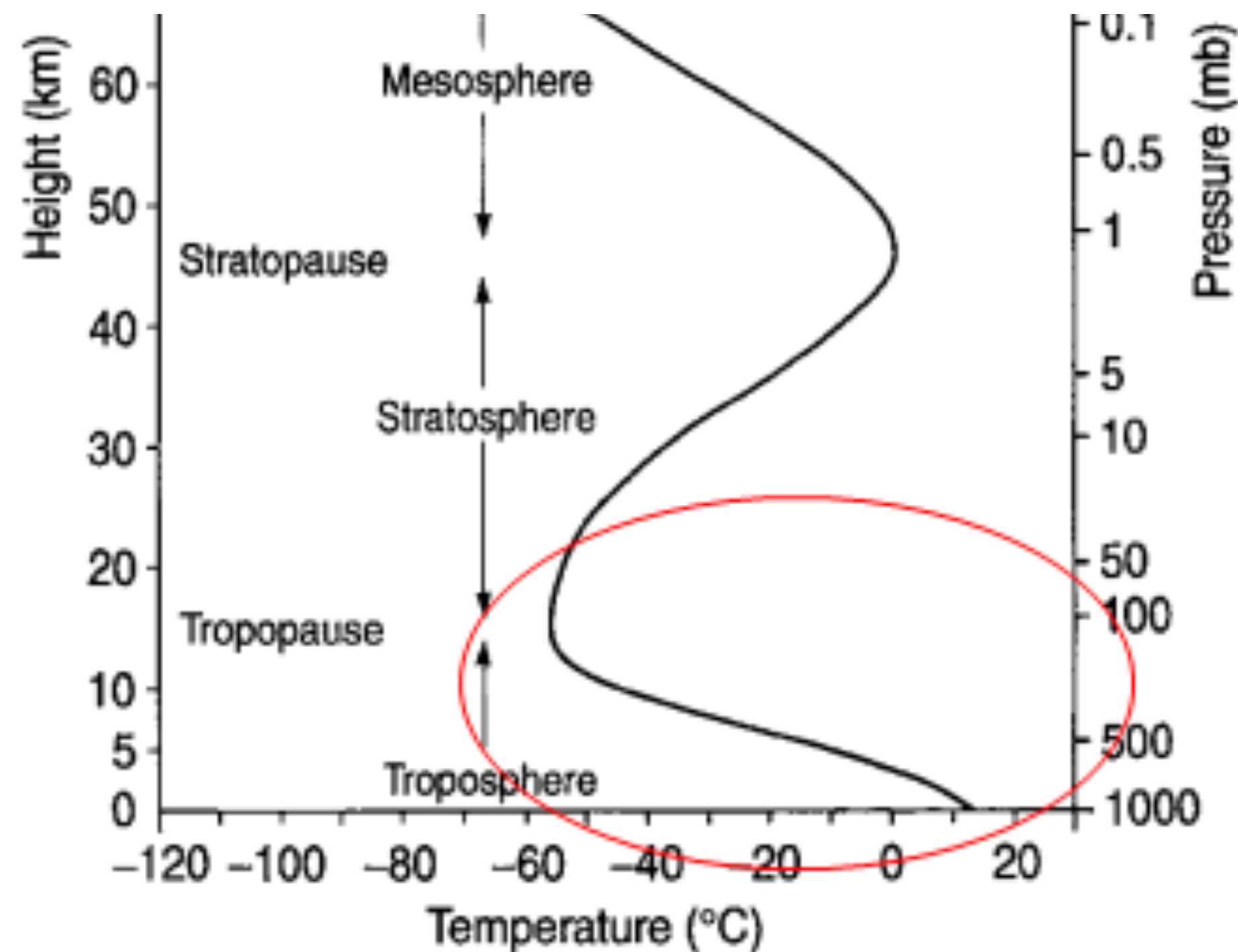


# Atmospheric Pressure Structure

Hot air rises but it also gets colder as you go up, how does that work?



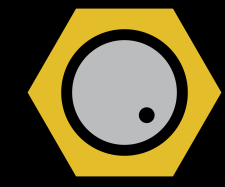
Change in pressure with altitude causes a change in the temperature



As you go up in the atmosphere the pressure drops and how it does this is important.



# Consider a Column of Air

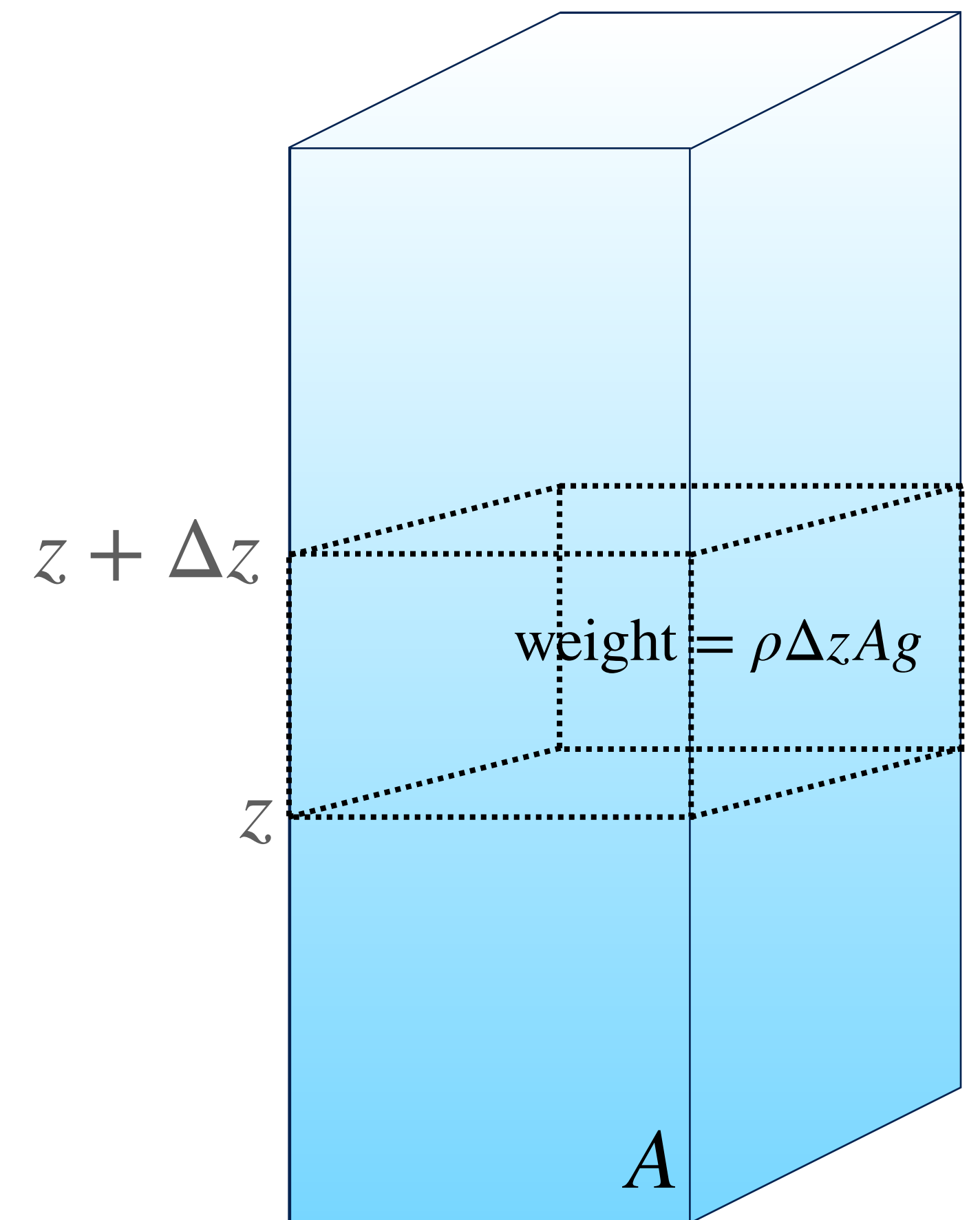


How does the pressure change with height,  $z$ ?

The pressure for a column of air is just due to the weight of that air

$$\text{weight} = \rho Ag \Delta z$$

$$P(z) - P(z + \Delta z) = \frac{\rho(z)Ag\Delta z}{A} = \rho(z)g\Delta z$$





# Consider a Column of Air

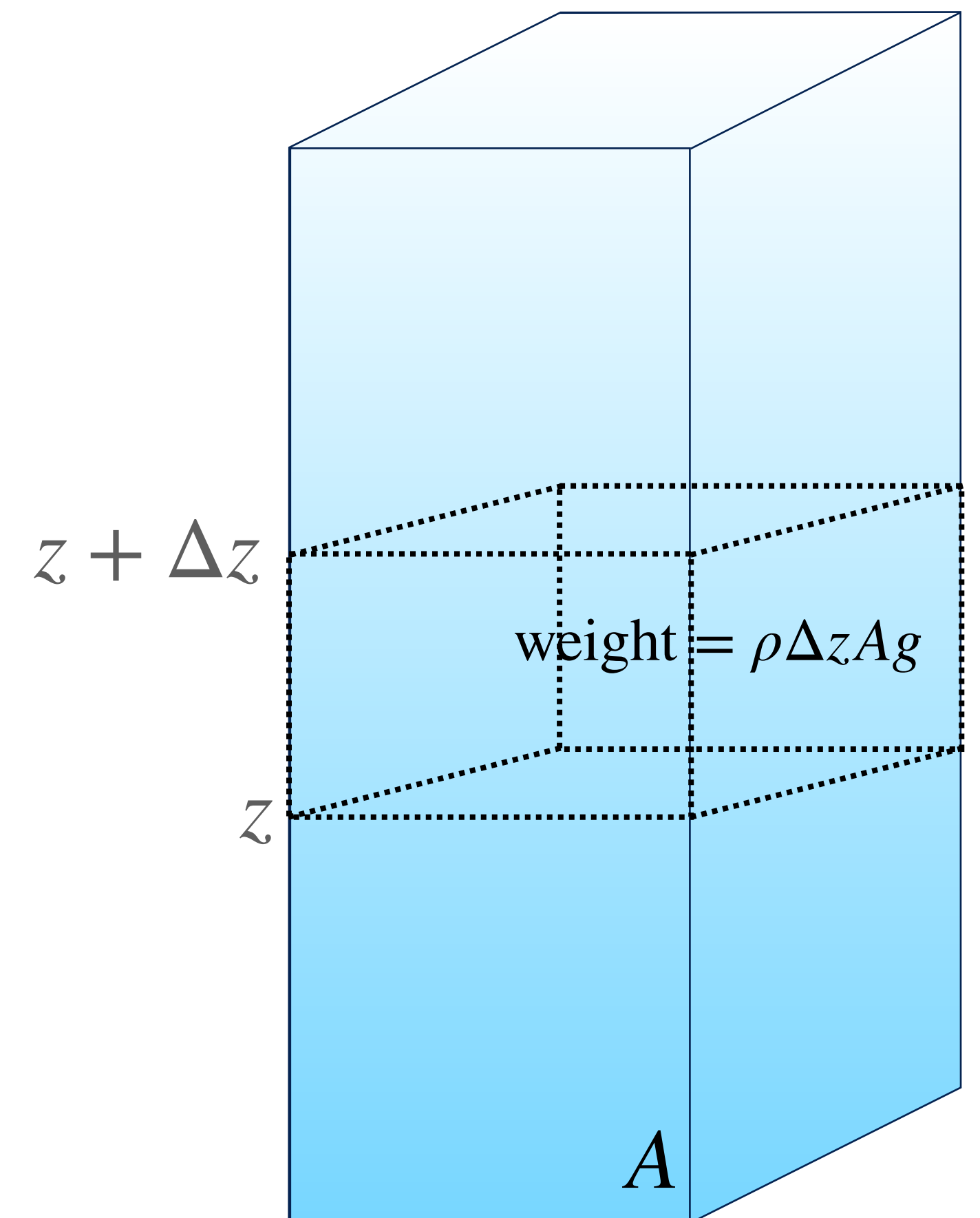
How does the pressure change with height,  $z$ ?

The pressure for a column of air is just due to the weight of that air

$$\text{weight} = \rho Ag \Delta z$$

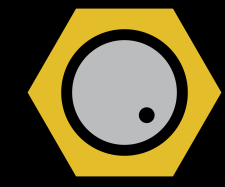
$$P(z) - P(z + \Delta z) = \frac{\rho(z) Ag \Delta z}{A} = \rho(z) g \Delta z$$

This assumes that density is constant. Therefore,  $\Delta z$  must be very small





# Consider a Column of Air



How does the pressure change with height,  $z$ ?

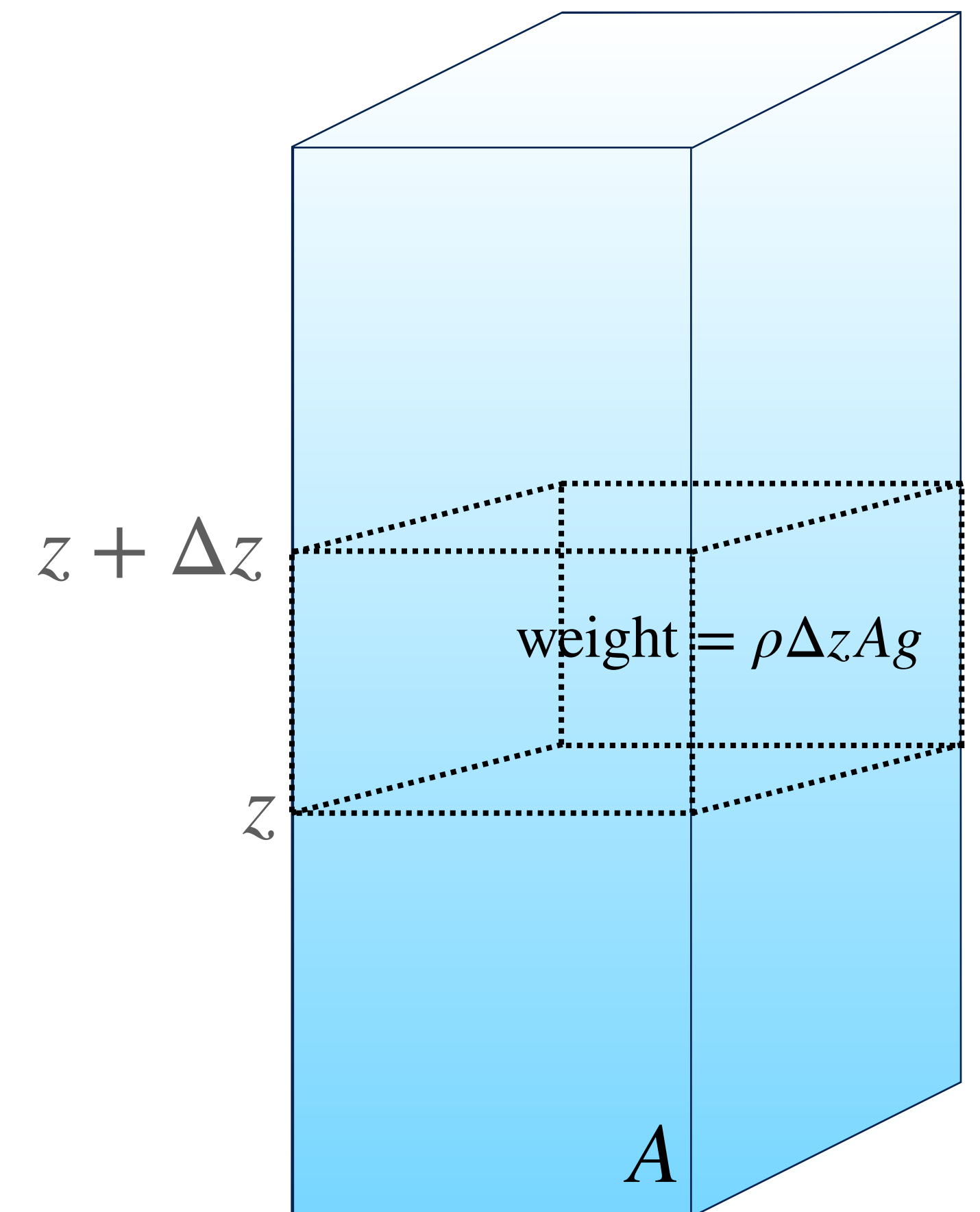
The pressure for a column of air is just due to the weight of that air

$$\text{weight} = \rho Ag \Delta z$$

$$P(z) - P(z + \Delta z) = \frac{\rho(z) Ag \Delta z}{A} = \rho(z) g \Delta z$$

This assumes that density is constant. Therefore,  $\Delta z$  must be very small

At the limit where  $\Delta z \rightarrow 0$



# Consider a Column of Air

How does the pressure change with height,  $z$ ?

The pressure for a column of air is just due to the weight of that air

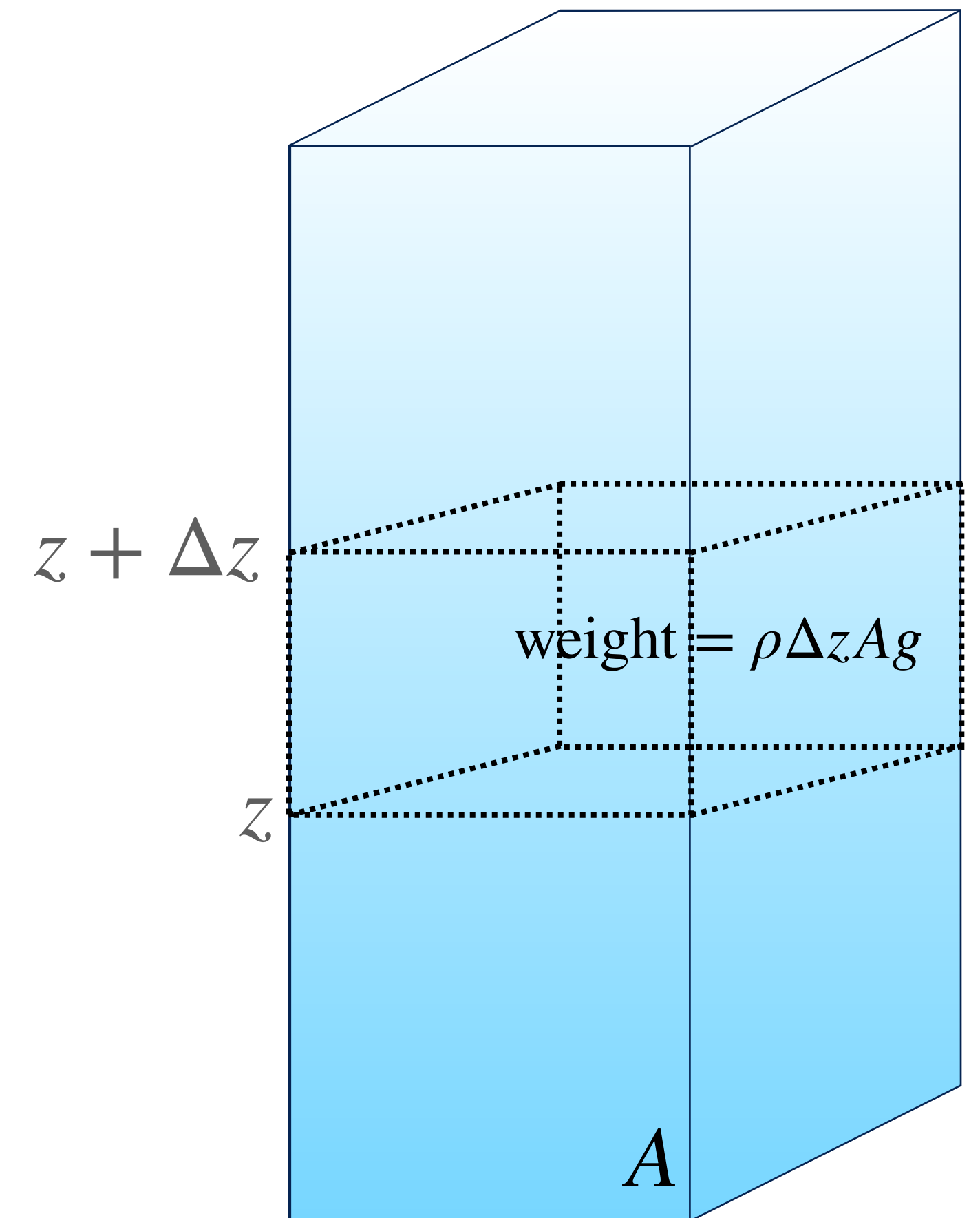
$$\text{weight} = \rho A g \Delta z$$

$$P(z) - P(z + \Delta z) = \frac{\rho(z) A g \Delta z}{A} = \rho(z) g \Delta z$$

This assumes that density is constant. Therefore,  $\Delta z$  must be very small

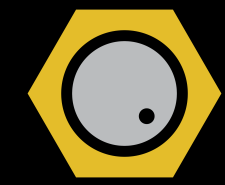
At the limit where  $\Delta z \rightarrow 0$

$$\frac{\partial P}{\partial z} = -\rho g$$





# Hydrostatic Equilibrium



In the limit that the air is not moving we can say it is in hydrostatic equilibrium

Change in pressure with increased altitude, is decreasing as density times gravity

$$\frac{\partial P}{\partial z} = -\rho g$$

This works for any situation where only the force acting is gravity

If the air is not moving this is then said to be in  
**Hydrostatic Equilibrium**

Treating it as an ideal gas:

$$PV = nRT = nk_B N_A T$$

Pressure

$$\frac{\partial P}{\partial z} = -\frac{g}{R' T} P$$

Density

$$\frac{\partial(\rho T)}{\partial z} = -\frac{g}{R'} \rho$$

Have to keep T in the derivative as it may change with altitude

# Atmospheric Scale Height

Height at which pressure decreases by a factor of  $e$  (exponent)

$$\frac{\partial(\rho T)}{\partial z} = -\frac{g}{R'}\rho$$

If we fix  $T$  (for Earth average  $T = 287$  K)

We get the rate of change of density with height is equal to minus constant times density

If we differentiate density with height we get,

$$\rho(z) = \rho_0 e^{-\frac{z}{H}}$$

where,

$$H = \frac{R' T}{g} = \frac{RT}{M_{air}g} = \frac{k_B T}{\mu g}$$

SCALE HEIGHT

This is the length scale of the atmosphere where  $P$  and  $\rho$  changes by  $e$



# Optical Depth and Absorption Cross Sections

How much stuff the light will pass through

Optical depth ( $\tau$ ) is a dimensionless measure of how far the light has penetrated down into the atmosphere from the top

Roughly how much 'stuff' the light will pass through

It takes into account the modifying effects of both mass extinction and density, at a specific wavelength

$$\tau_\nu = \int_z^{z_{\text{top}}} \kappa_\nu(z') \rho_a(z') dz'$$

Mass extinction coefficient      Density of gas      Altitude

# Optical Depth and Absorption Cross Sections

How much stuff the light will pass through

Optical depth ( $\tau$ ) is a dimensionless measure of how far the light has penetrated down into the atmosphere from the top  
Roughly how much 'stuff' the light will pass through

At slant geometries this becomes:

Such that the Earth's atmosphere at slant geometries is 75x that at normal to the planet. Hot Jupiters range from ~35-90x normal

$$\tau(\lambda, z) \approx \sigma(\lambda) n(z) \sqrt{2\pi R_p H}$$

Absorbing cross section      Volume density      Area of atmosphere



# Effective Altitude



Height at which pressure decreases by a factor of e (exponent)

We can then calculate the effective altitude of a planetary atmosphere by assuming it is in hydrostatic equilibrium with a constant density profile and gravity we get,

Effective altitude of transmission  $\rightarrow$

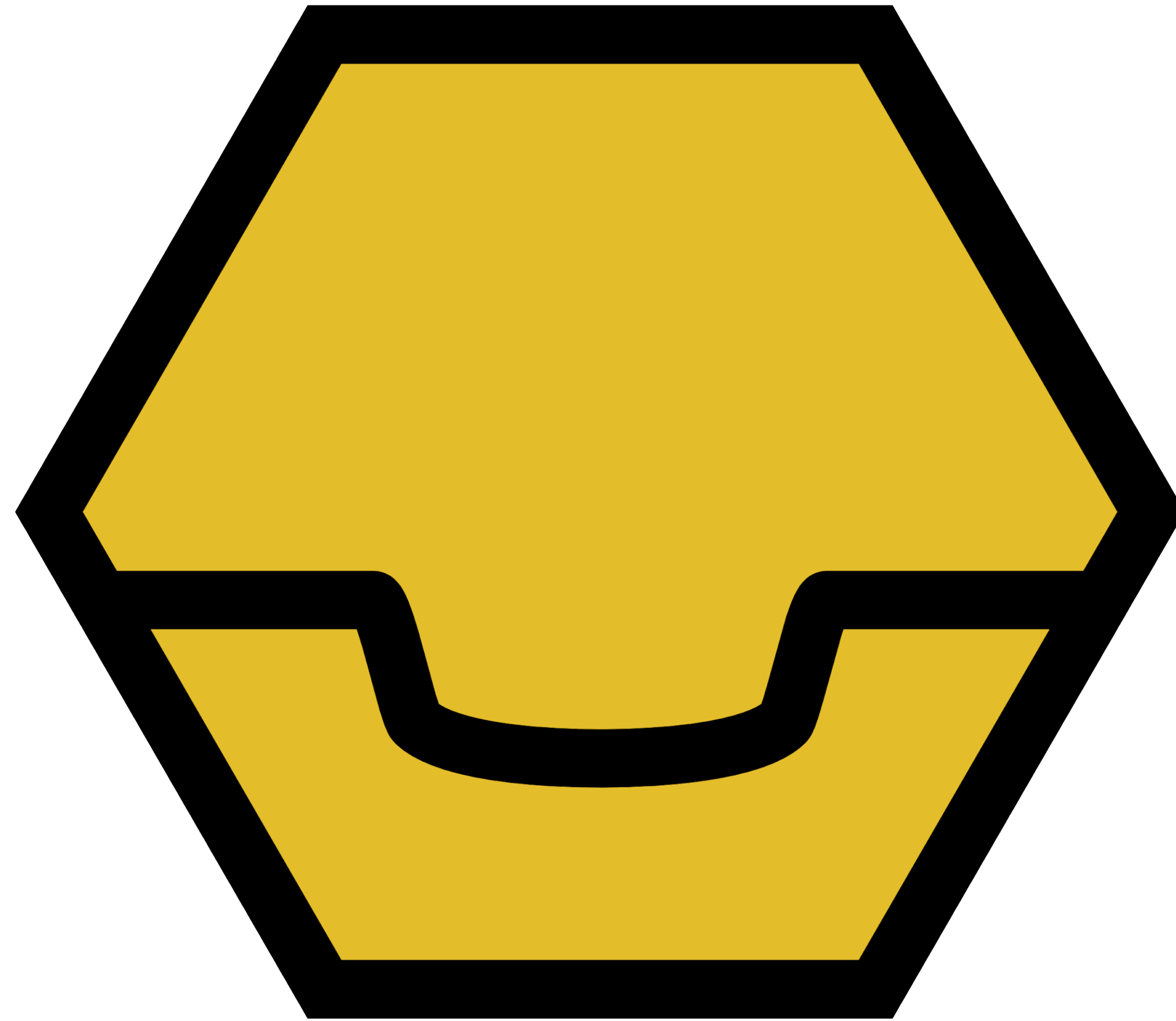
$$z(\lambda) = H \ln \left( \frac{\xi_{\text{abs}} P_{z=0} \sigma_{\text{obs}}(\lambda)}{\tau_{\text{eq}}} \times \sqrt{\frac{2\pi R_p}{k_B T_p \mu g_p}} \right)$$

Species abundance  $\rightarrow$   $\xi_{\text{abs}}$   
Pressure base  $\rightarrow$   $P_{z=0}$   
Species cross section  $\rightarrow$   $\sigma_{\text{obs}}(\lambda)$   
Scale height  $\rightarrow$   $H$   
Optical depth  $\rightarrow$   $\tau_{\text{eq}}$



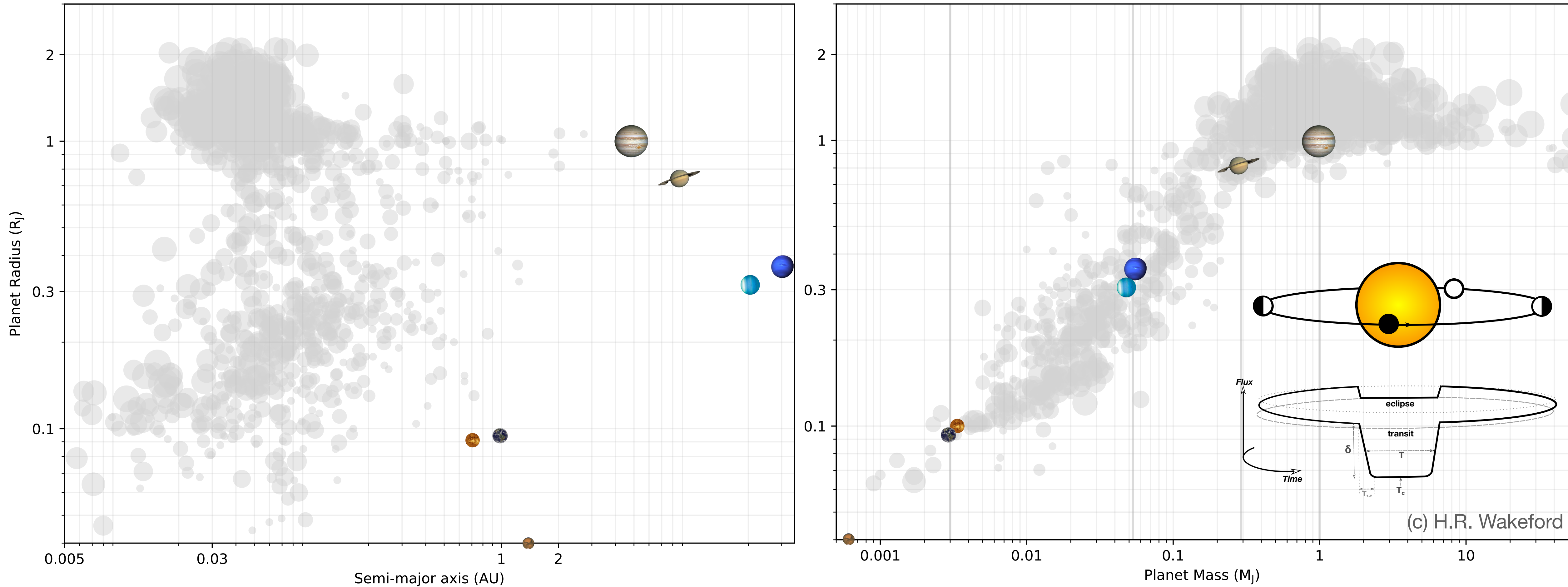
# Getting Transmission Spectra from Data

An introduction



# Exoplanet distribution compared to the solar system

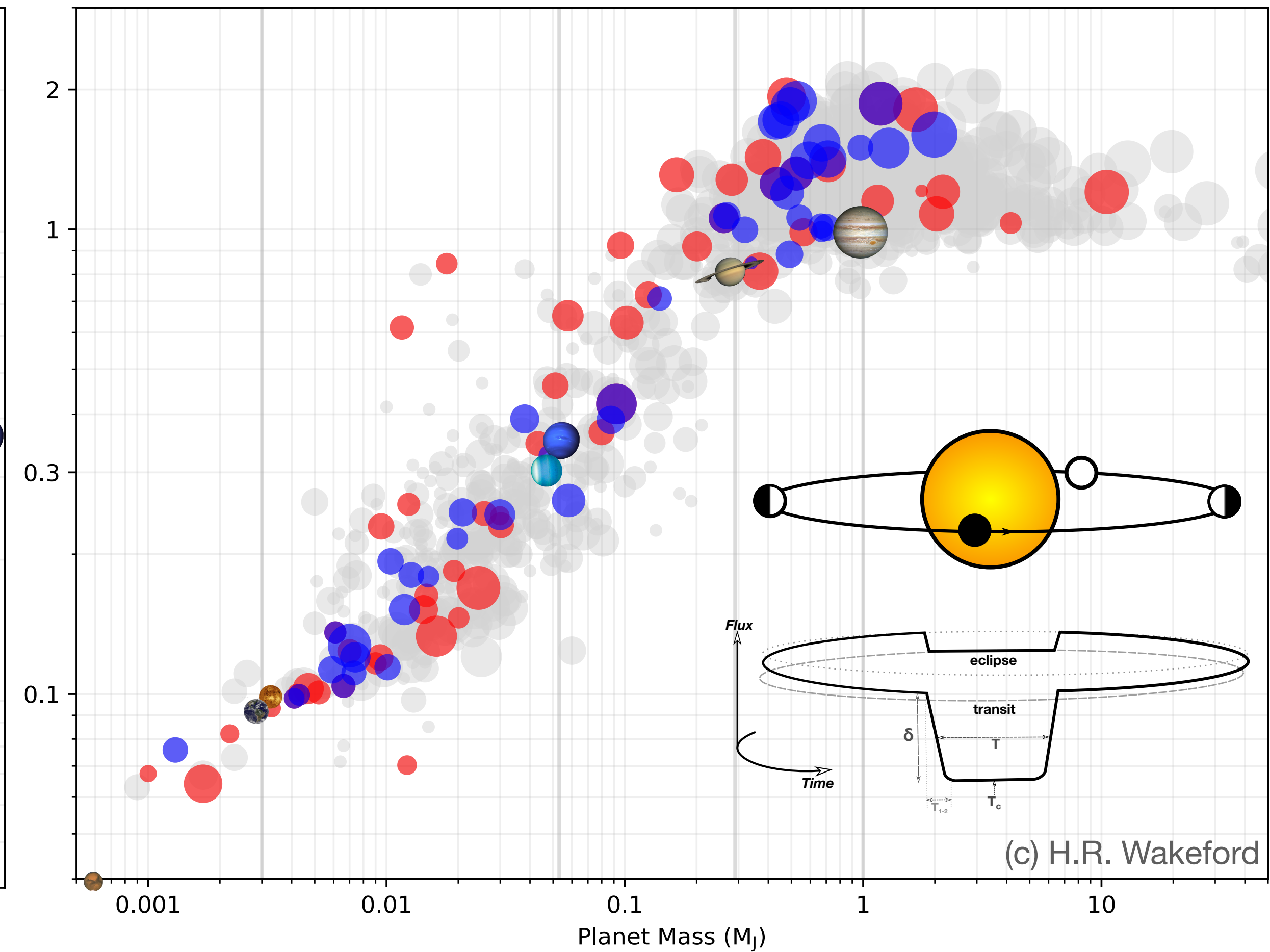
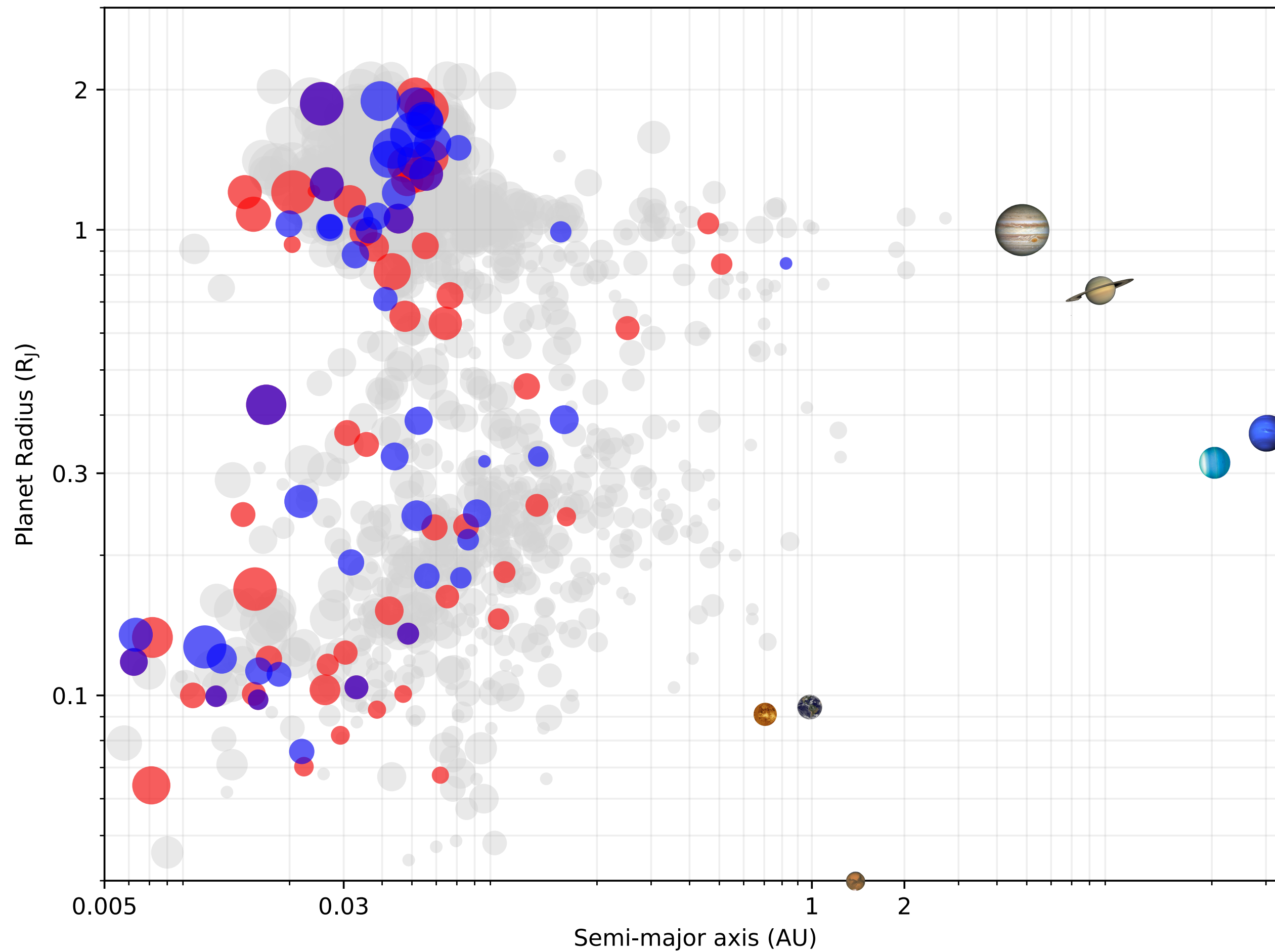
1000+ exoplanets have both Mass and Radius measurements





# Transiting Exoplanet Atmospheres

How do we measure the atmosphere of a transiting exoplanet?

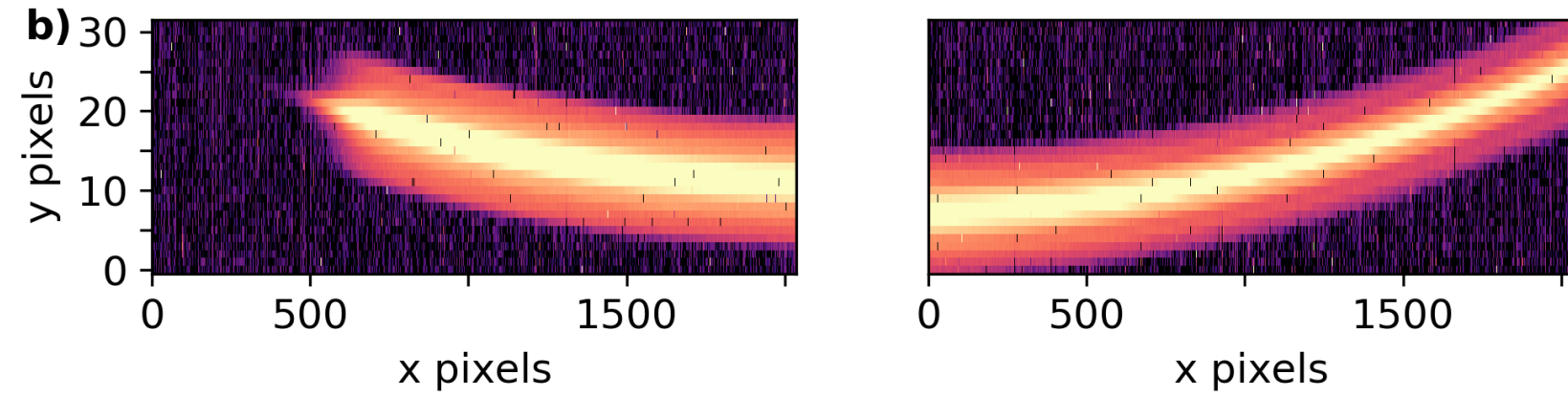


(c) H.R. Wakeford

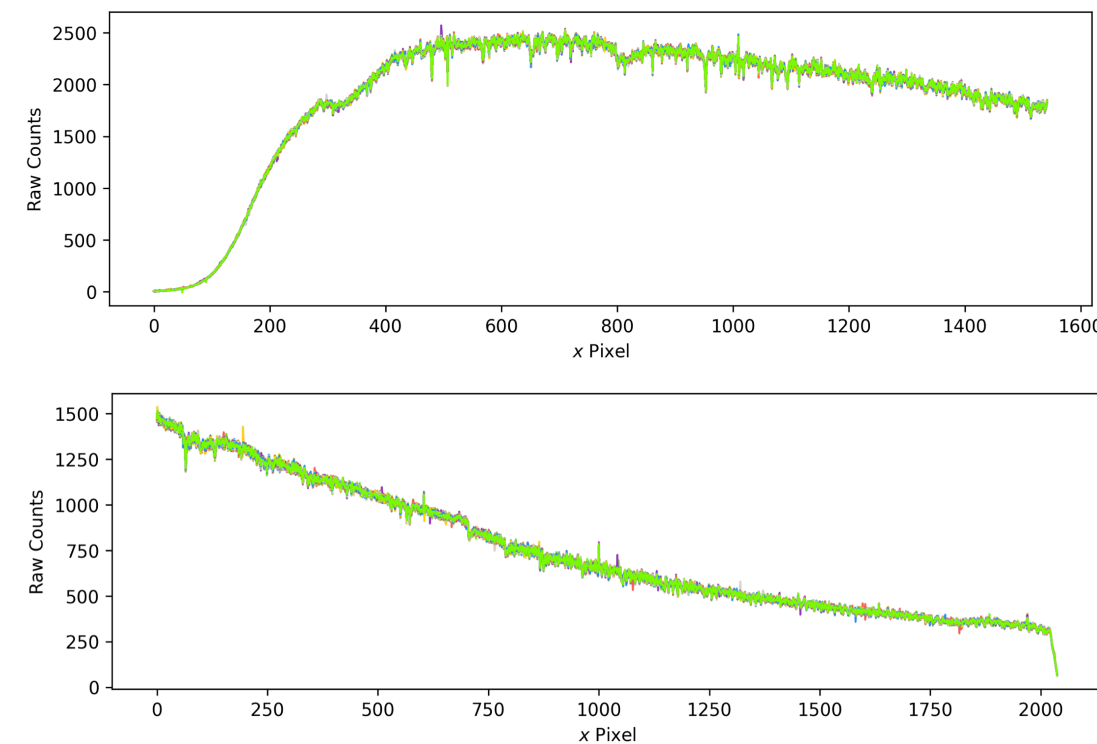
# From Observations to Light Curves to Spectra



Measuring the change in transit depth as a function of wavelength



From 2D images  
to  
1D stellar spectra

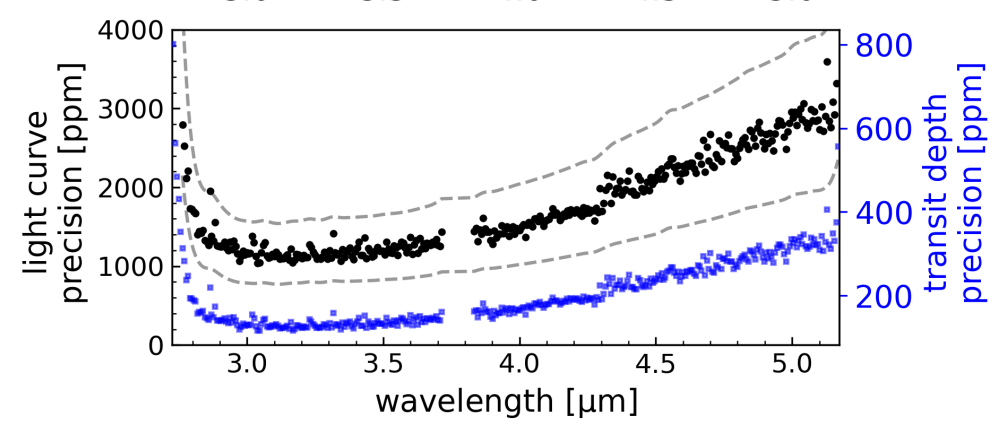
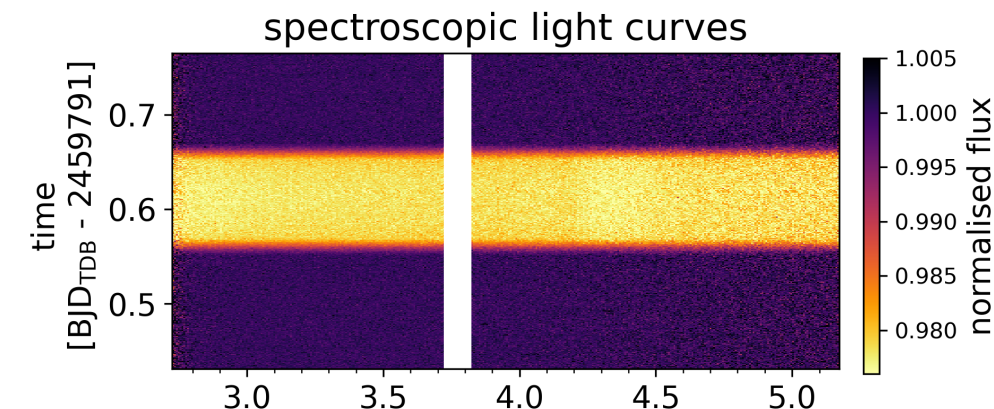
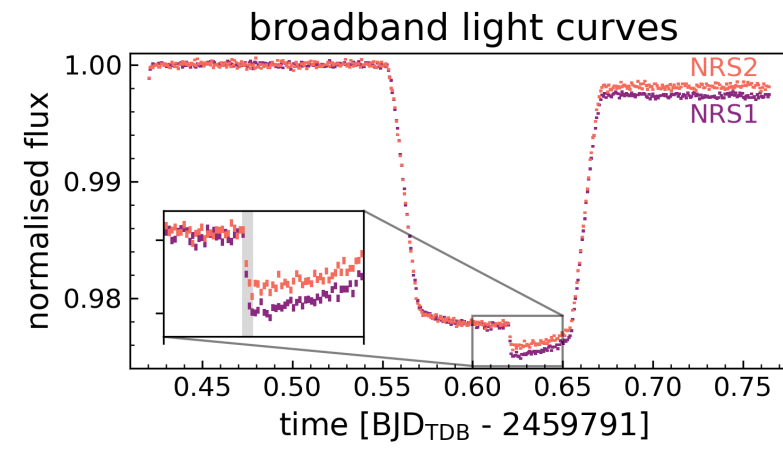
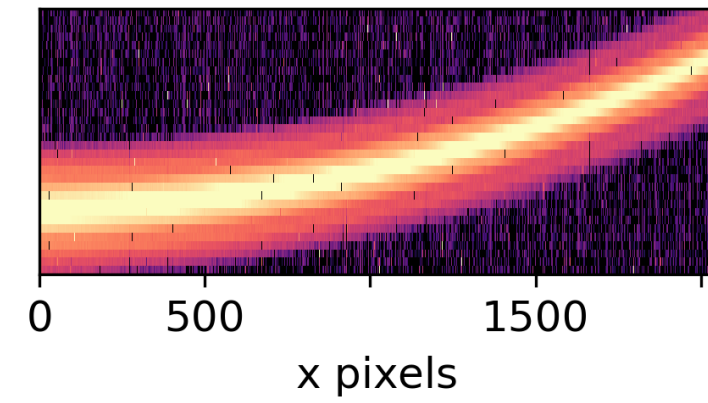
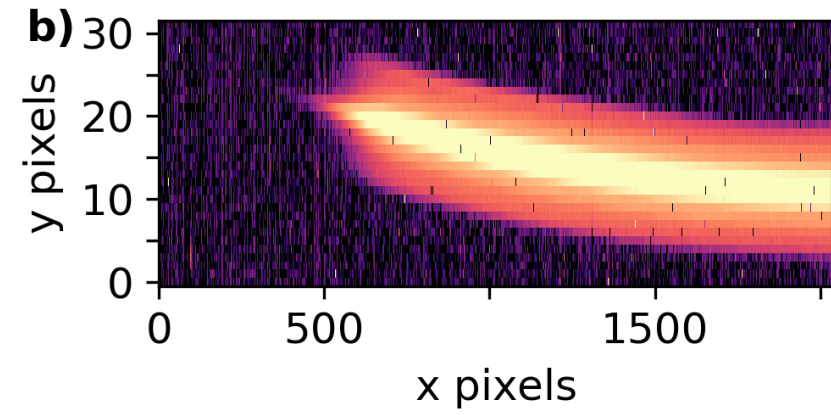




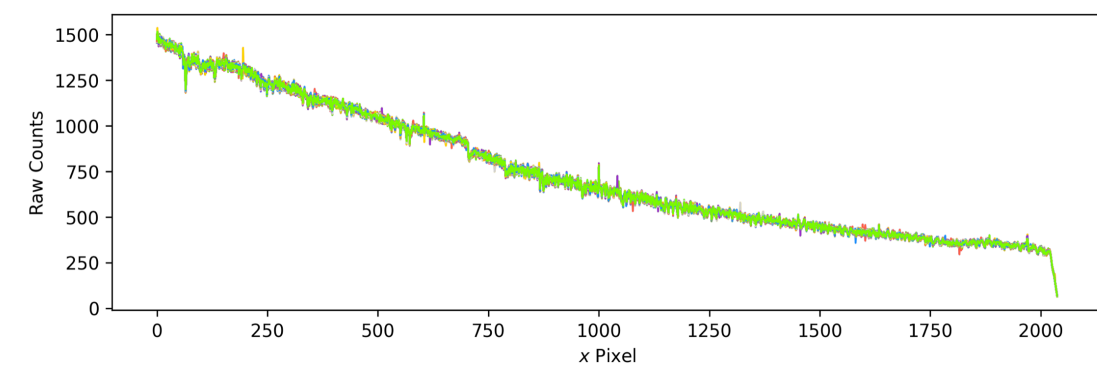
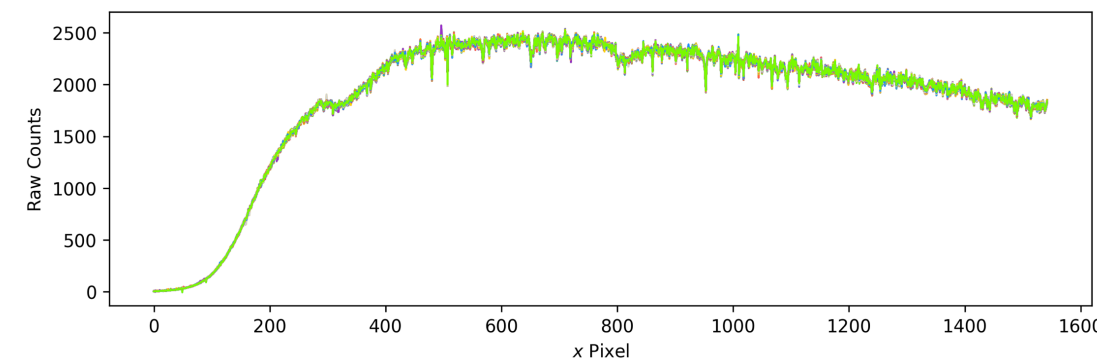
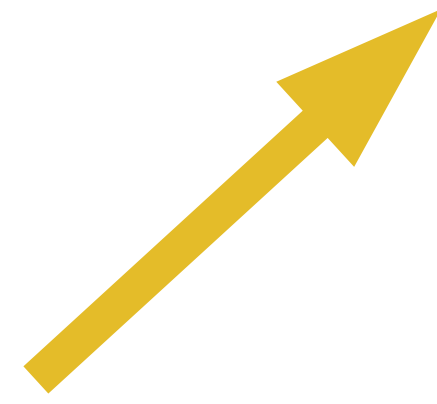
# From Observations to Light Curves to Spectra



## Measuring the change in transit depth as a function of wavelength

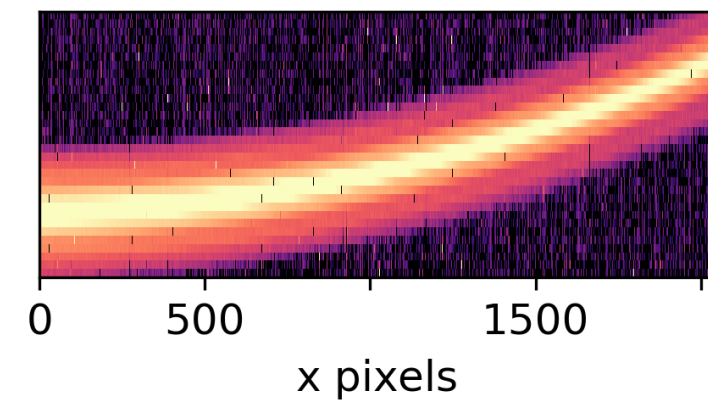
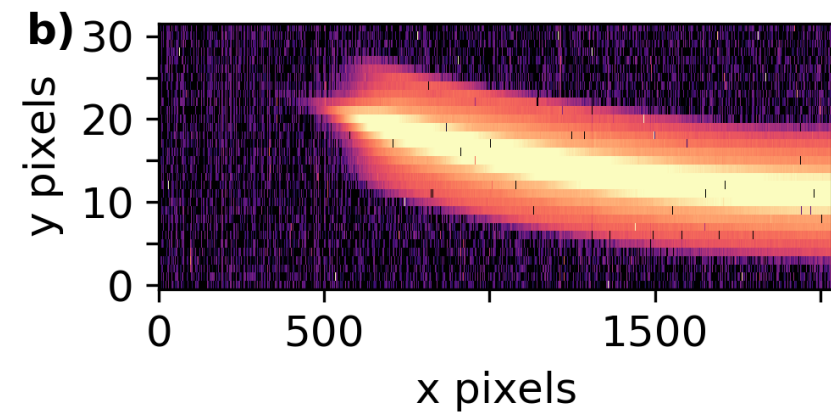


From 2D images  
to  
1D stellar spectra

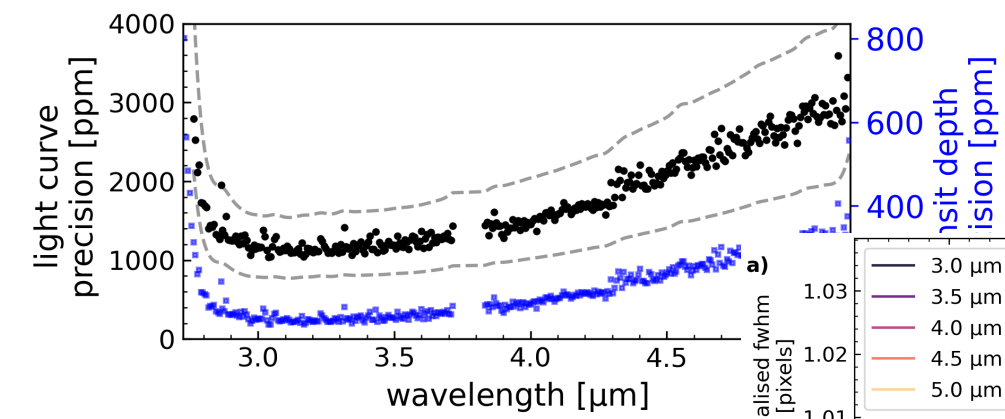
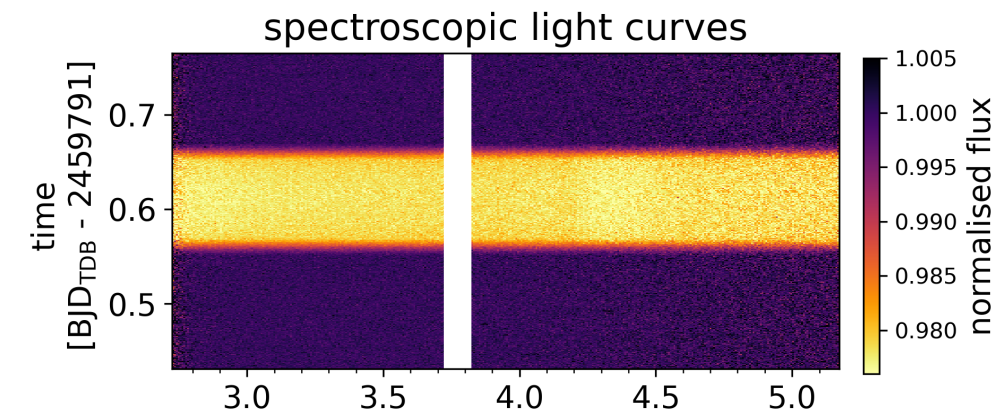
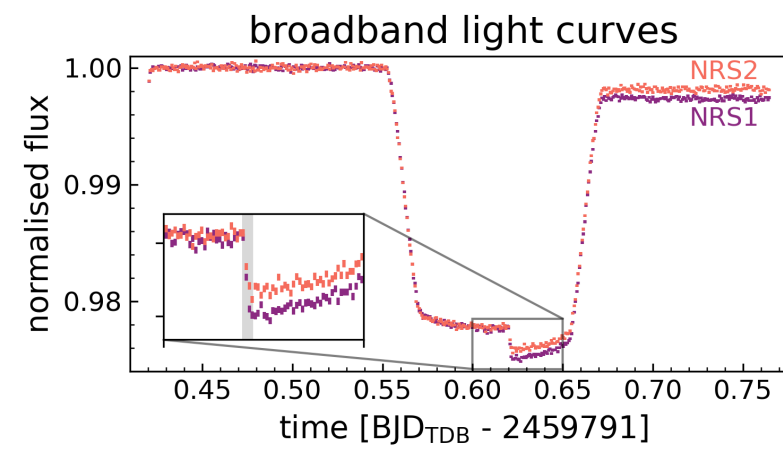
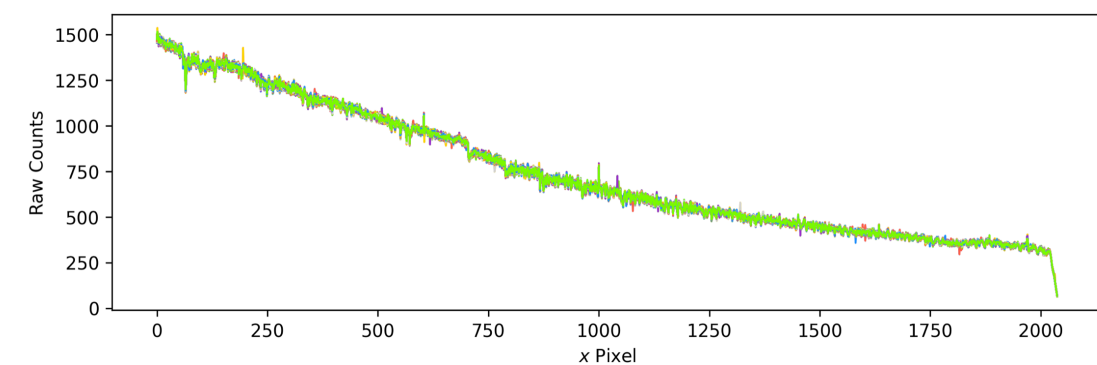
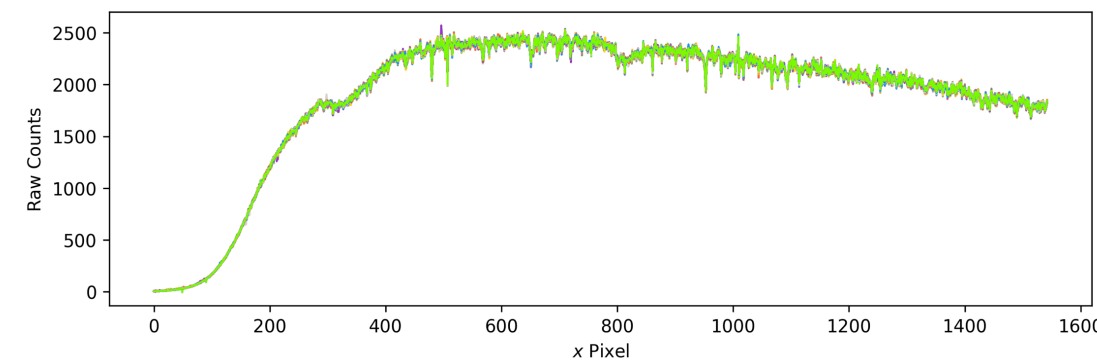
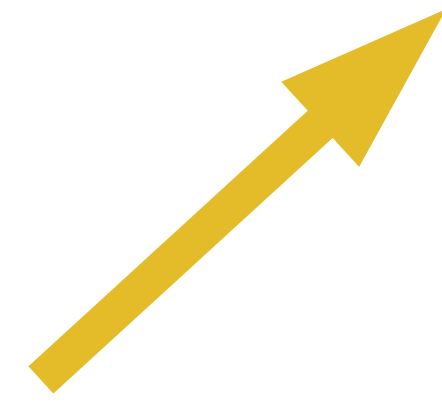


# From Observations to Light Curves to Spectra

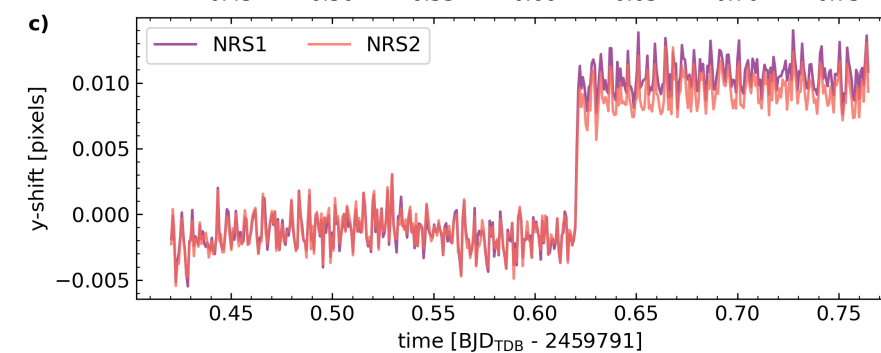
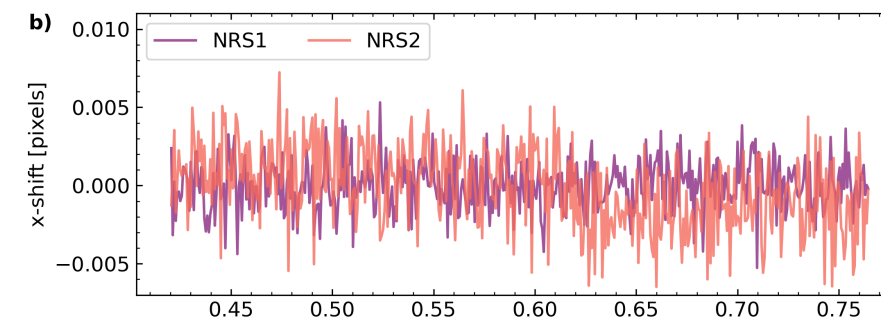
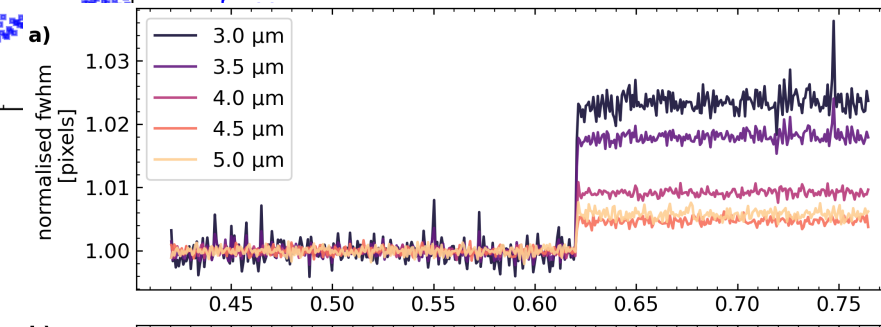
Measuring the change in transit depth as a function of wavelength



From 2D images  
to  
1D stellar spectra



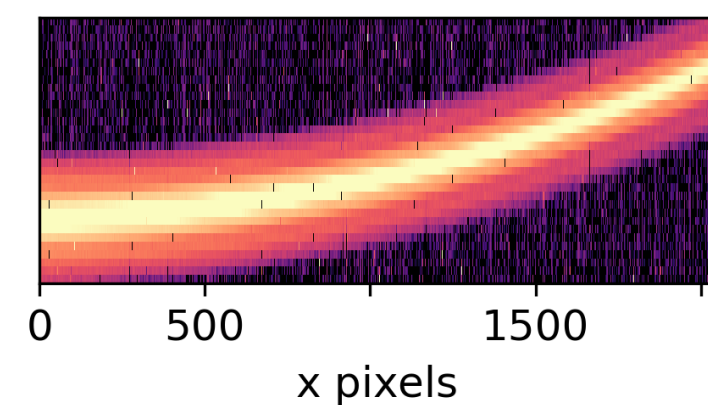
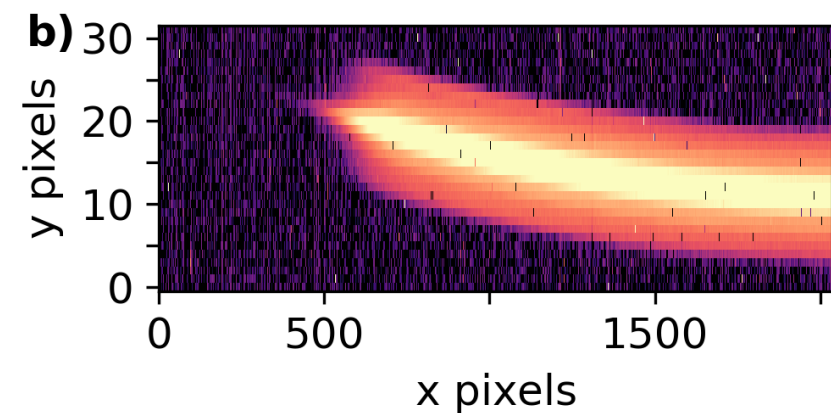
Detrending  
parameters



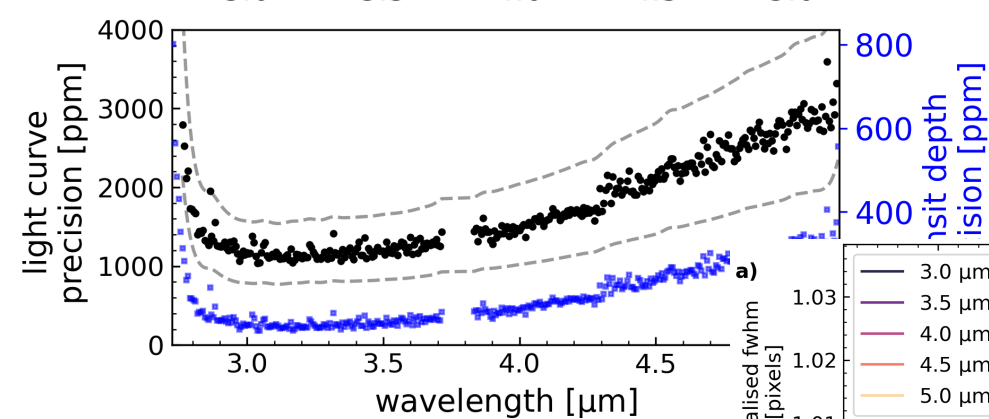
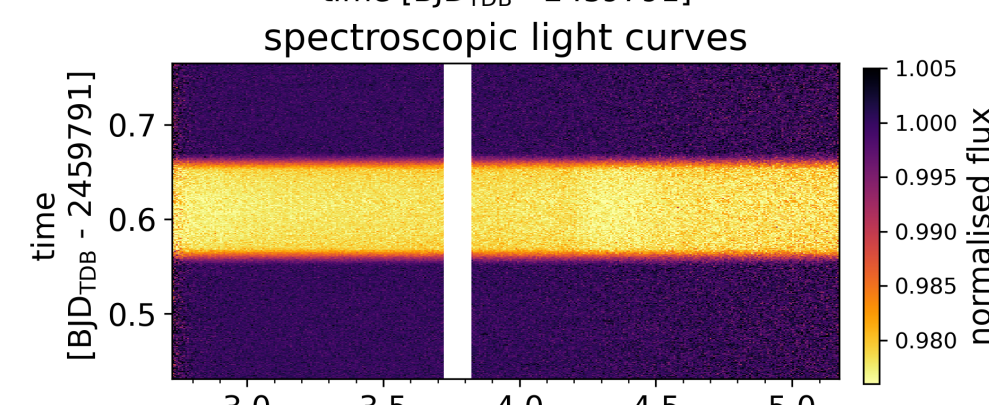
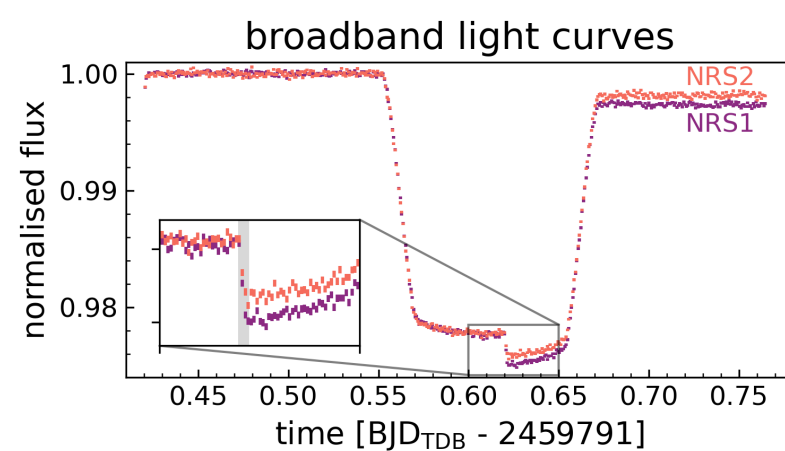
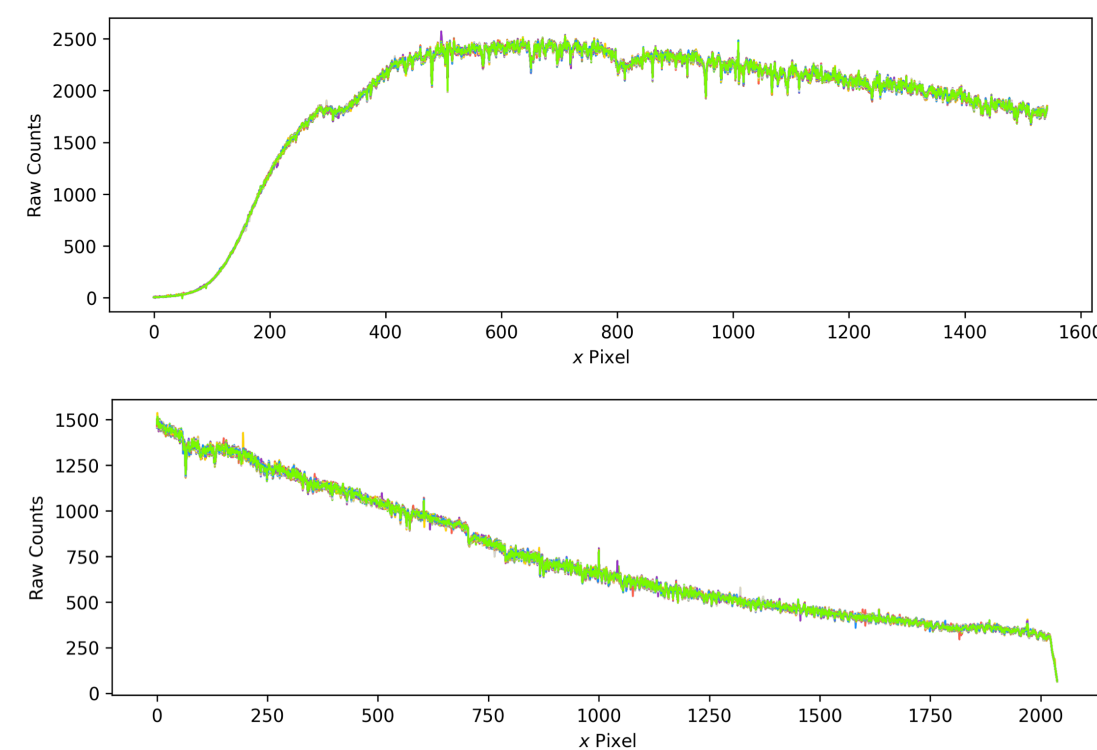
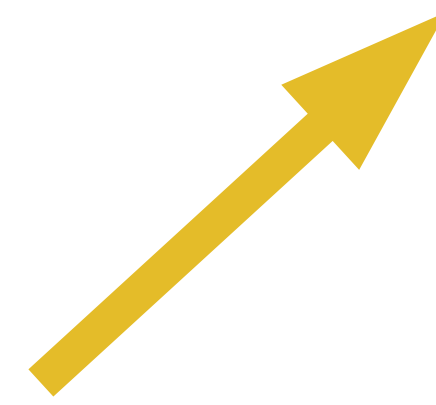


# From Observations to Light Curves to Spectra

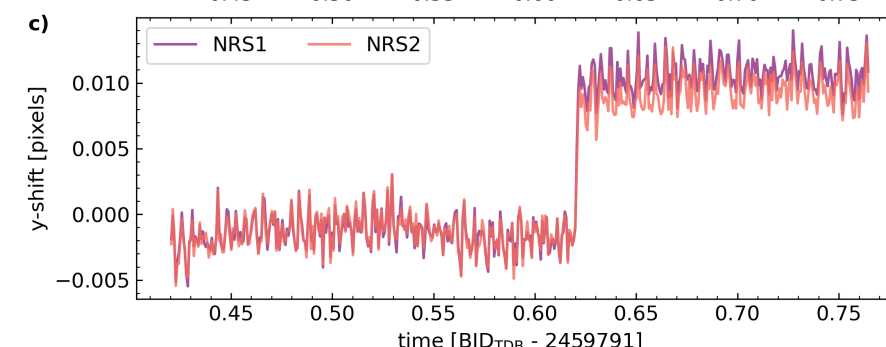
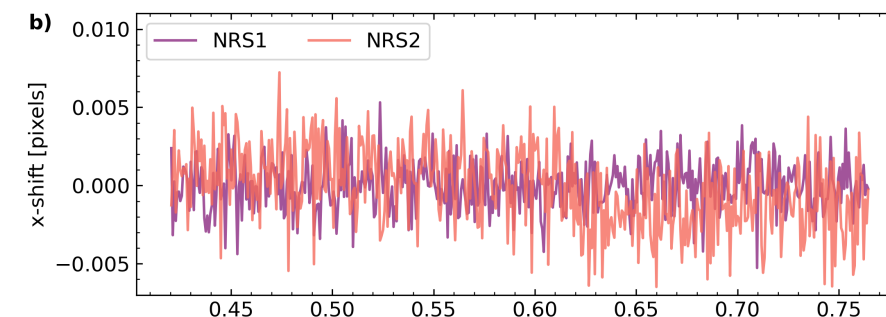
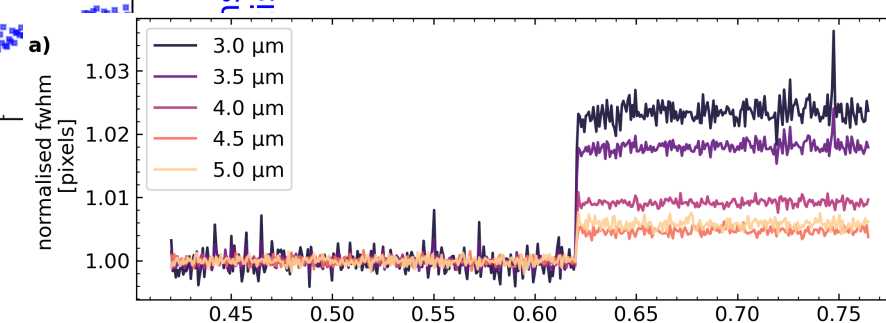
## Measuring the change in transit depth as a function of wavelength



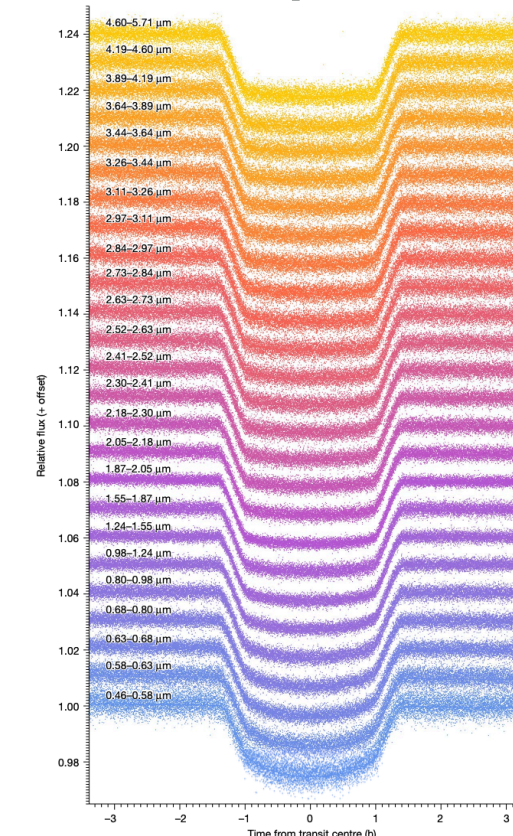
From 2D images  
to  
1D stellar spectra



Detrending  
parameters



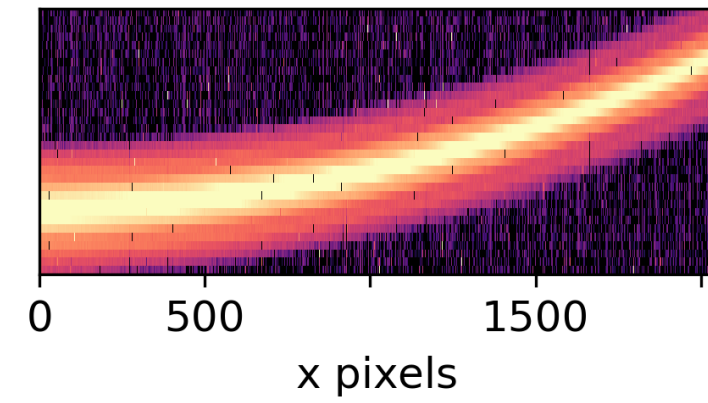
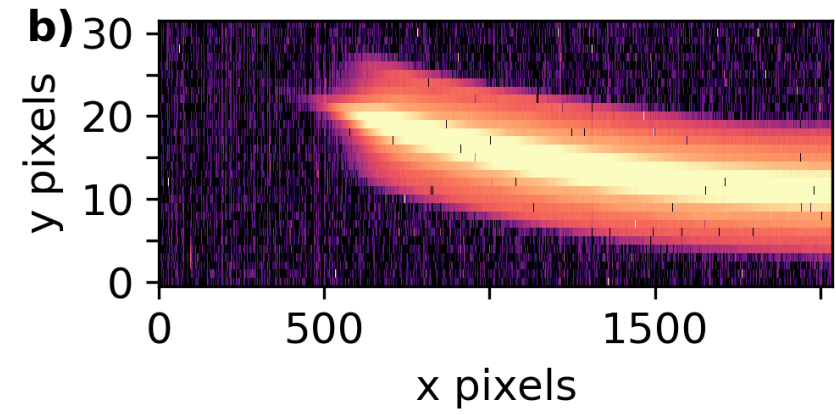
Fitted light curve



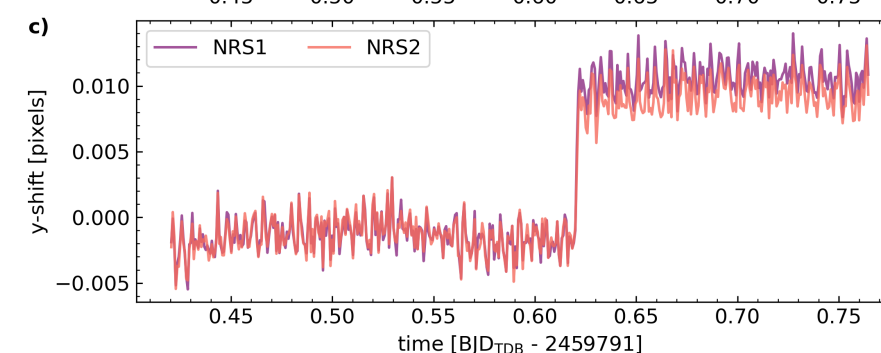
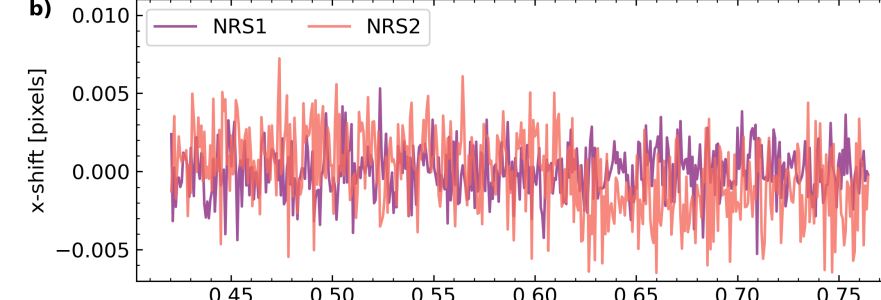
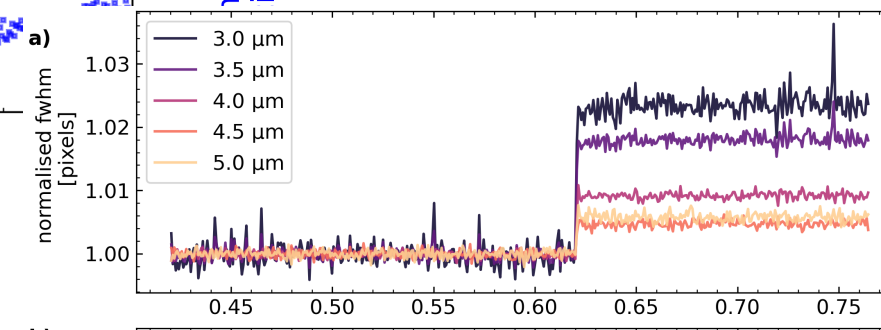
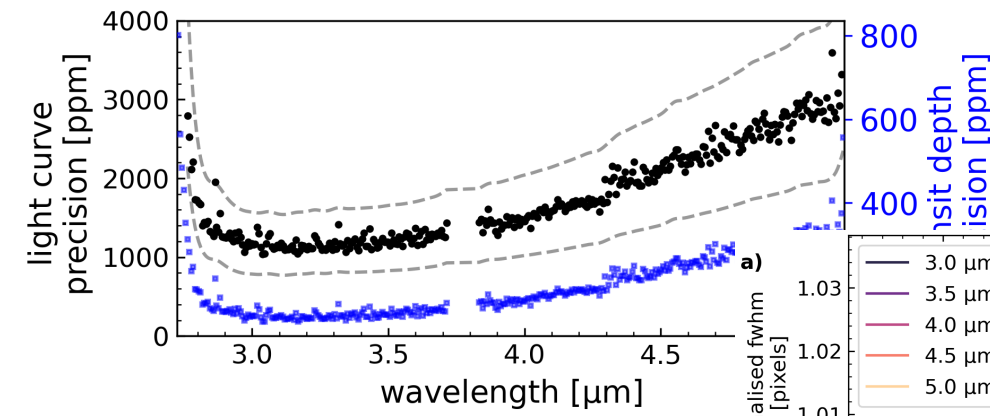
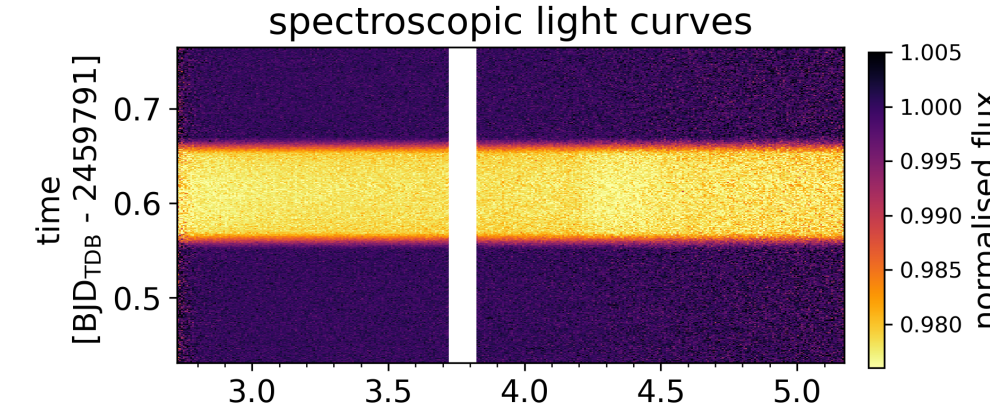
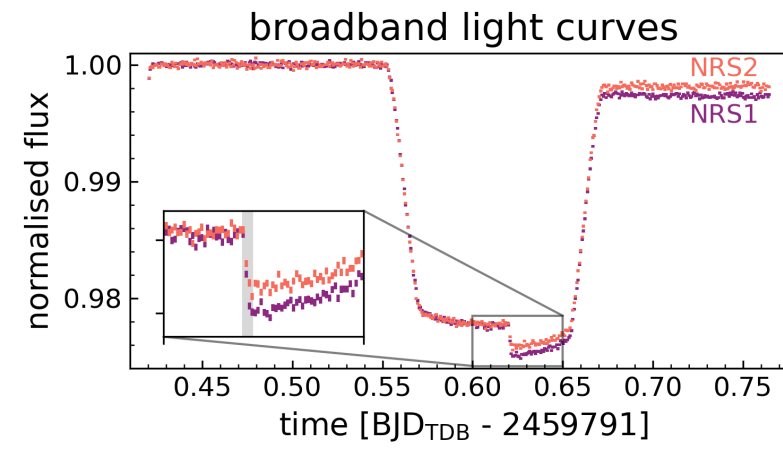
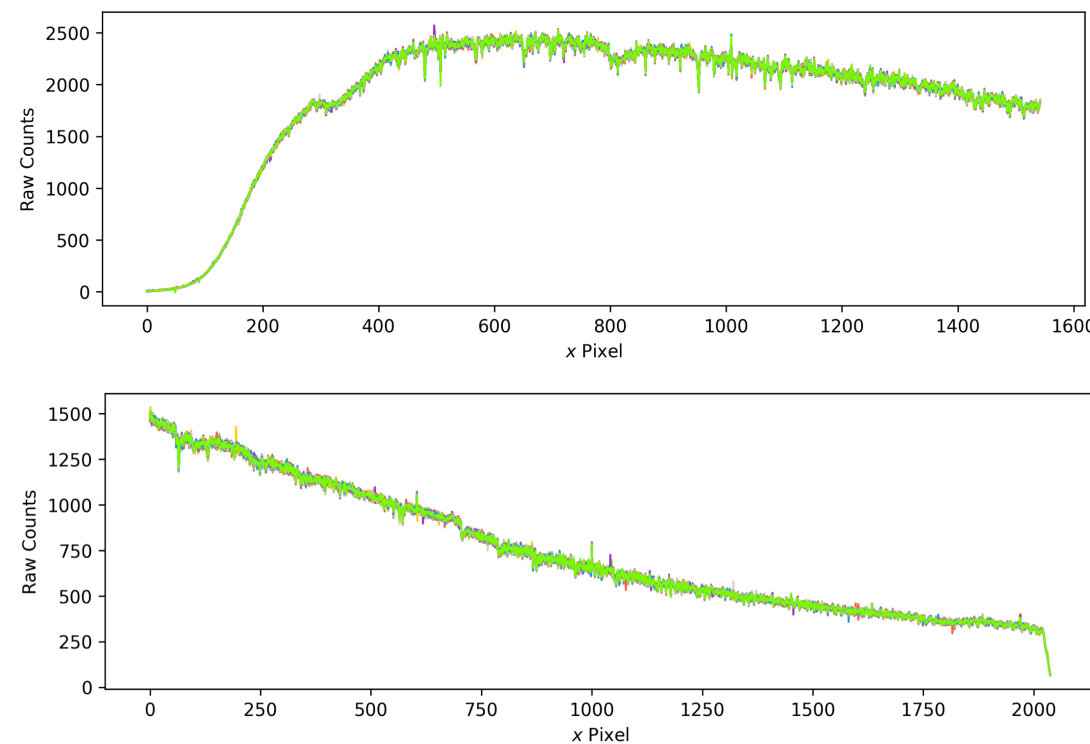


# From Observations to Light Curves to Spectra

Measuring the change in transit depth as a function of wavelength

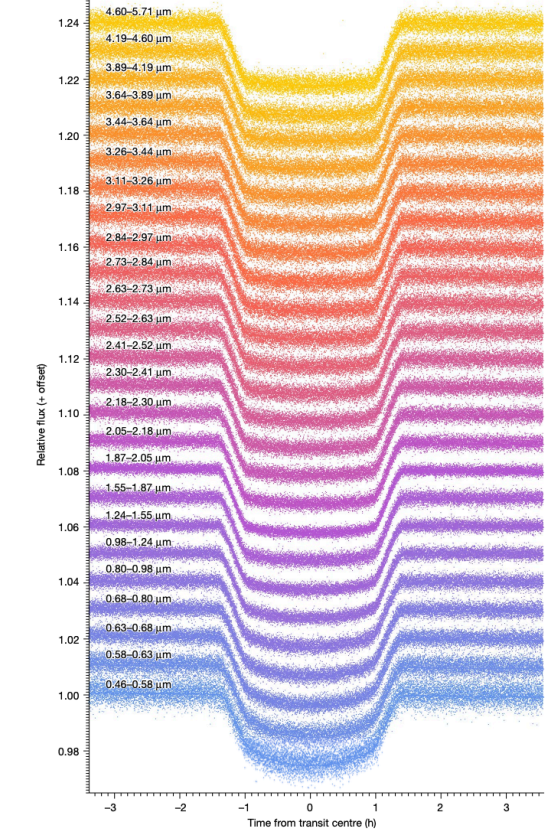


From 2D images  
to  
1D stellar spectra

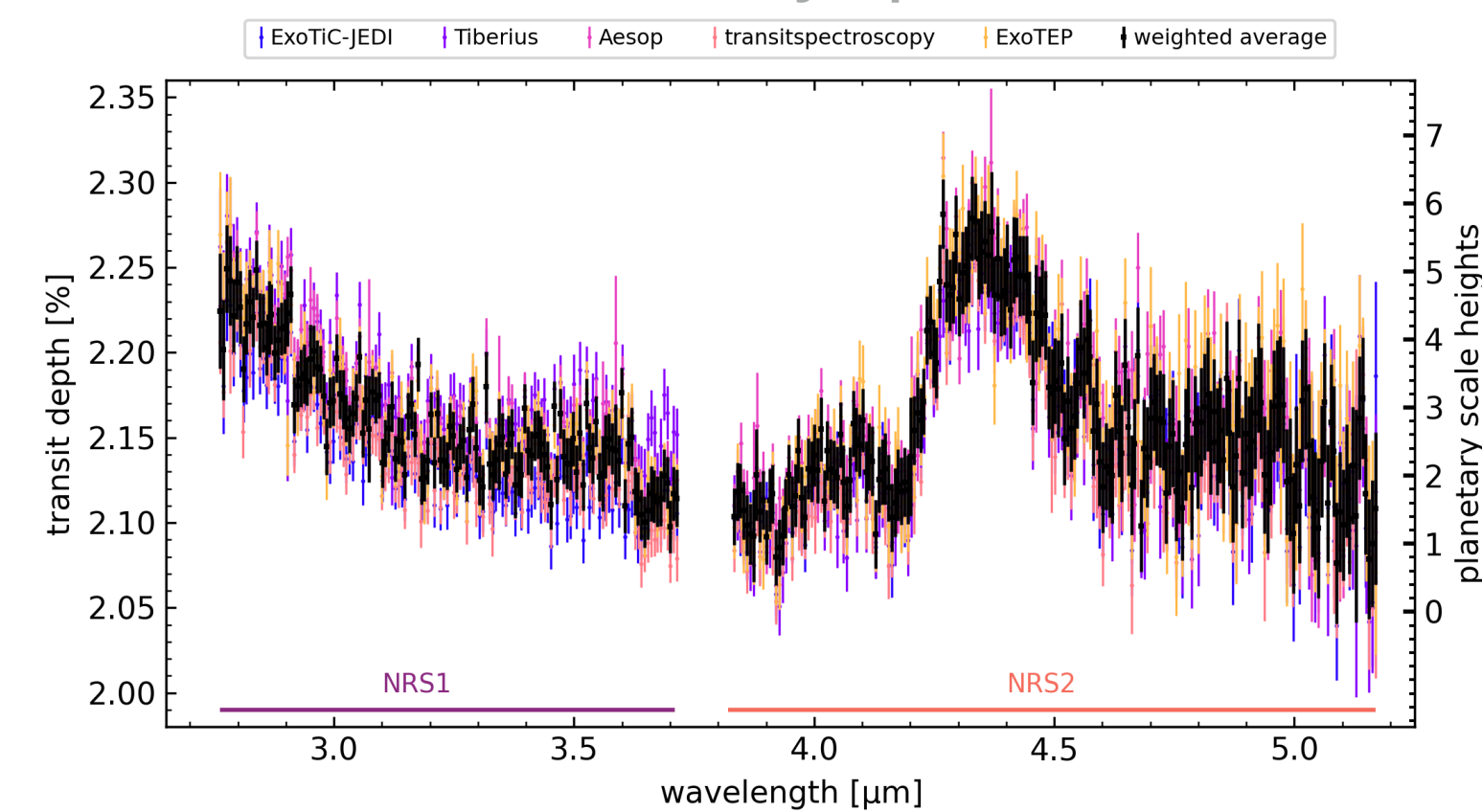


+  
Detrending  
parameters

Fitted light curve



Planetary spectrum





# Fitting Your Light Curve Systematics



Accurately treating systematics is key even when not apparent in the data

## Systematic Model

### Simple

Single systematic models  
Common-mode  
wavelength independent  
model

### Complex

Marginalization  
Jitter decorrelation  
GP

## Solver

Least-square minimizer

Fastest

MCMC/ nested  
sampler

Slow

GP

Faster

## Parameter Estimation

Single uncertainty on parameters  
Output covariance matrix

Full posterior of estimated parameters  
Correlation between parameters

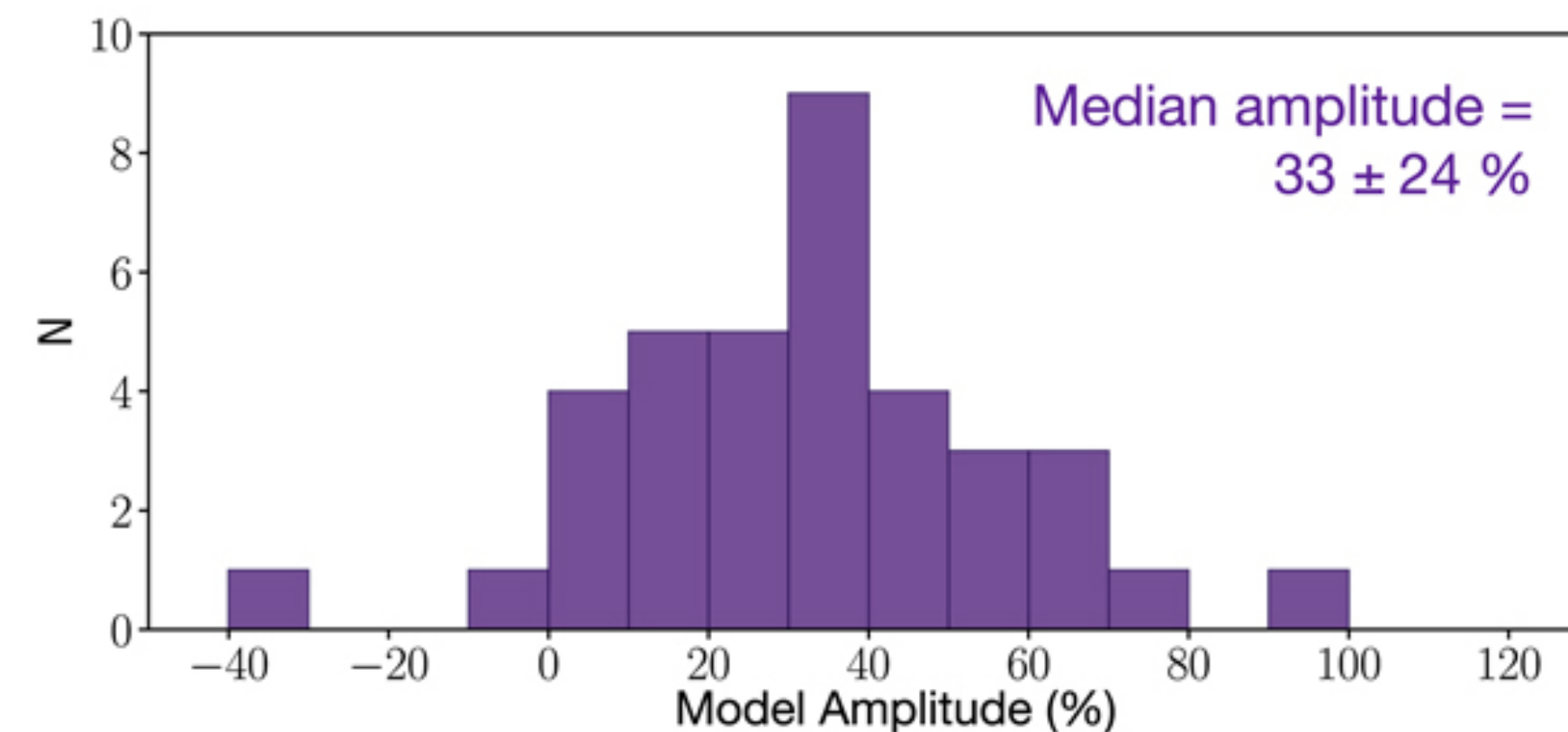
The larger suite of models considered, the smaller the space assigned to the probability that none of your models can explain your data.

# Transmission Spectra with Hubble

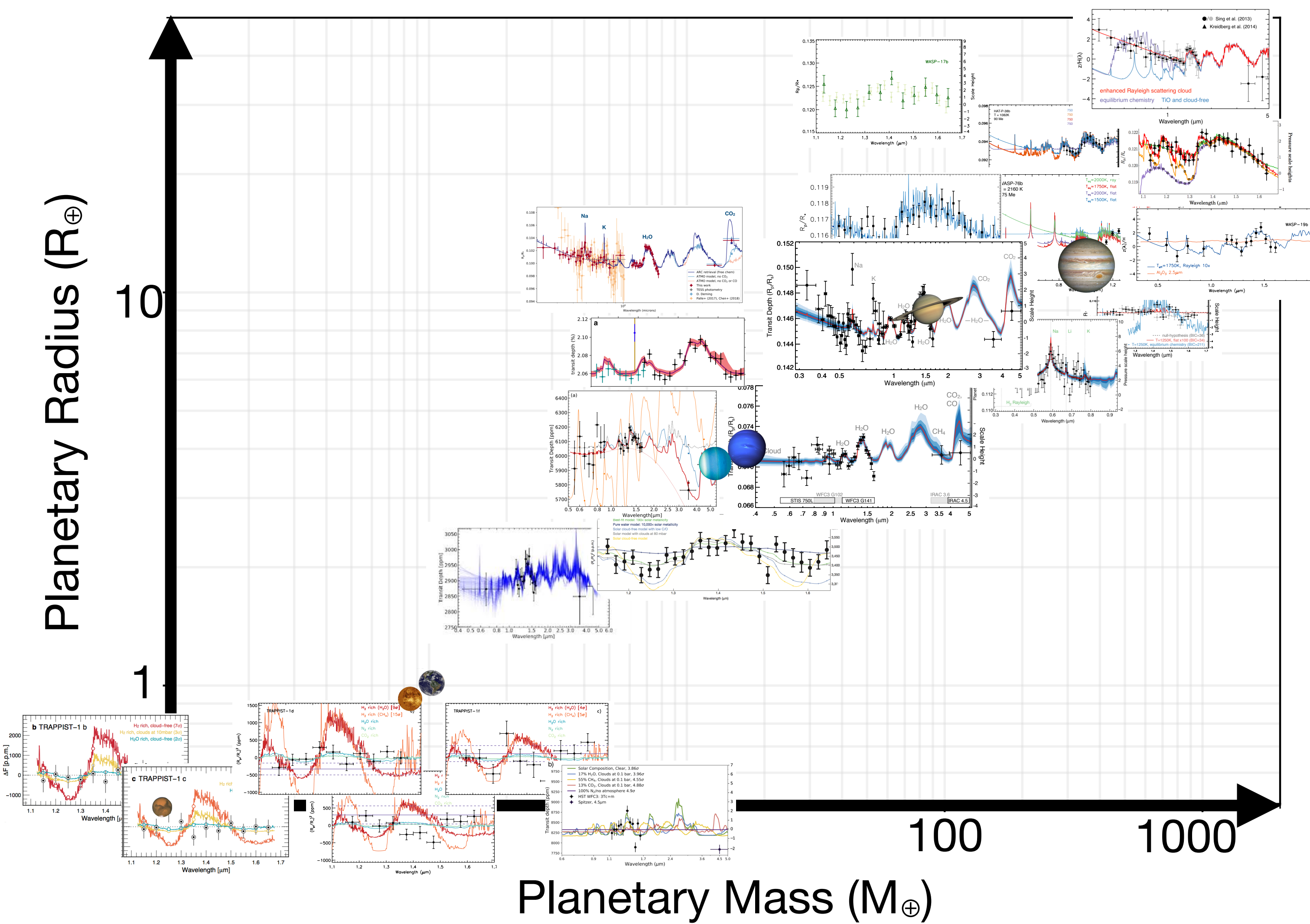


Cloudy with a chance of water

Water vapor has been measured in over 80% of planets



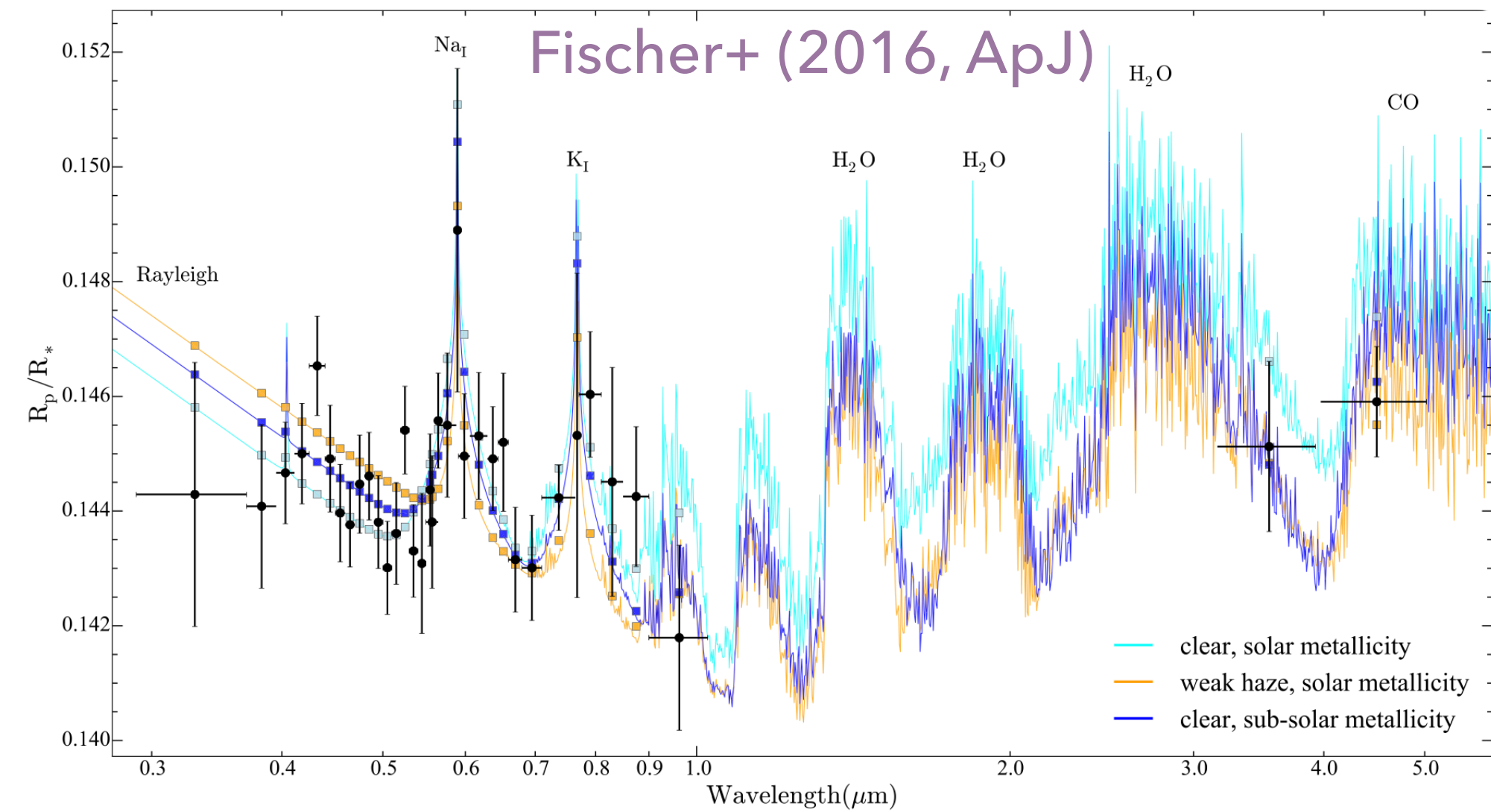
But it is often muted to around 1/3 of expected





# Panchromatic Transmission of WASP-39b

## Previous work and predictions



Clear Na and K features suggest an atmosphere with minimal high altitude cloud opacity

Prediction —> strong H<sub>2</sub>O features in near-IR

**WASP-39b**  
Transiting  
Jupiter-radius Saturn-mass world

**Star**  
0.93 Solar mass  
0.89 Solar Radii

**Planet**  
0.28 Jupiter Mass  
1.27 Jupiter Radii

Distance: 750 light years  
Constellation: Virgo

Period: 4.055 days  
Temperature: 1100 K

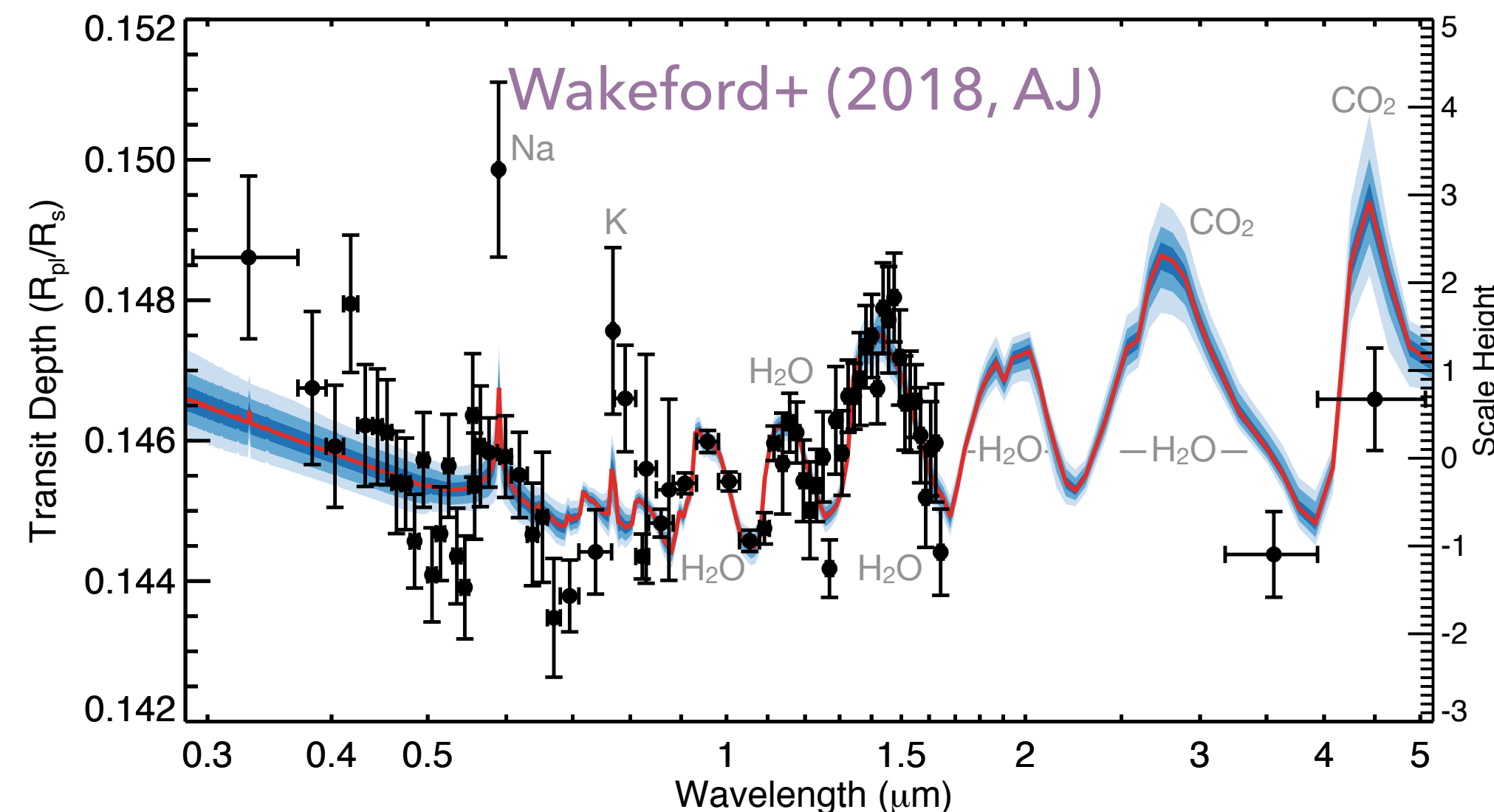
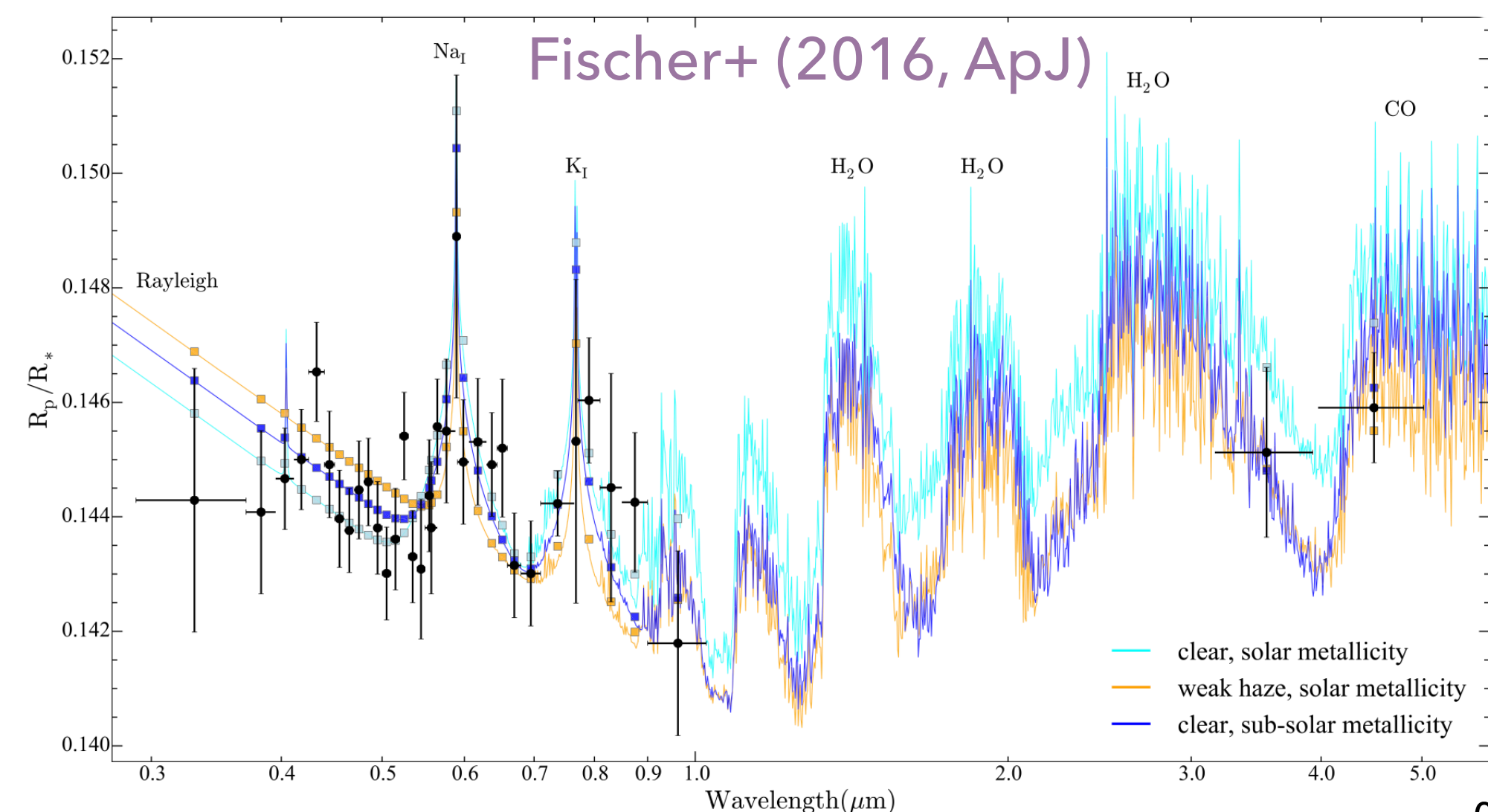
Well studied atmosphere with Hubble, Spitzer, VLT & JWST transmission spectra

exocast.org/exocup2022 @exocastExocup



# Panchromatic Transmission of WASP-39b

## Previous work and predictions



Clear Na and K features suggest an atmosphere with minimal high altitude cloud opacity

Prediction  $\rightarrow$  strong H<sub>2</sub>O features in near-IR

### WASP-39b

Transiting  
*Jupiter-radius Saturn-mass world*

**Star**

- 0.93 Solar mass
- 0.89 Solar Radii

**Planet**

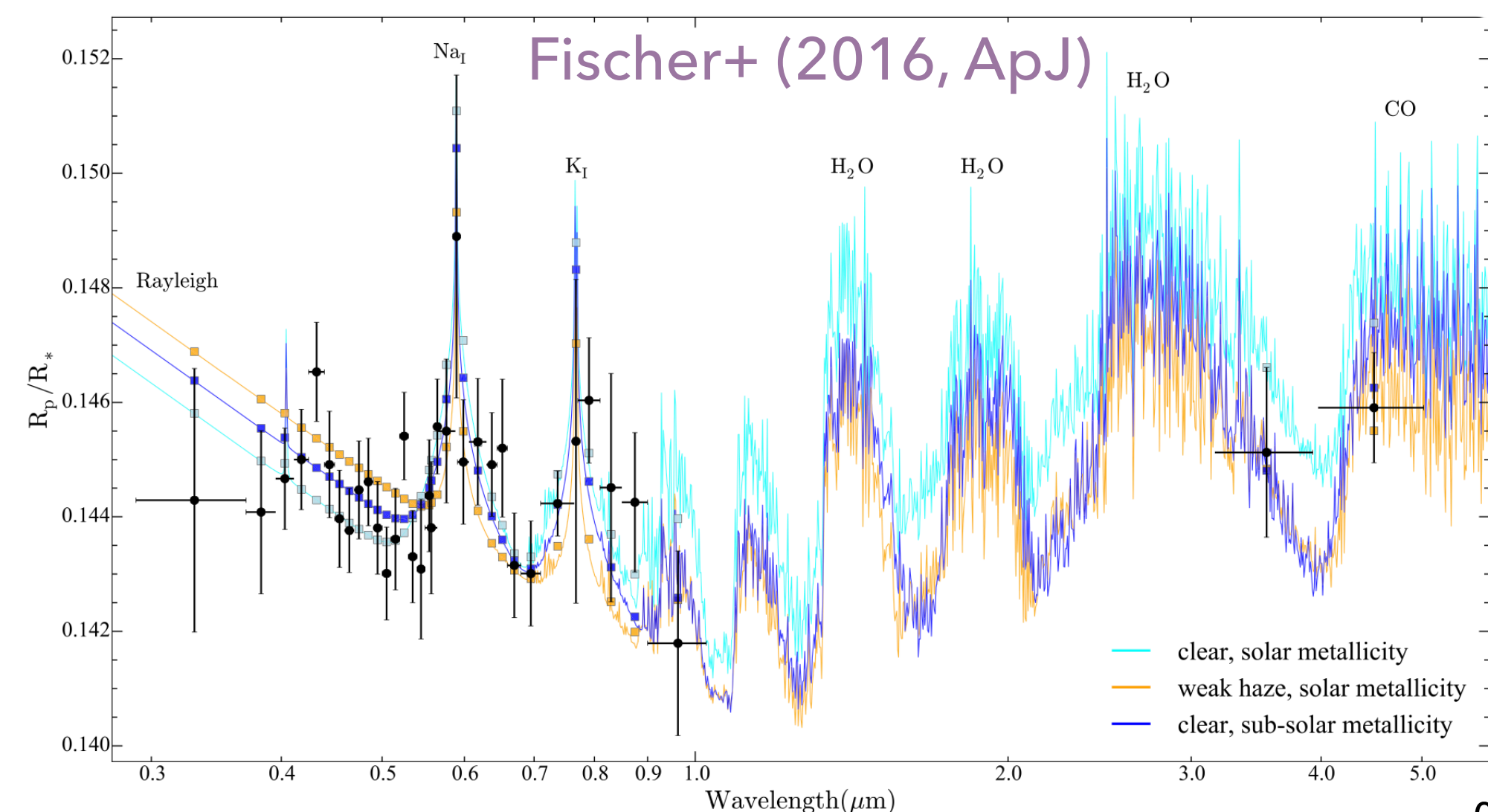
- 0.28 Jupiter Mass
- 1.27 Jupiter Radii
- Distance: 750 light years
- Constellation: Virgo
- Period: 4.055 days
- Temperature: 1100 K
- Well studied atmosphere with Hubble, Spitzer, VLT & JWST transmission spectra

[exocast.org/exocup2022](http://exocast.org/exocup2022)
 @exocastExocup



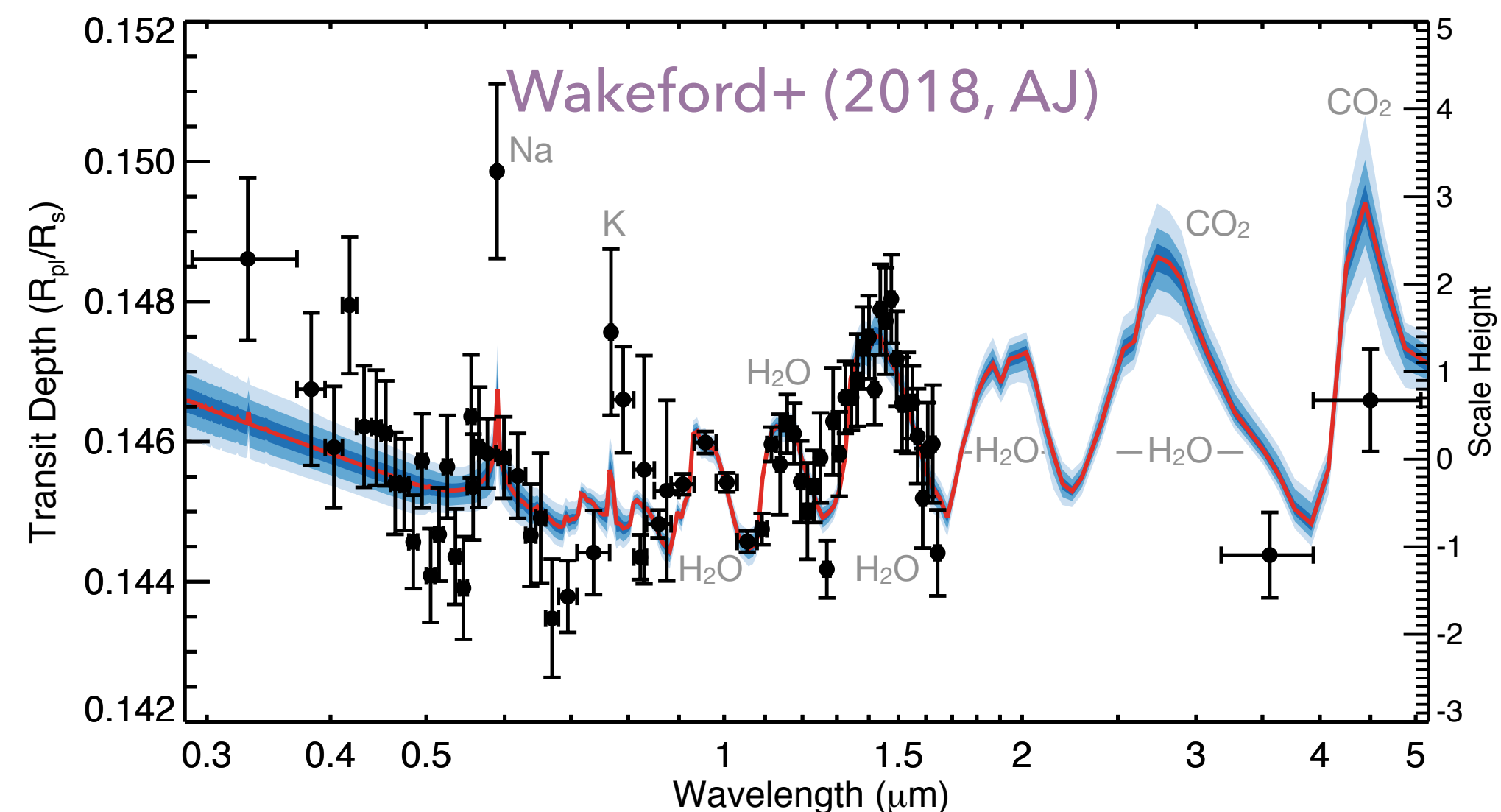
# Panchromatic Transmission of WASP-39b

## Previous work and predictions



HST/WFC3 IR grisms show three distinct H<sub>2</sub>O absorption features with indication of super solar metallicity

Prediction —> strong absorption by CO<sub>2</sub> in the IR with JWST



Clear Na and K features suggest an atmosphere with minimal high altitude cloud opacity

Prediction —> strong H<sub>2</sub>O features in near-IR

### WASP-39b

Transiting  
 Jupiter-radius Saturn-mass world

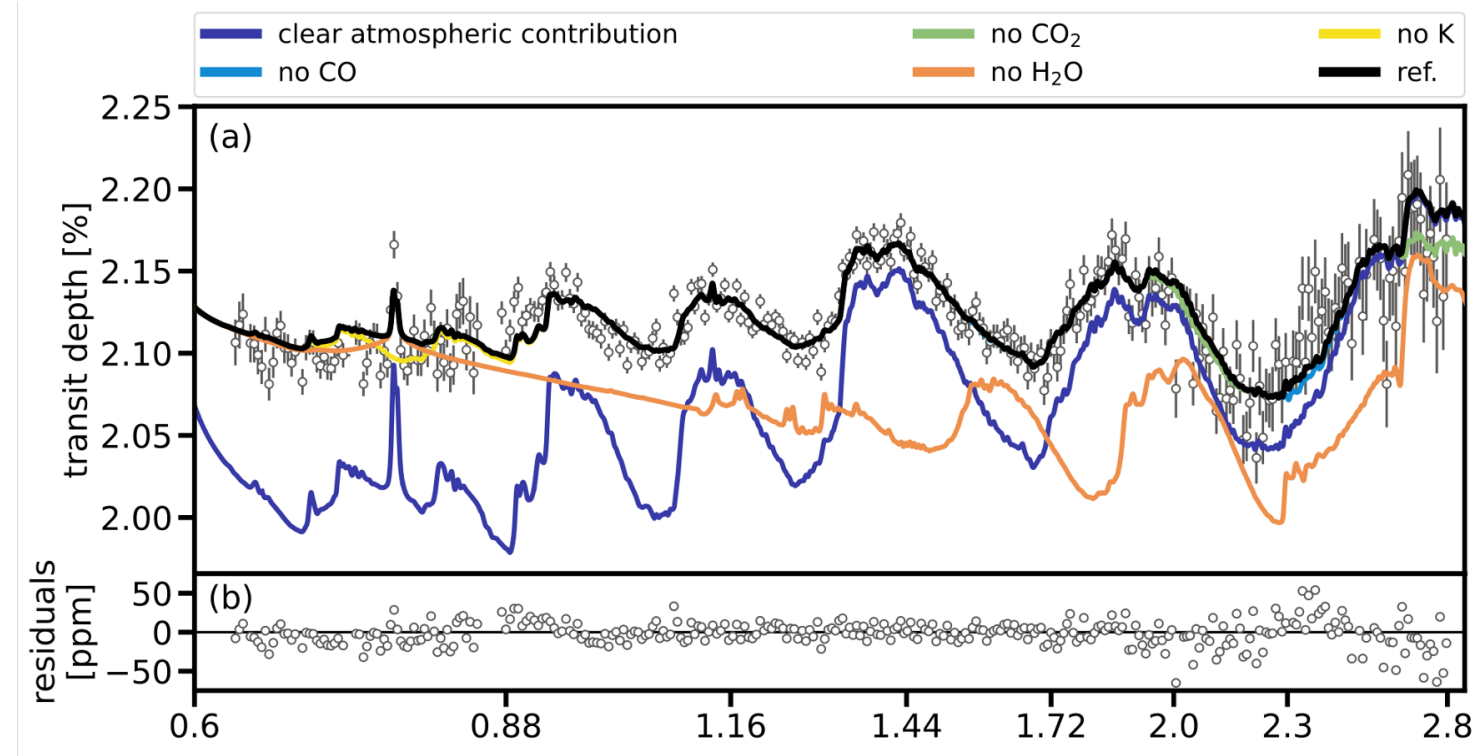
<b>Star</b>	0.93 Solar mass 0.89 Solar Radii
<b>Planet</b>	0.28 Jupiter Mass 1.27 Jupiter Radii
	Distance: 750 light years Constellation: Virgo
	Period: 4.055 days Temperature: 1100 K
	Well studied atmosphere with Hubble, Spitzer, VLT & JWST transmission spectra

[exocast.org/exocup2022](http://exocast.org/exocup2022)
 @exocastExocup

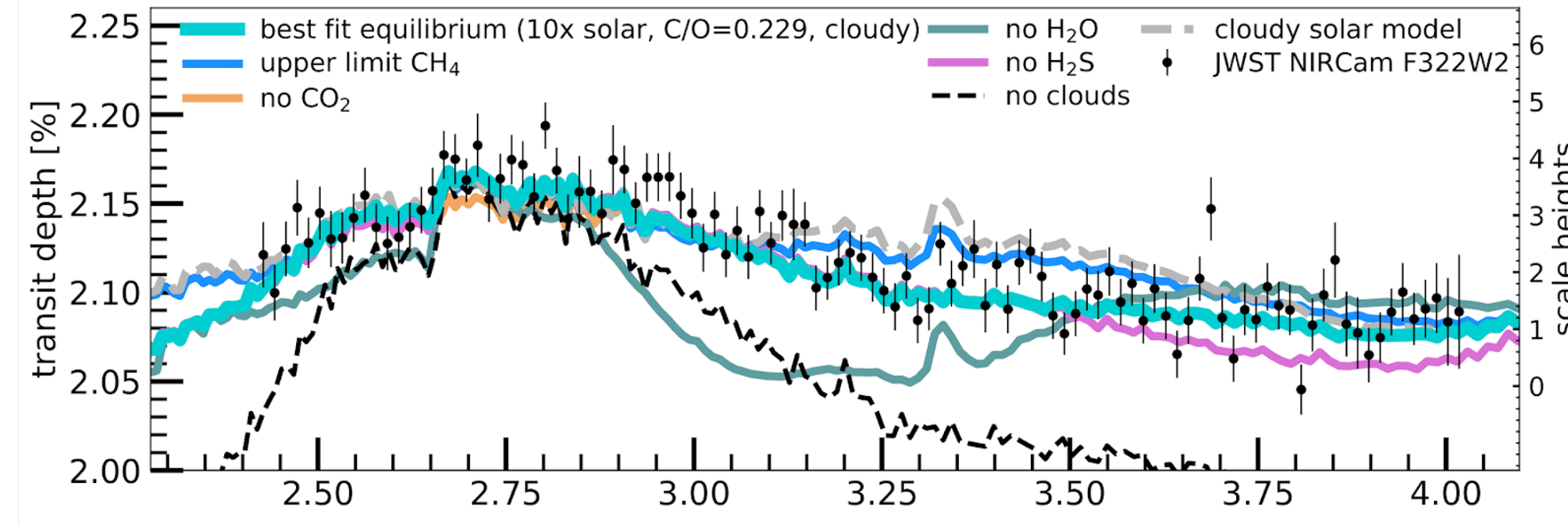


# WASP-39b Panchromatic Transmission Spectrum

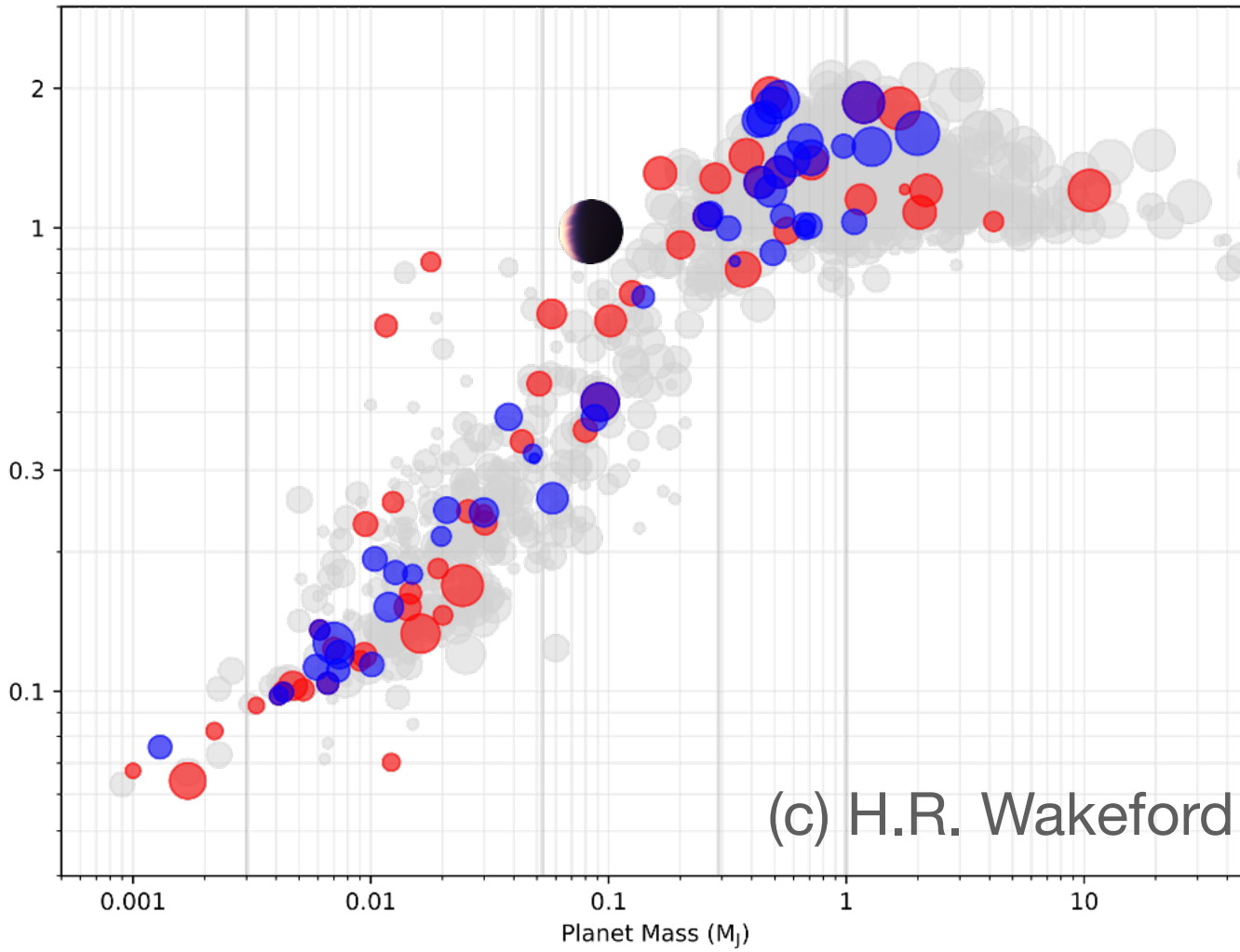
ERS 1366 Transiting Exoplanet Community ERS Program



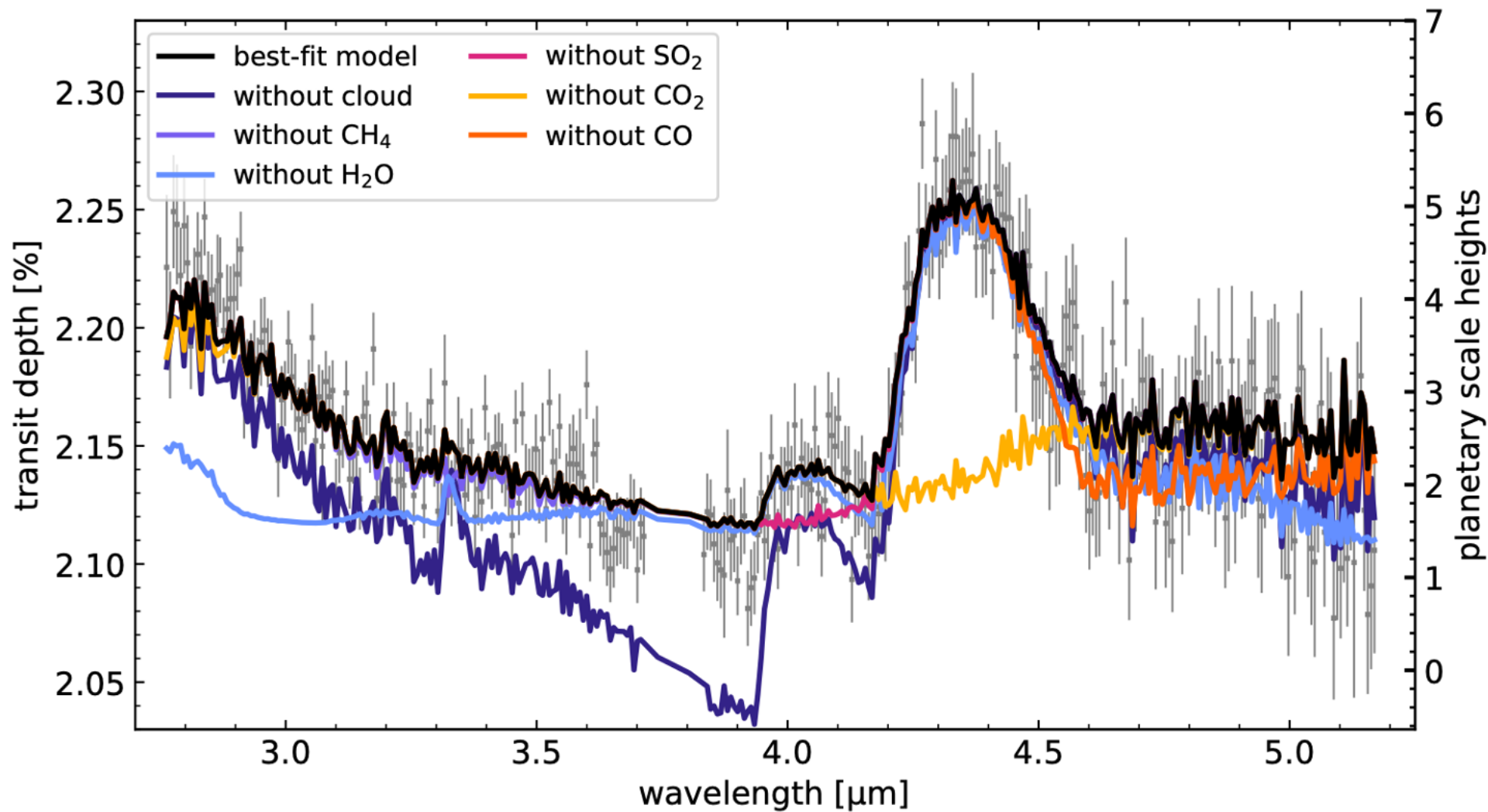
Feinstein, Radica+ (2023, Nature)



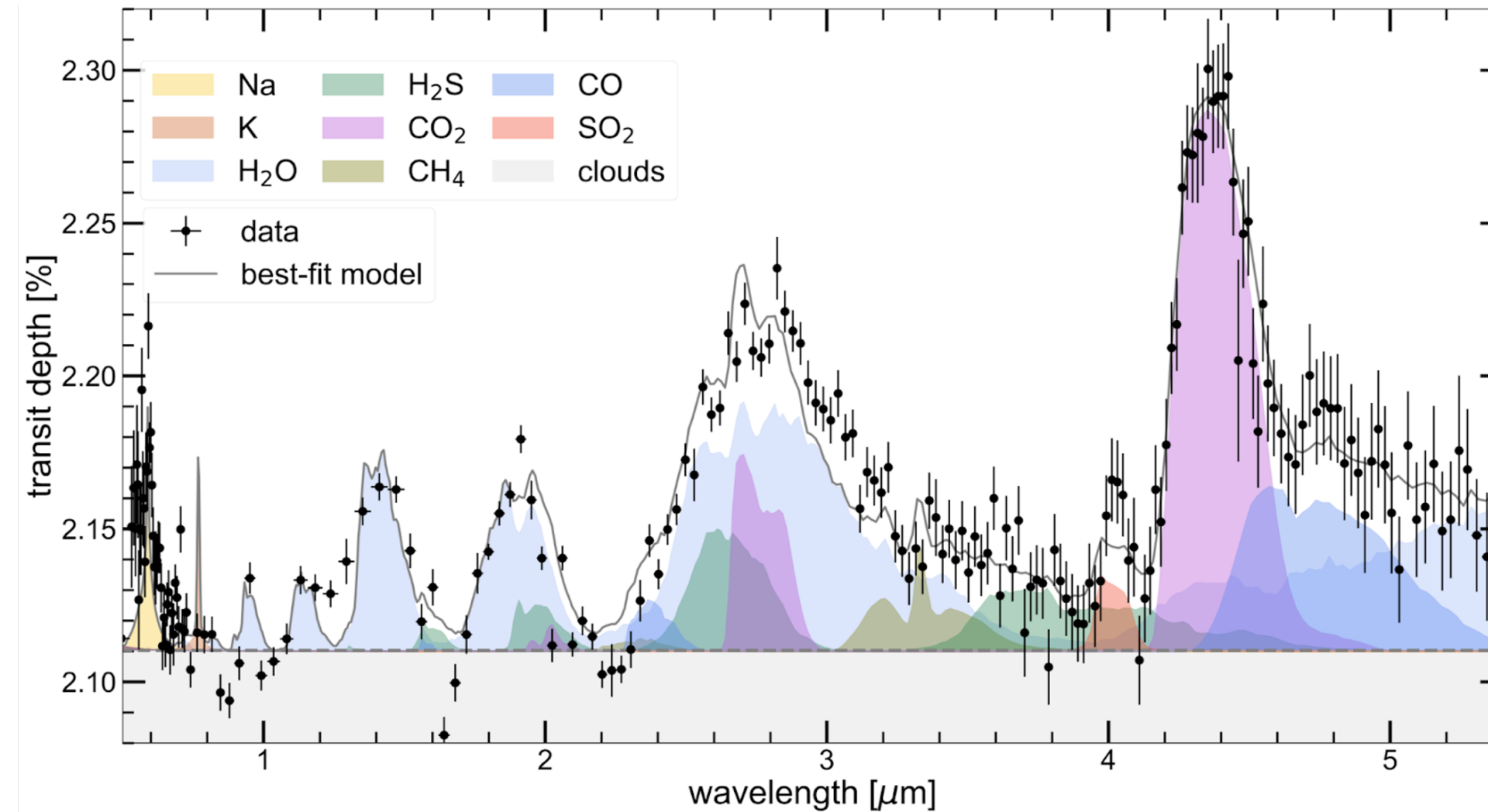
Ahrer, Stevenson+ (2023, Nature)



(c) H.R. Wakeford



Alderson, Wakeford+ (2023, Nature)



Rustamkulov, Sing+ (2023, Nature)

Spectrum from 0.6 – 5.2 μm

- Detection of K, H<sub>2</sub>O, CO<sub>2</sub>, CO, SO<sub>2</sub>, aerosol opacity
- [M/H] > solar
- C/O < solar



# ERS Panchromatic Transmission of WASP-39b

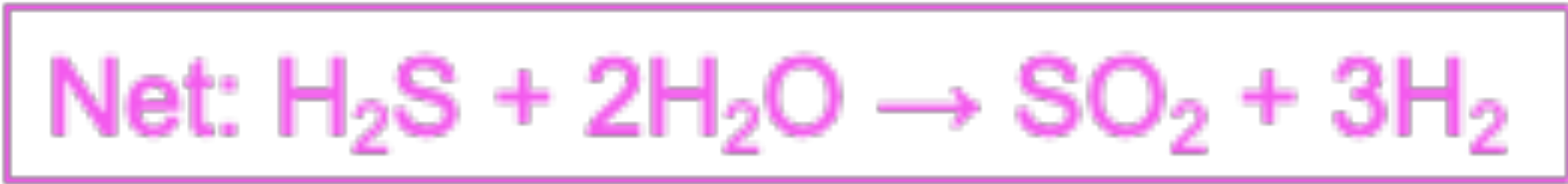
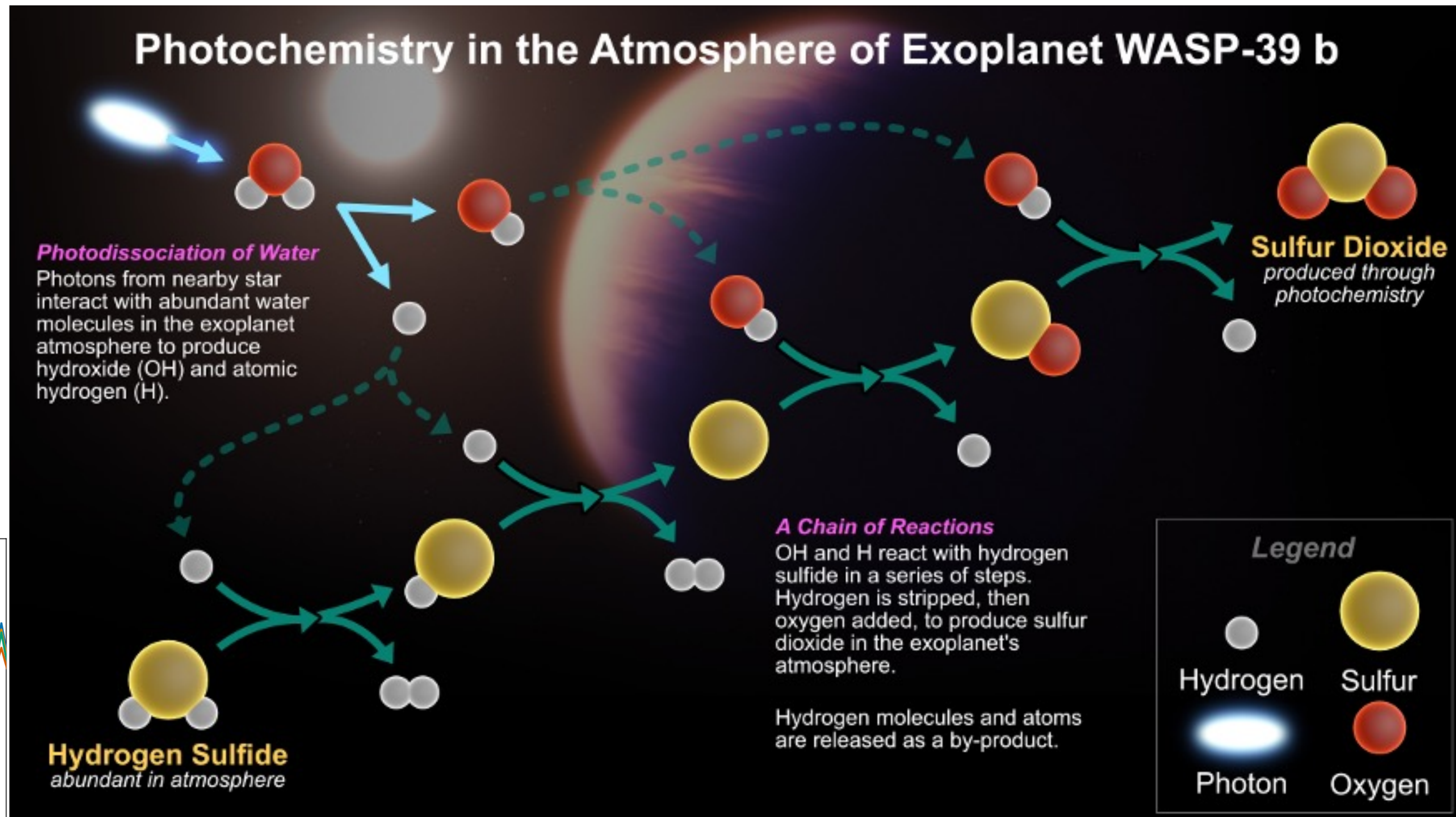
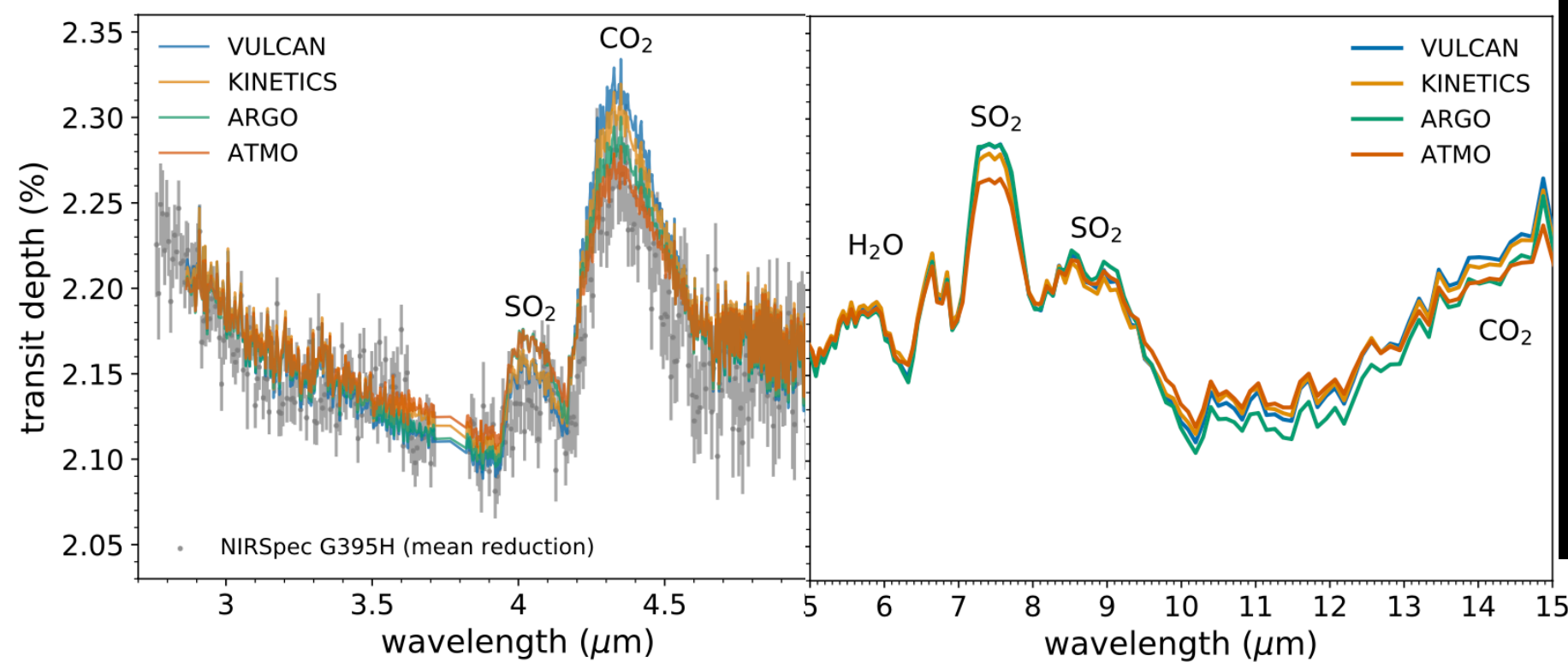
## Discovery of SO<sub>2</sub> photochemistry in the atmosphere of WASP-39b



### Developed the SO<sub>2</sub> chemical pathway

Confirm SO<sub>2</sub> absorption at 2.6σ in PRISM data & 4.5σ in G395H data  
Stronger signatures of SO<sub>2</sub> are expected with MIRI

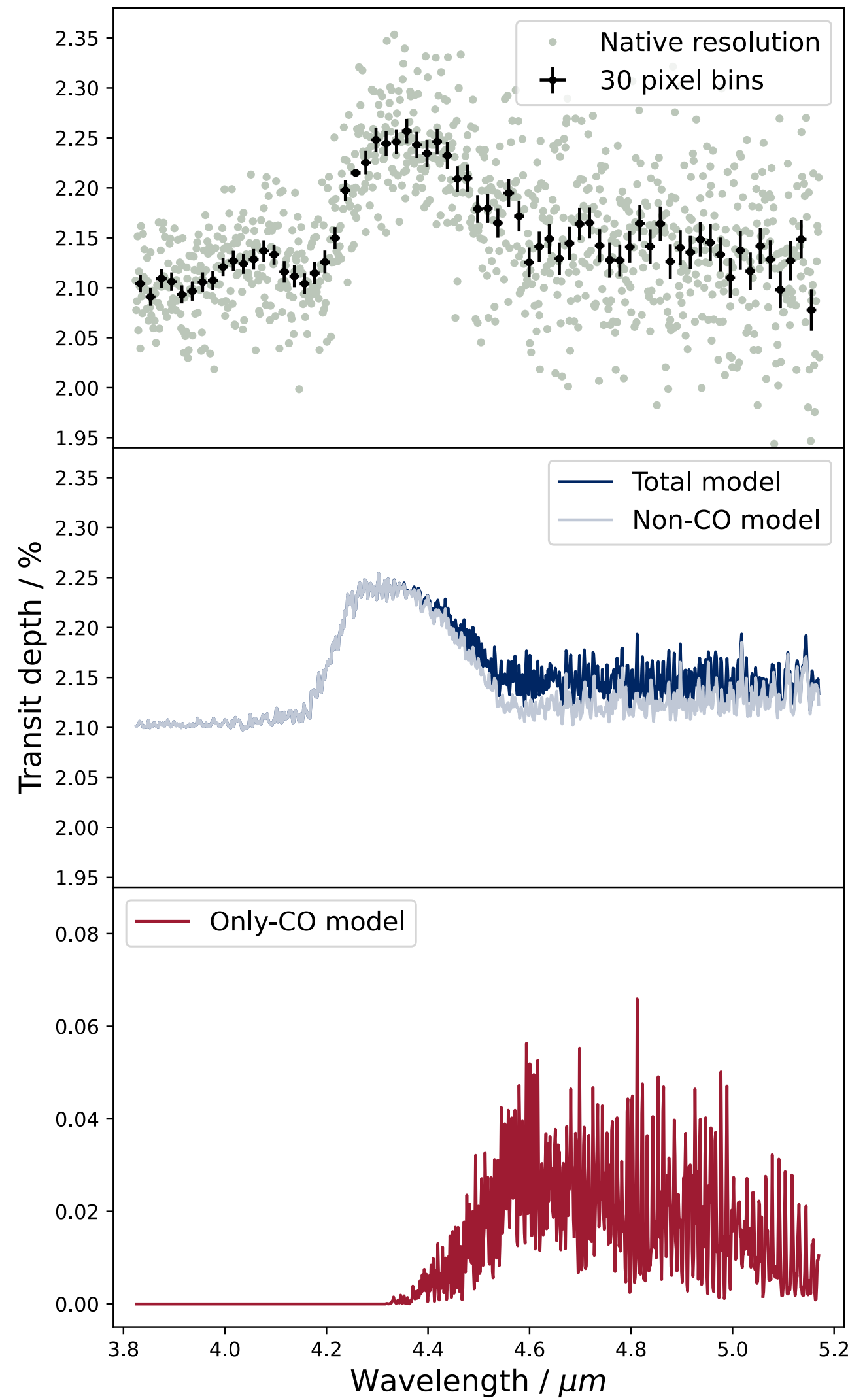
Tsai, Lee et al. 2023, Nature



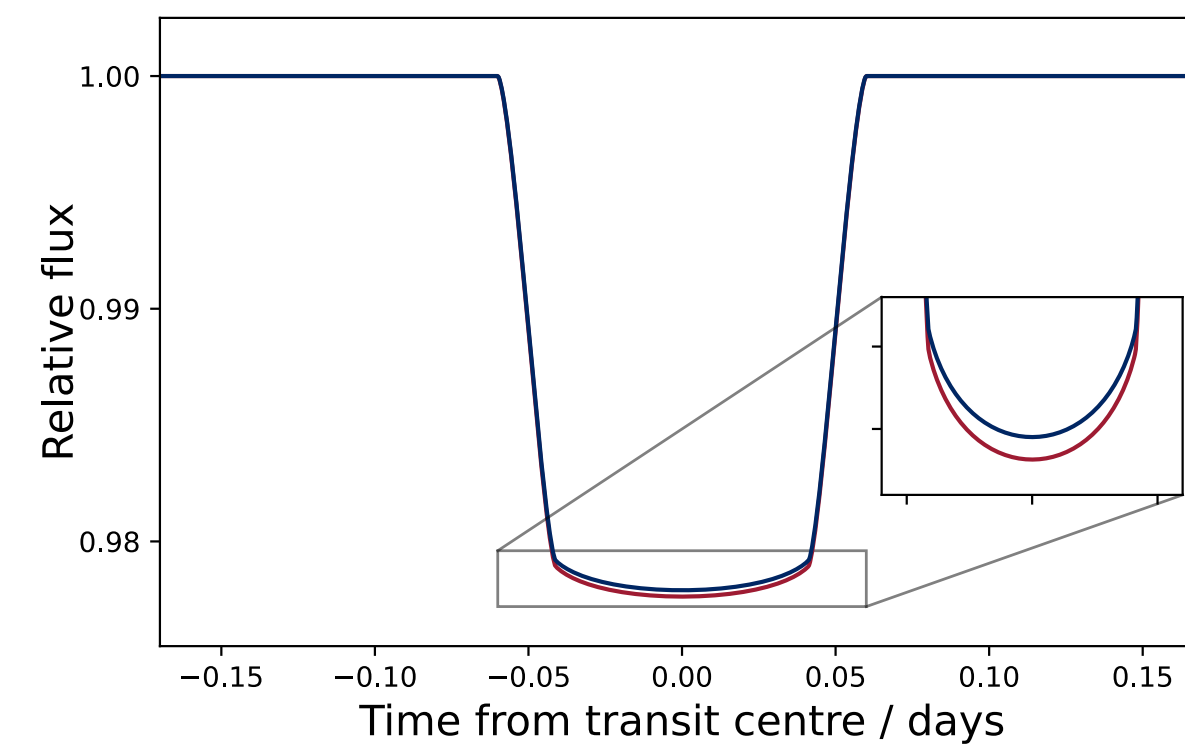
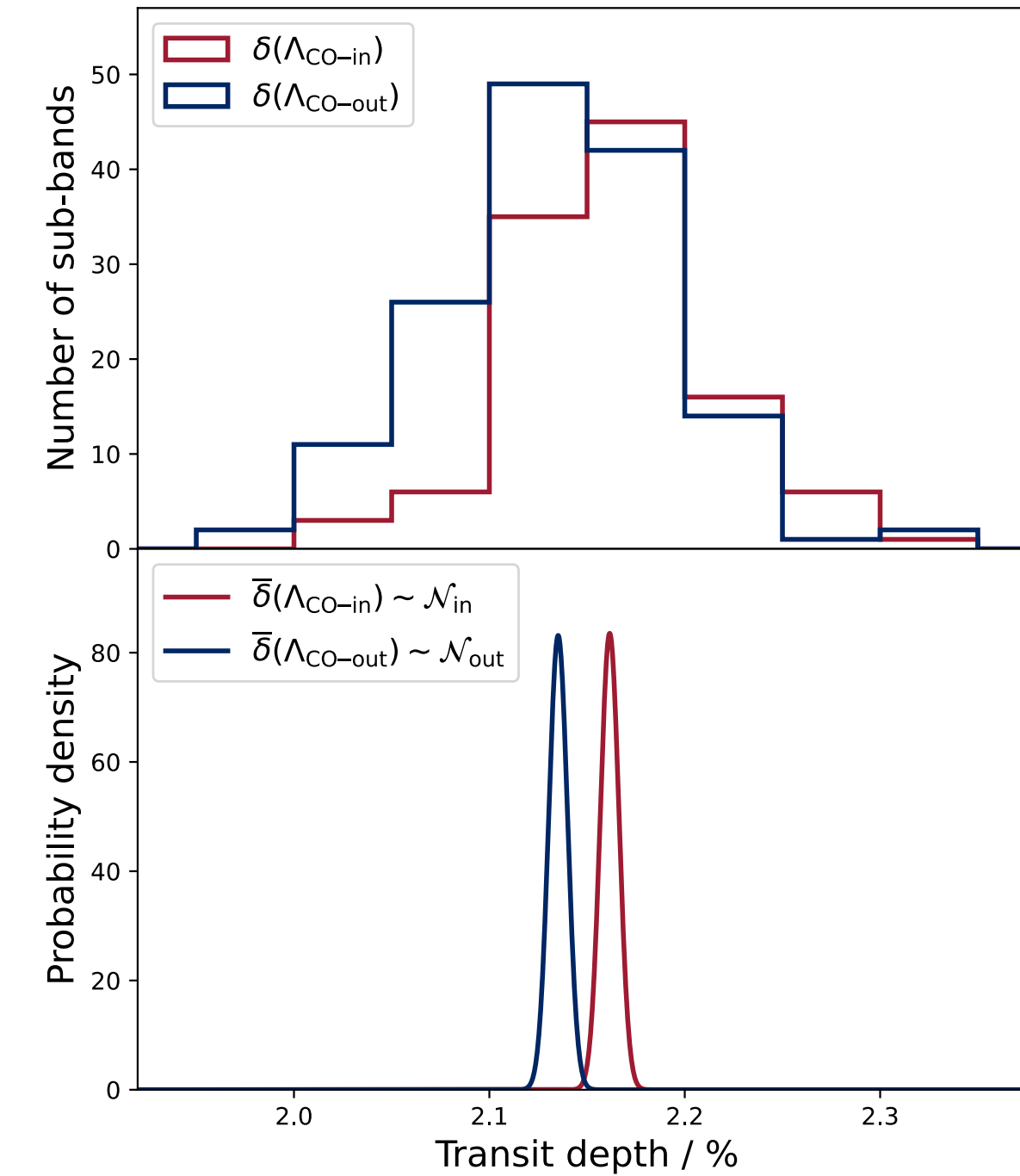
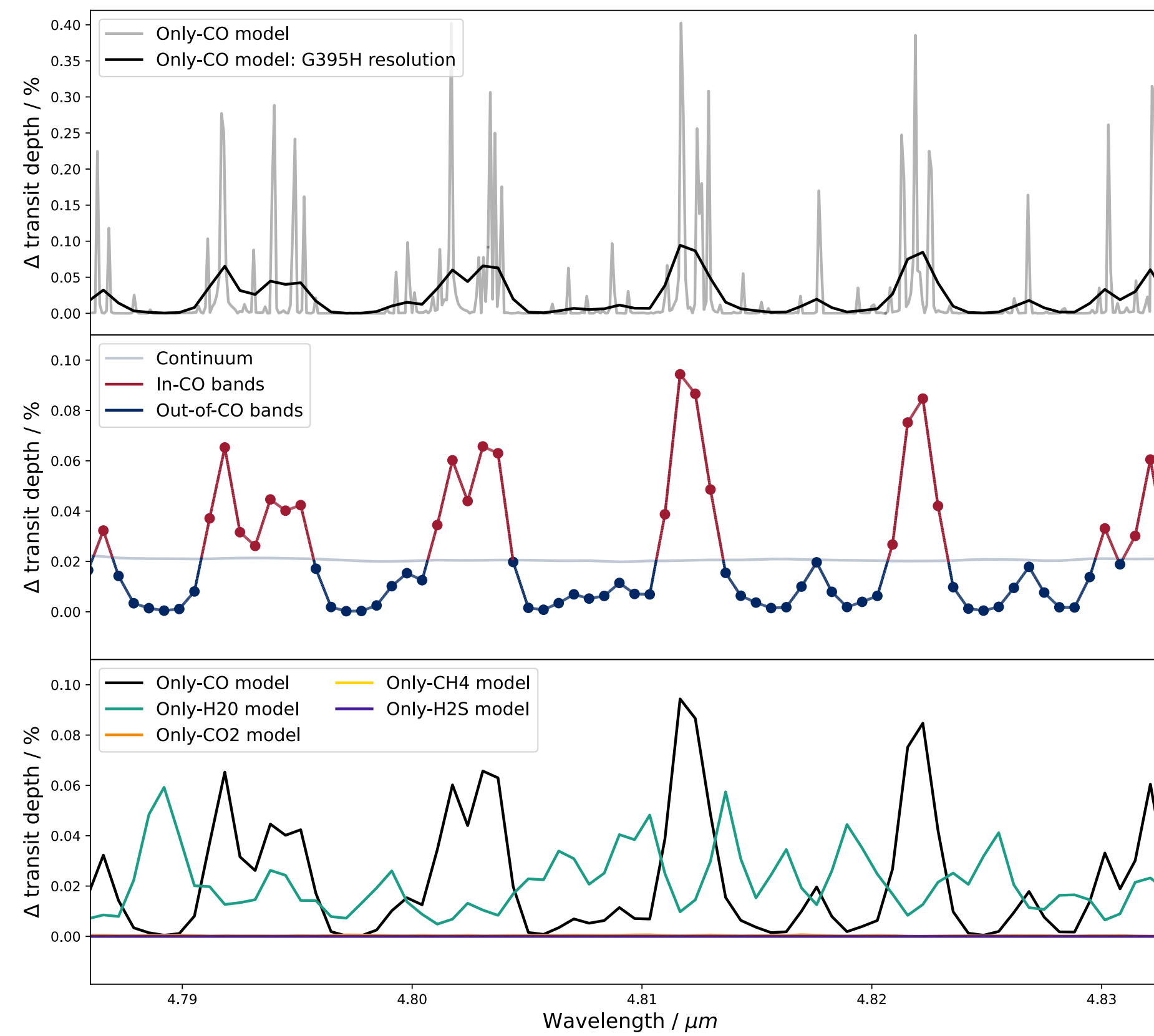


# Panchromatic Transmission of WASP-39b [Ancillary]

## NIRSpec/G395H High-Resolution CO



Ar R~2700 we detect a  $264 \pm 68$  ppm signal of the CO fundamental band structure

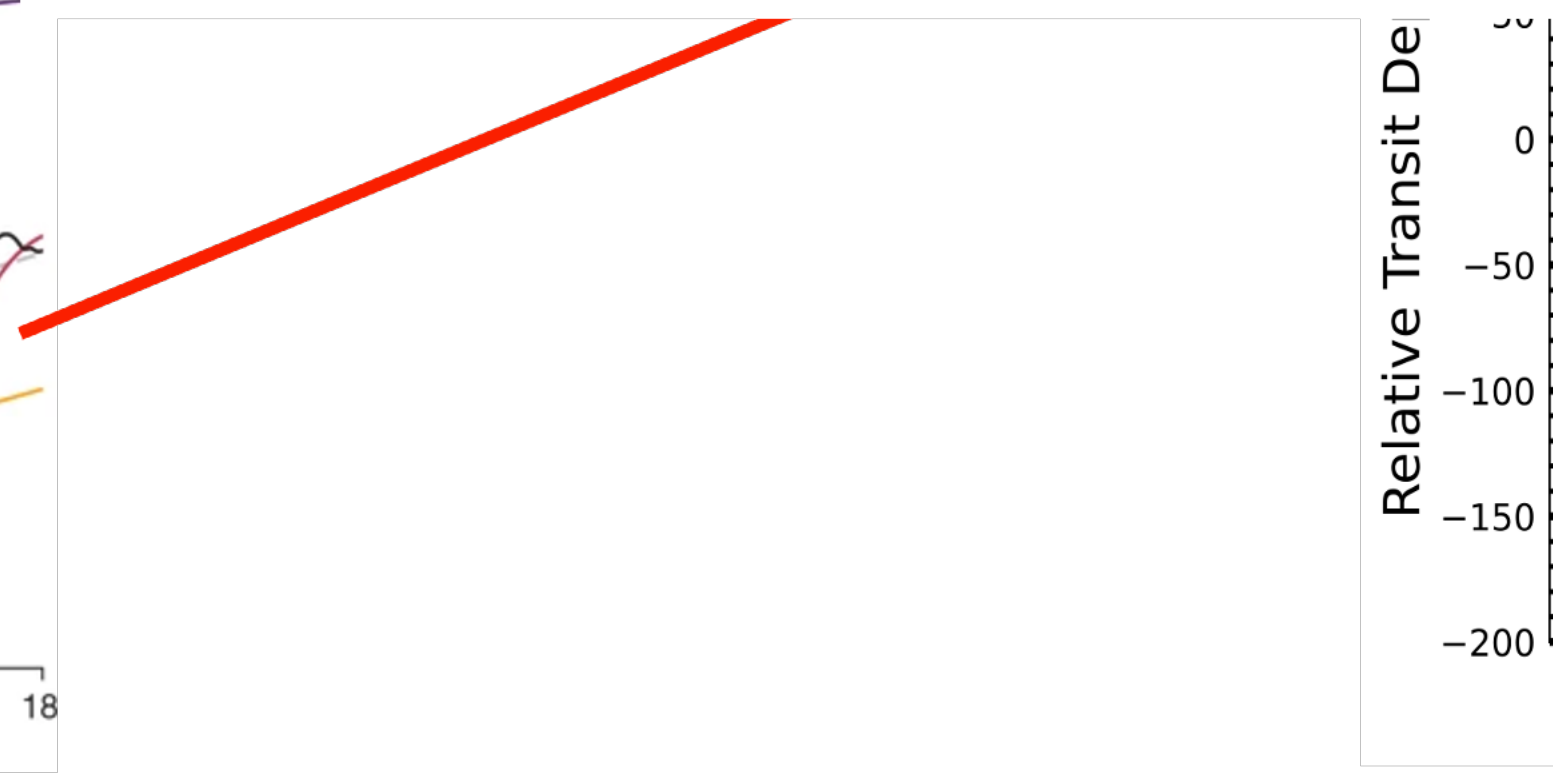
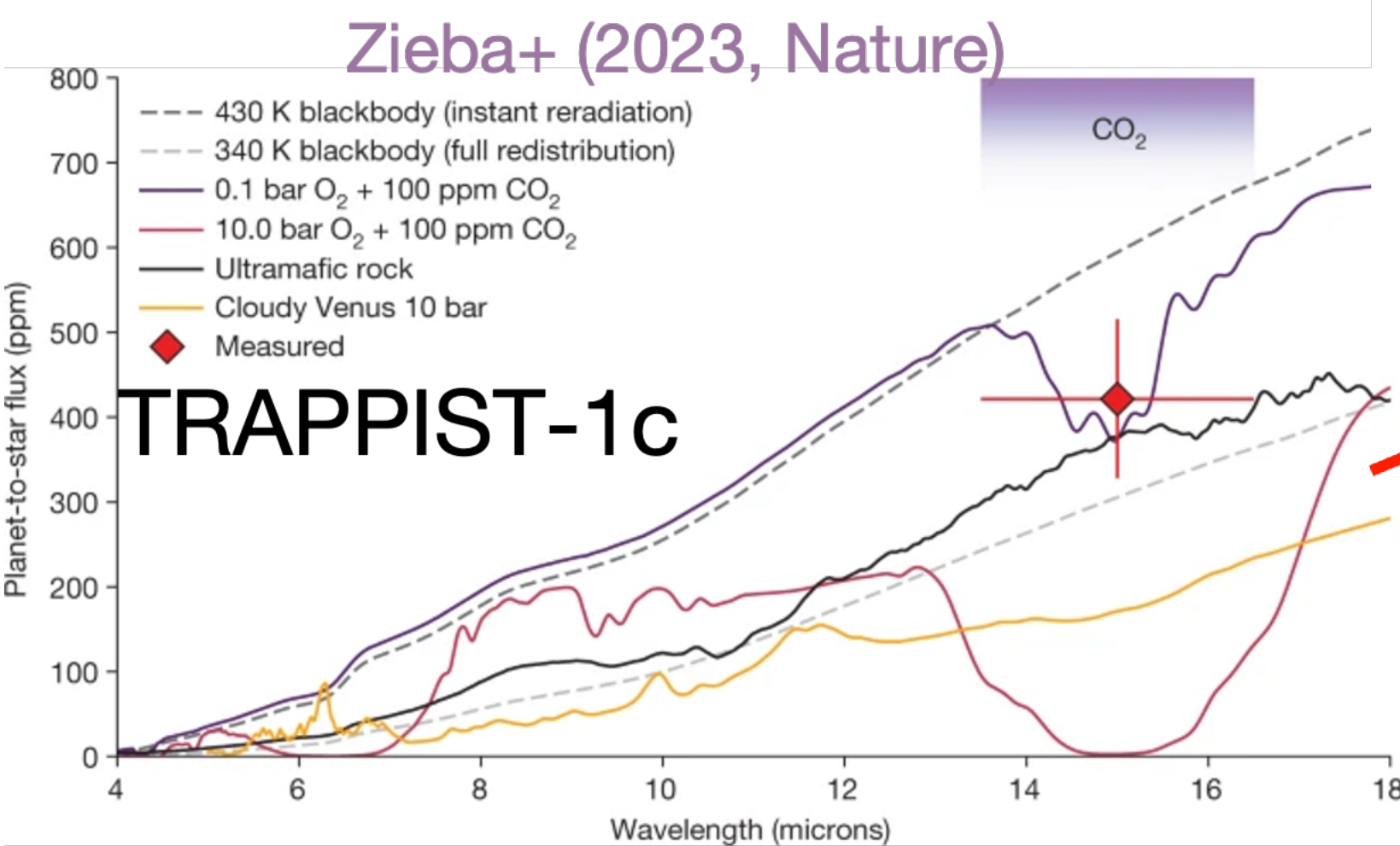
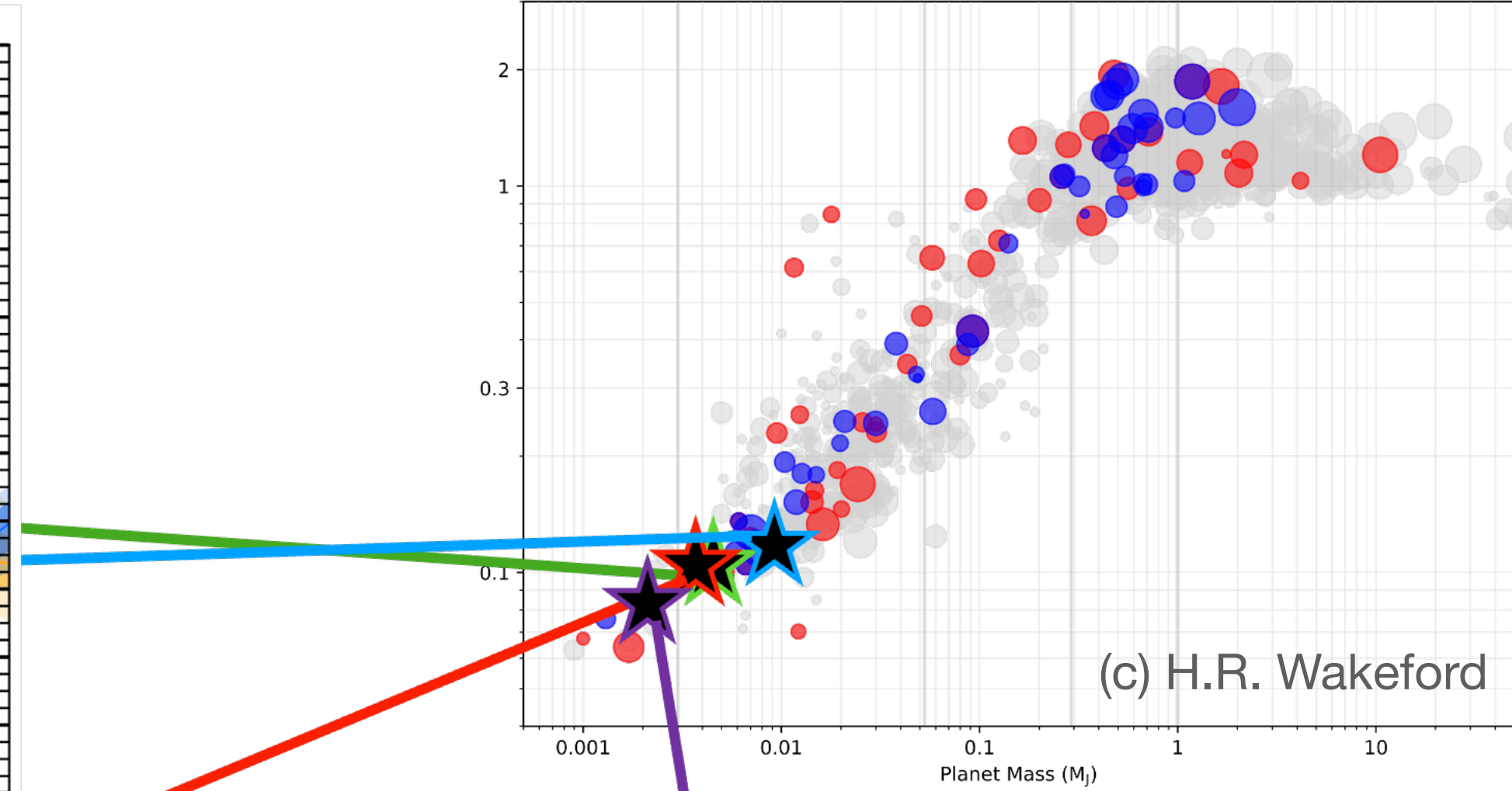
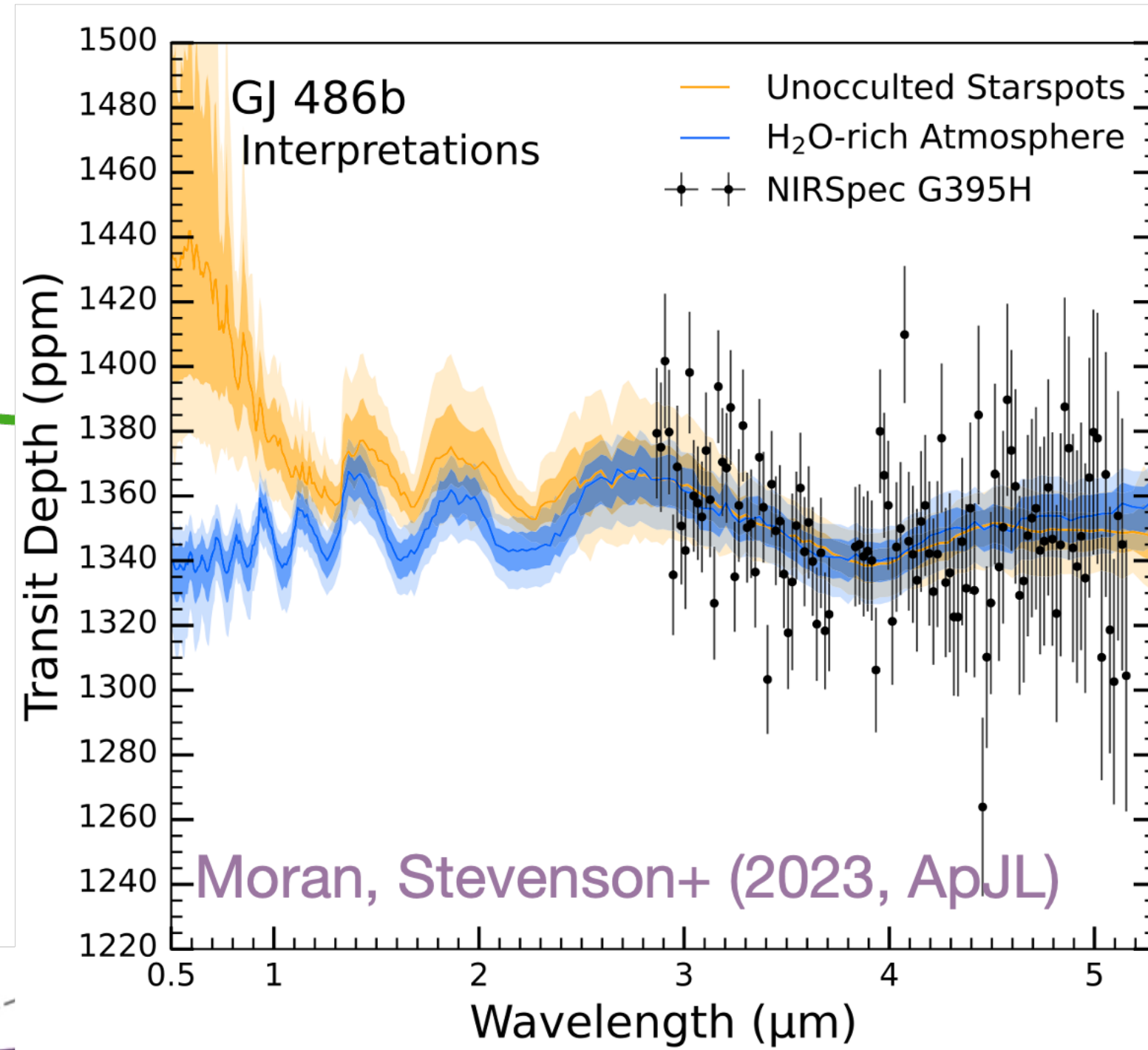
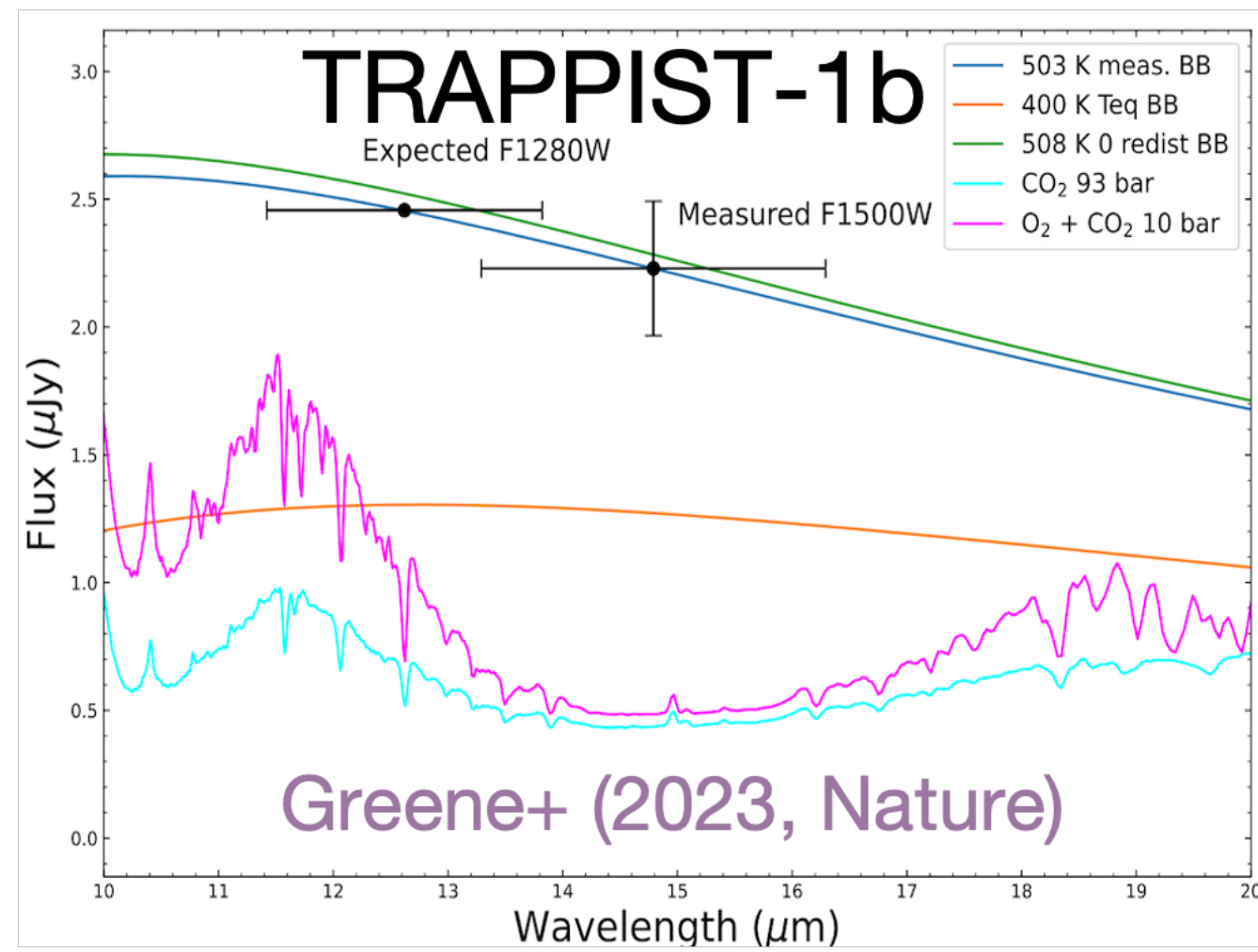


[Grant, Lothringer et al. 2023, ApJL]



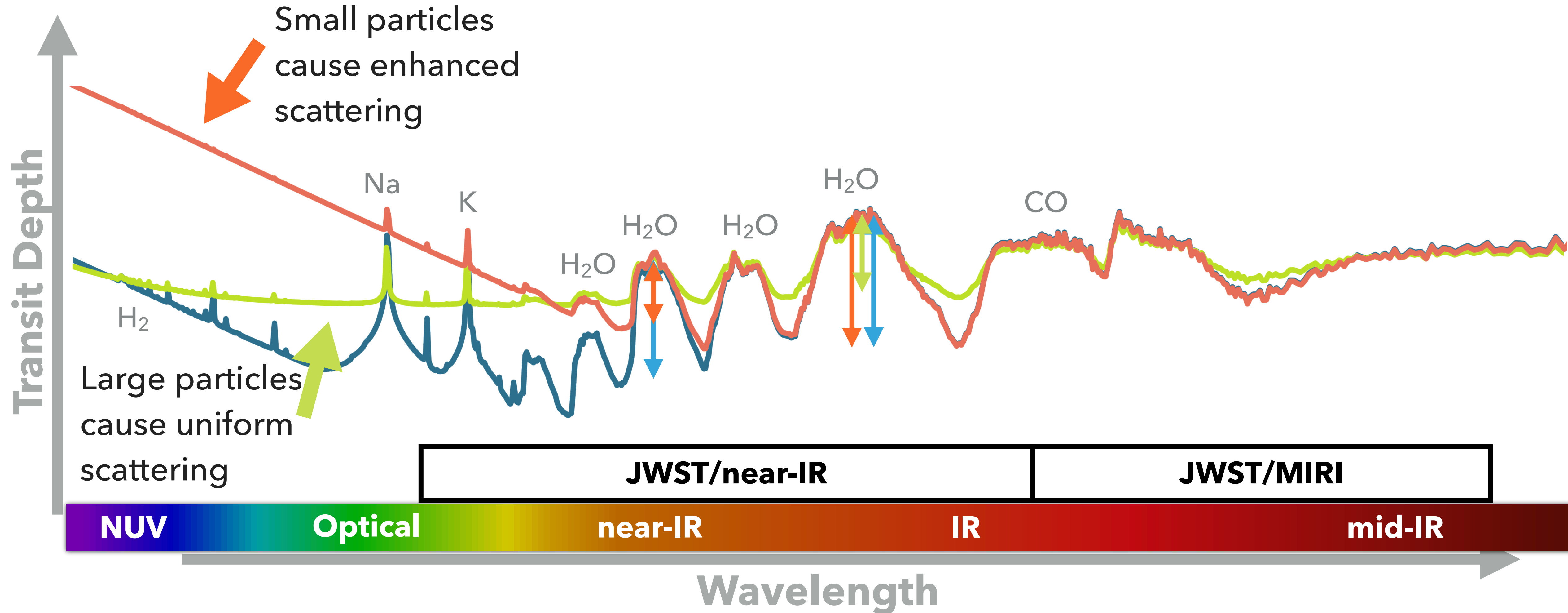
# Atmospheric Scale Height

Height at which pressure decreases by a factor of e (exponent)



# Transiting Exoplanet Atmospheres

How do we measure the atmosphere of a transiting exoplanet?



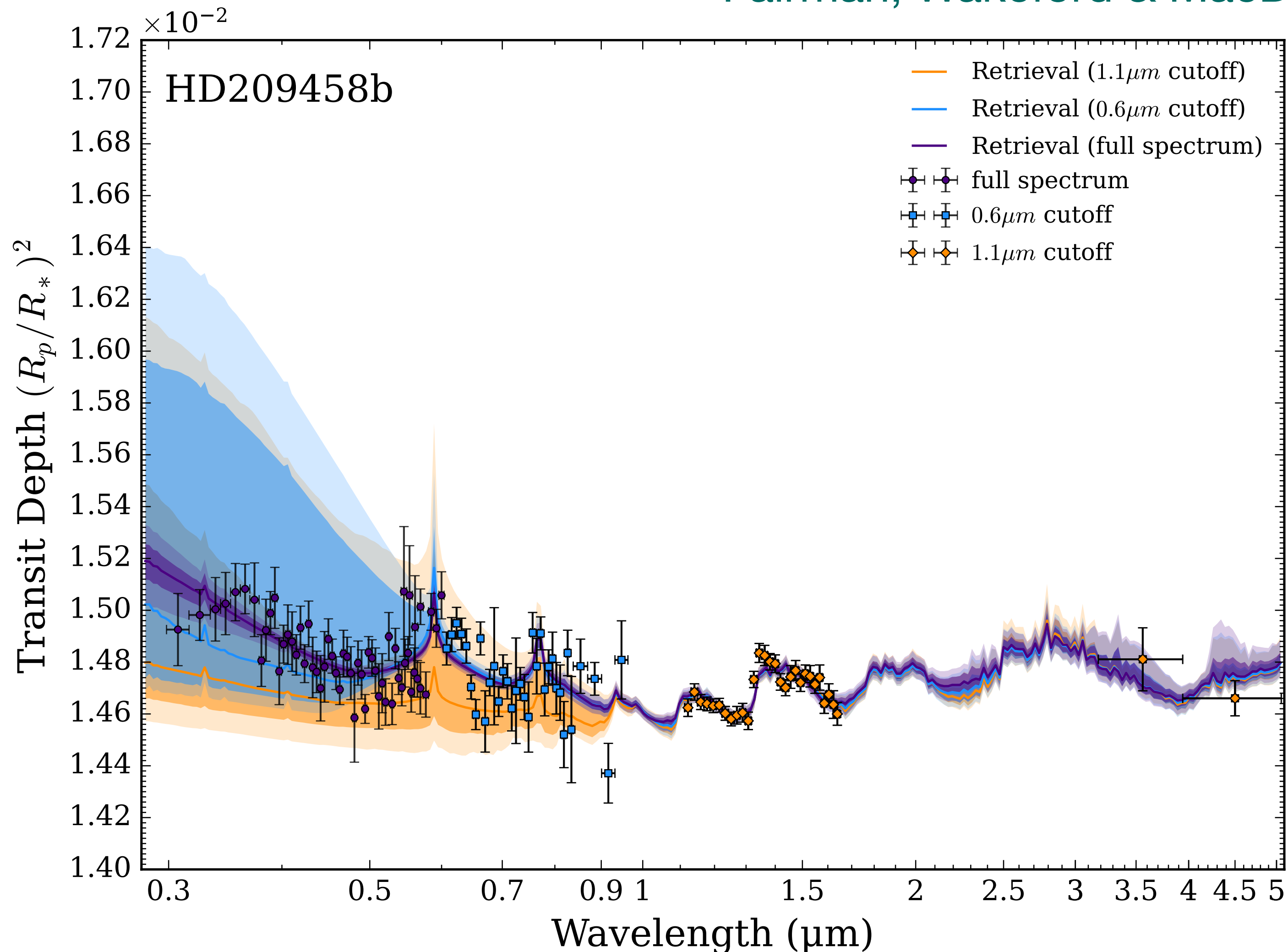


# Evaluate the impact of exoplanet aerosols

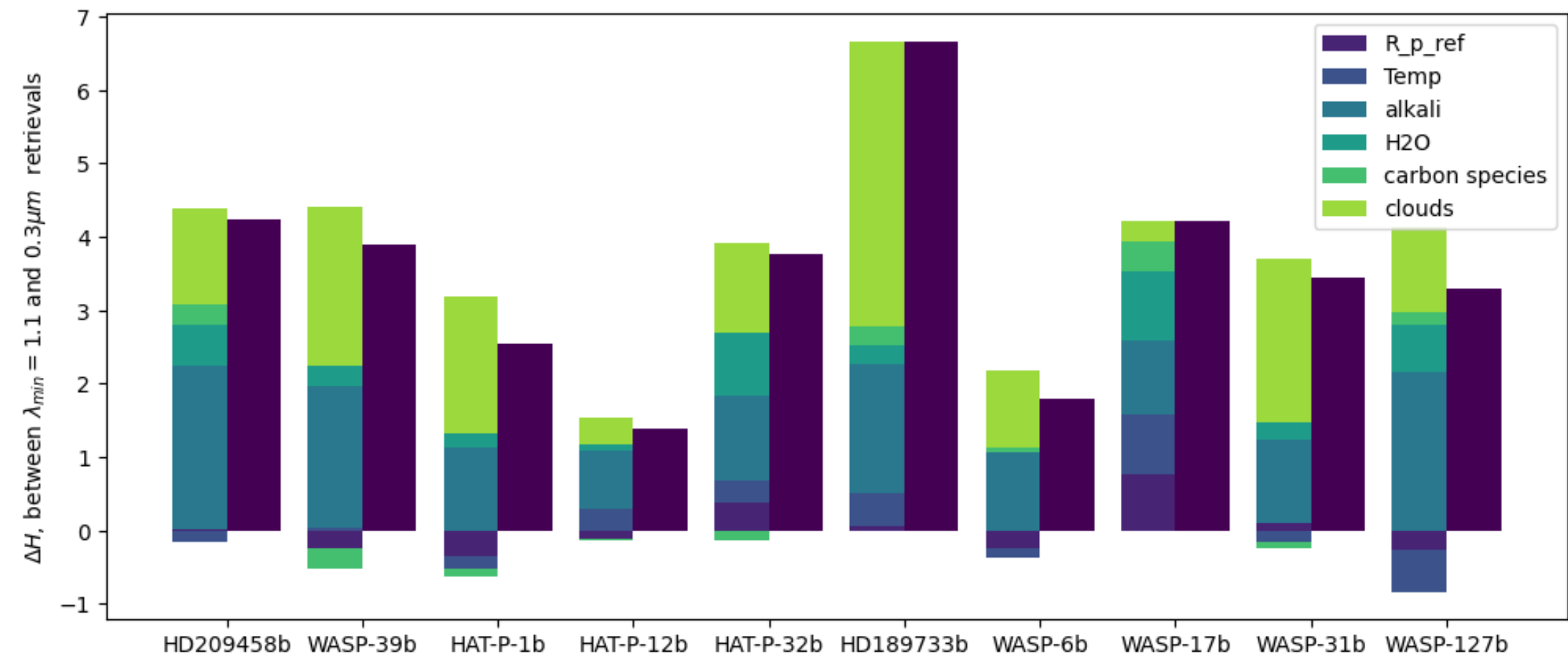


The UV-Optical will play a core role in assessing aerosols in exoplanet spectra

Fairman, Wakeford & MacDonald (in prep)

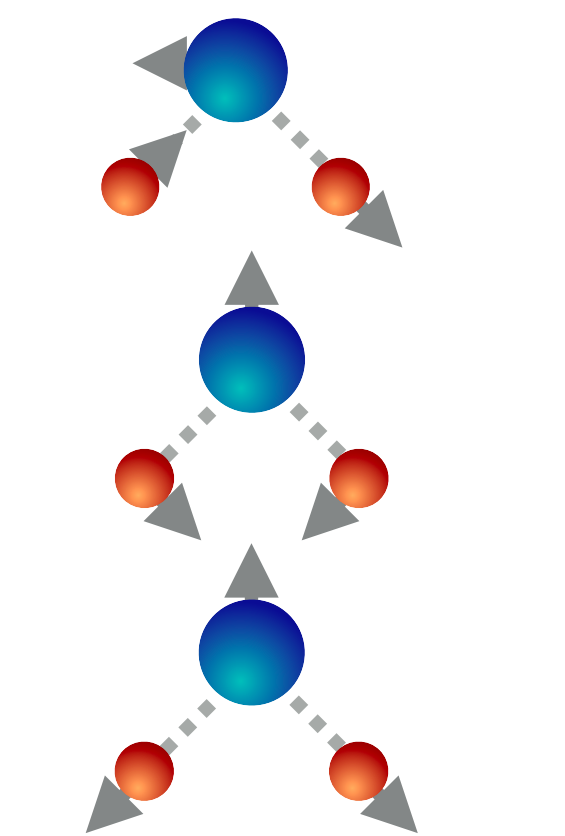
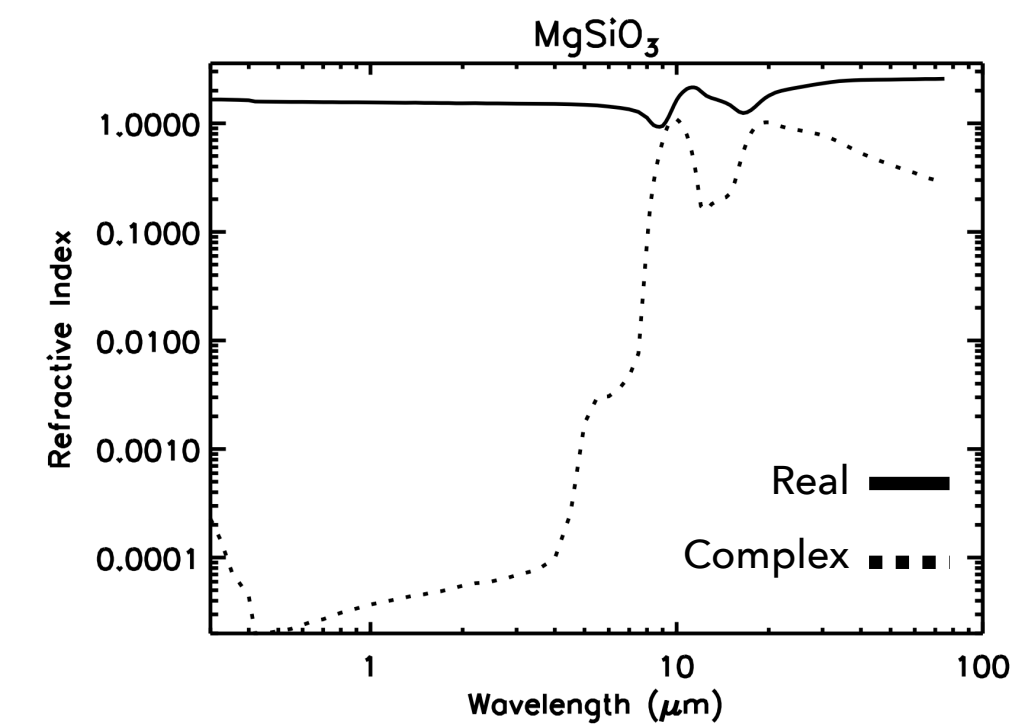
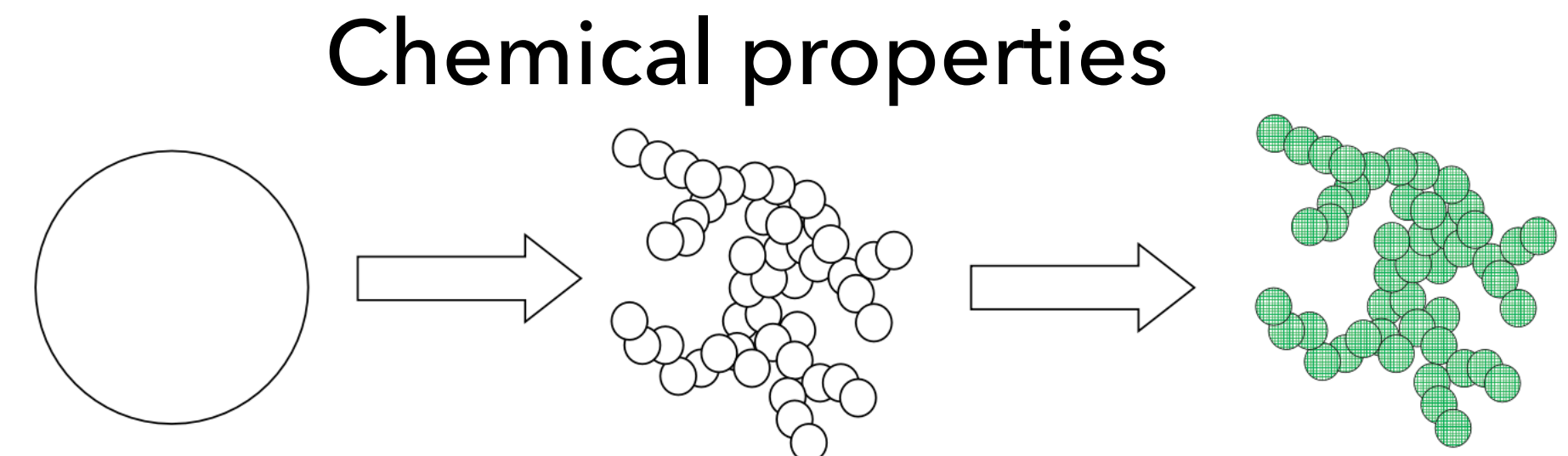
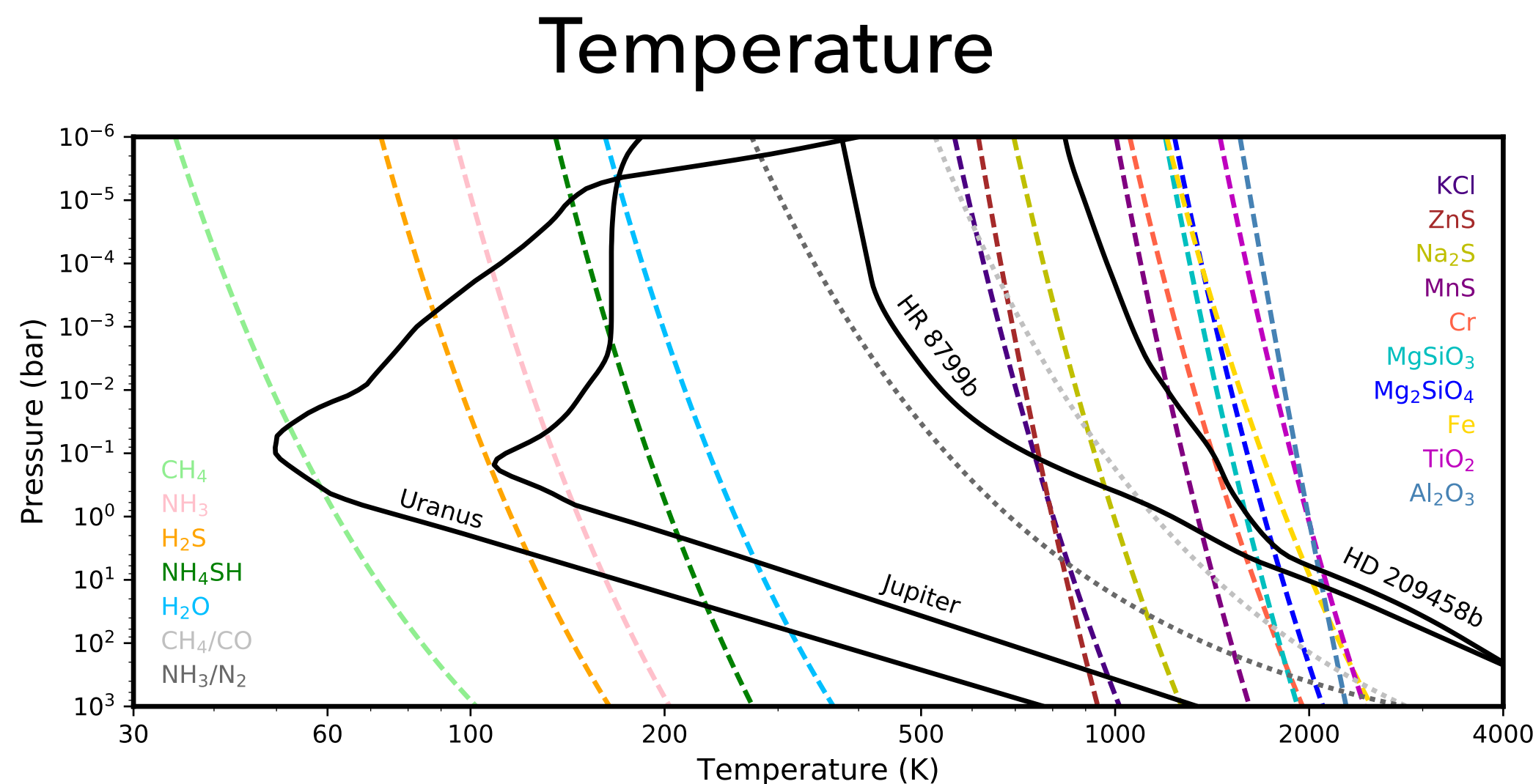
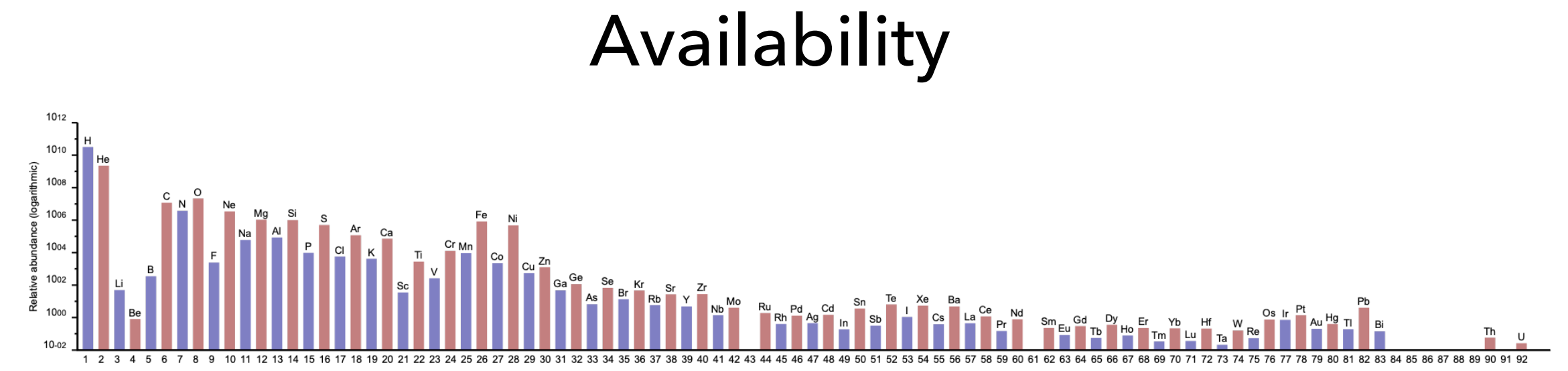
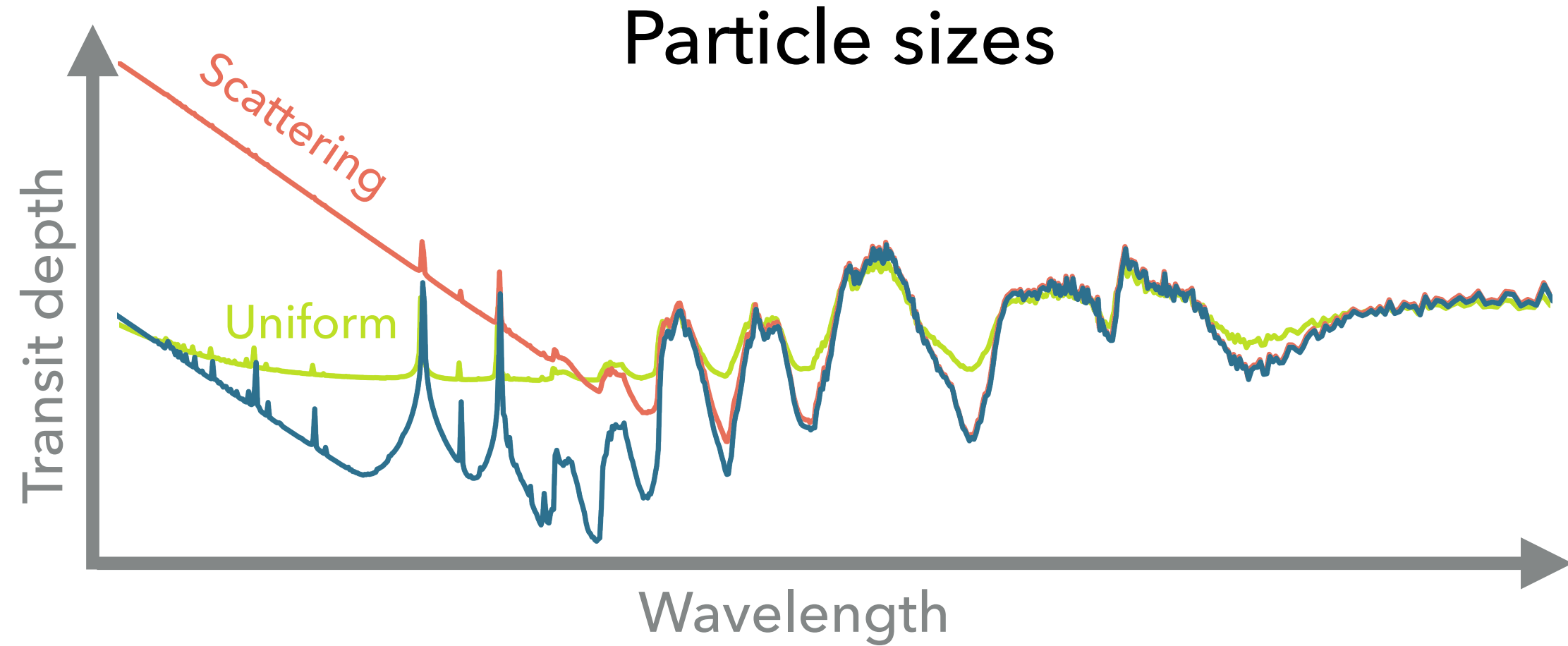


Evaluating the wavelength dependence of retrieved exoplanet properties shows that without information below 0.6 (JWST's blue limit) we cannot properly account for the impact of aerosols on the spectra



# Aerosols will be impacted by Temperature, Chemistry, and Dynamics

How do we measure the atmosphere of a transiting exoplanet?



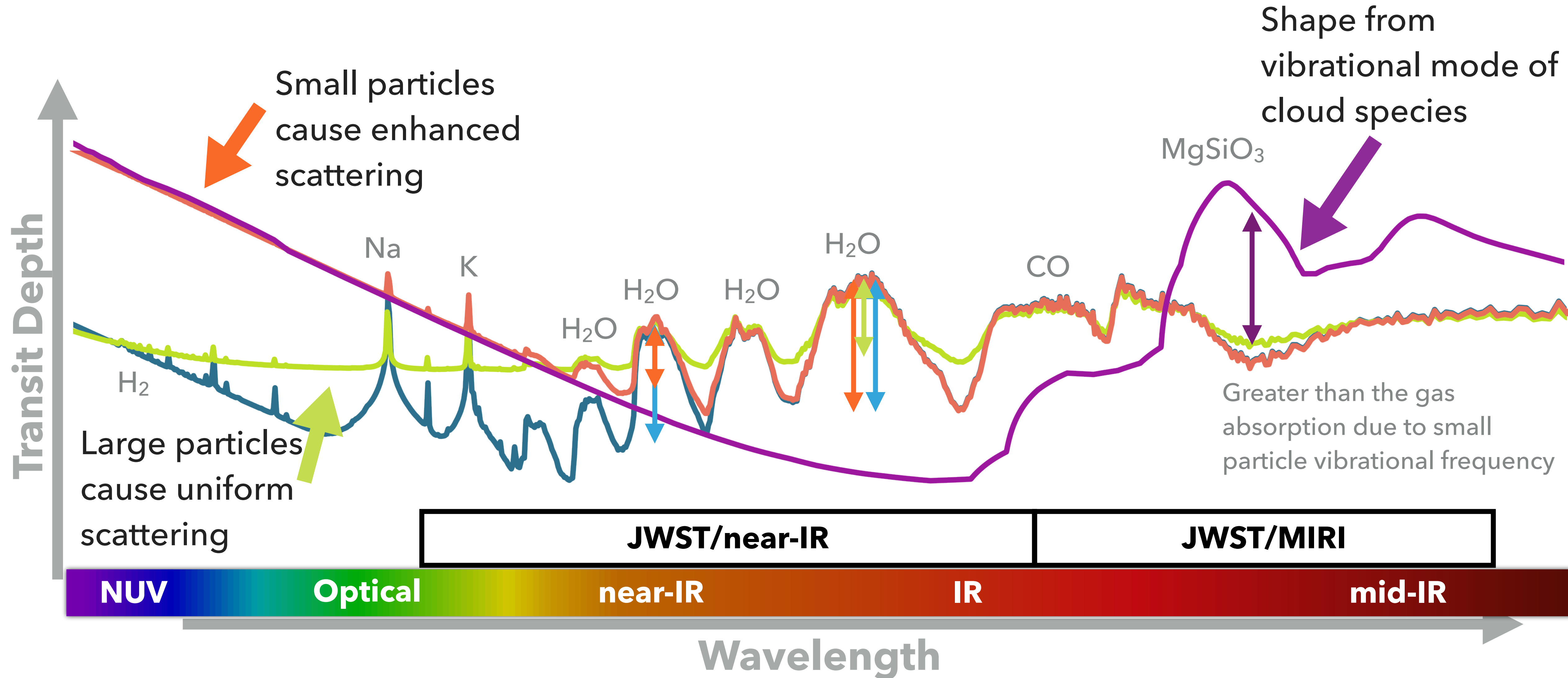
Wakeford & Sing (2015, A&A)

Gao, Wakeford, Moran & Parmentier (2021 JGReview)



# Transiting Exoplanet Atmospheres

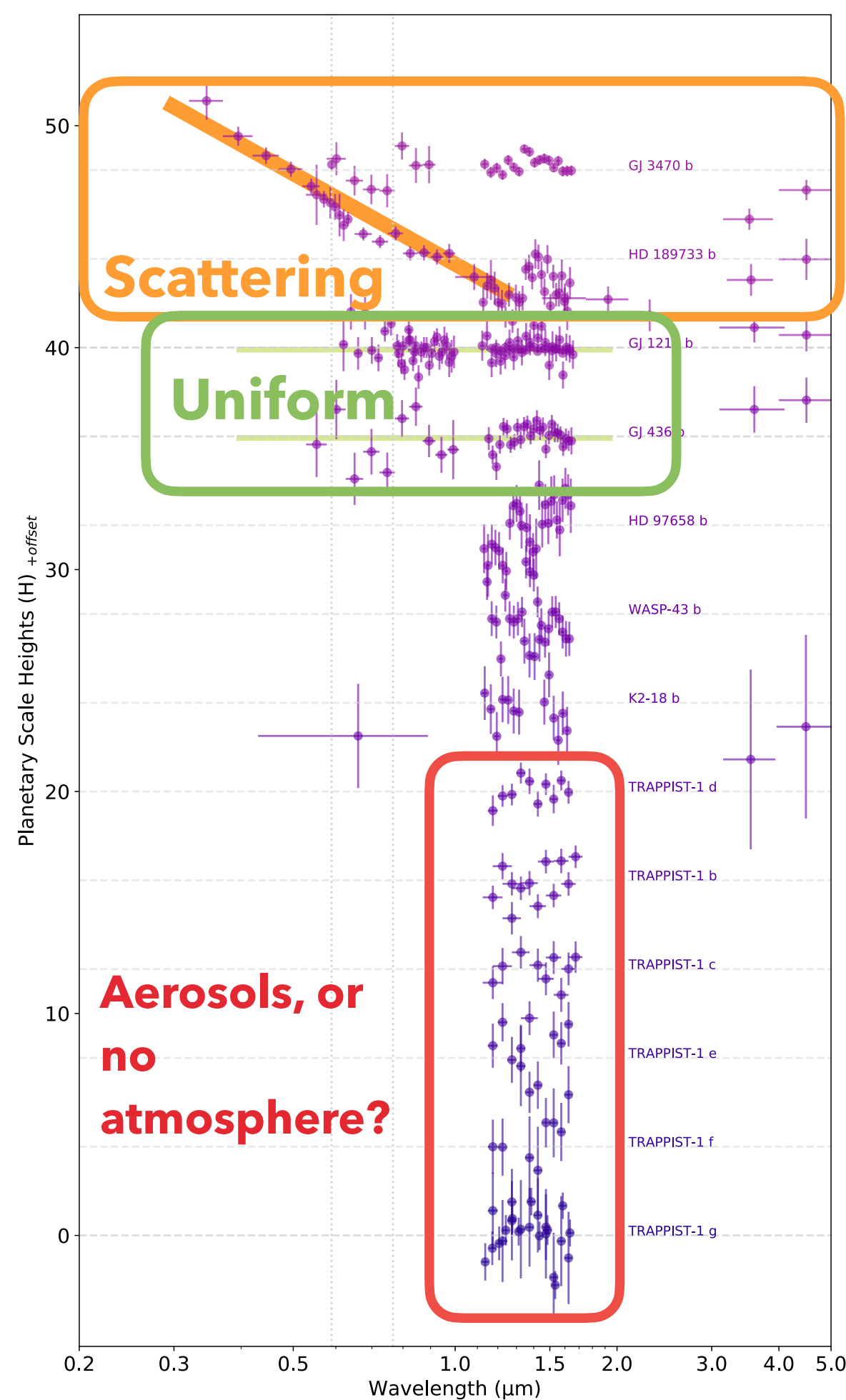
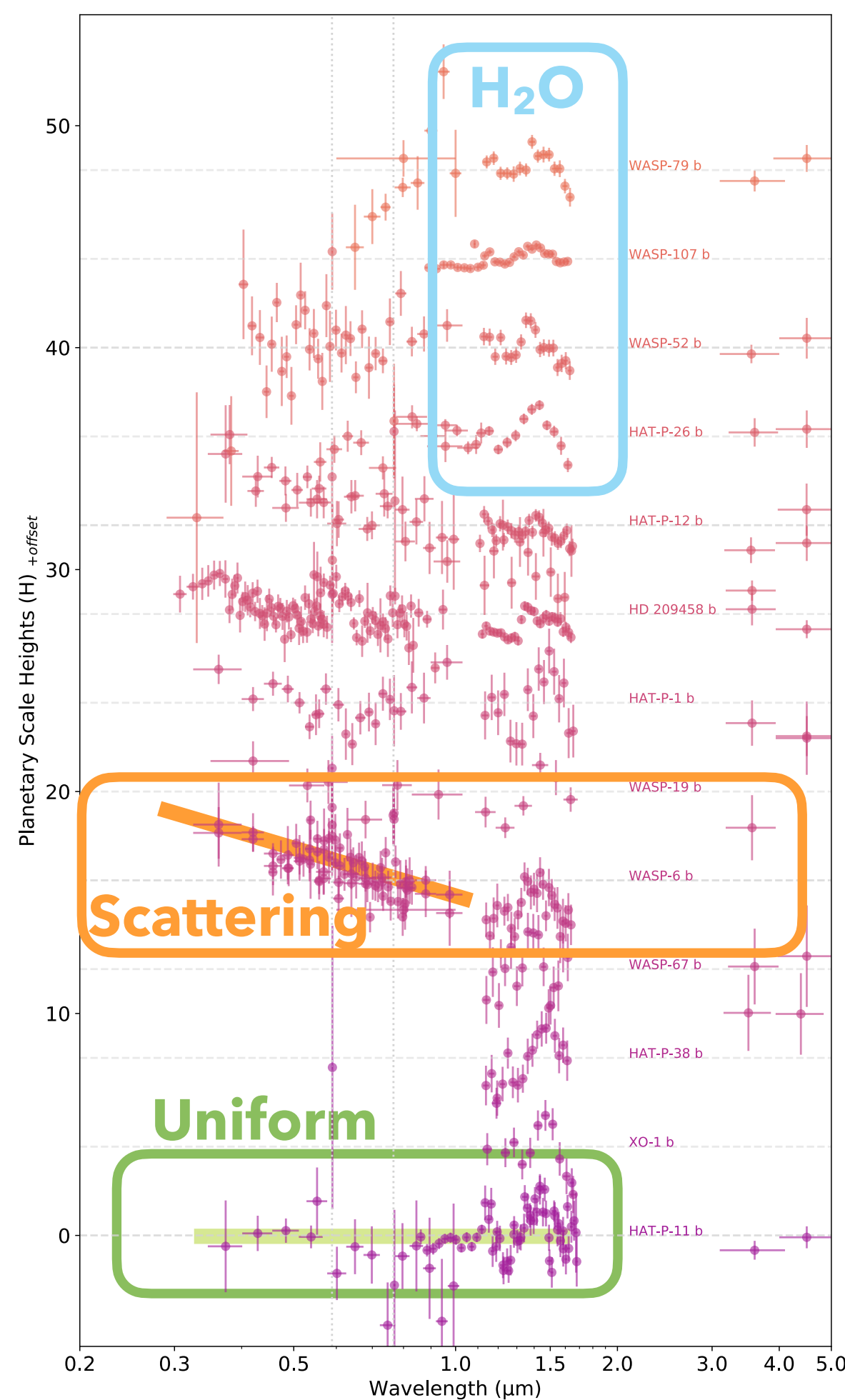
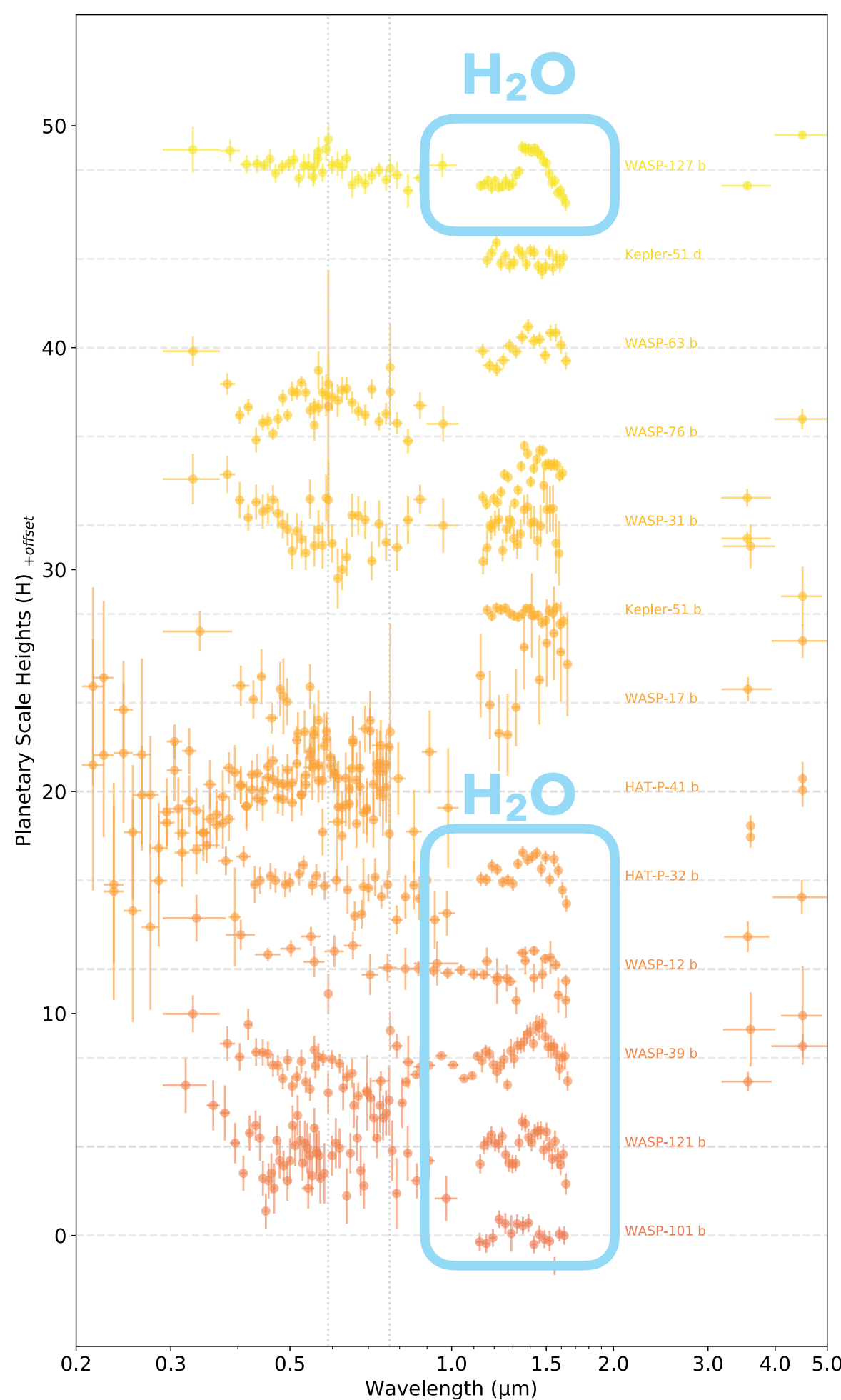
How do we measure the atmosphere of a transiting exoplanet?



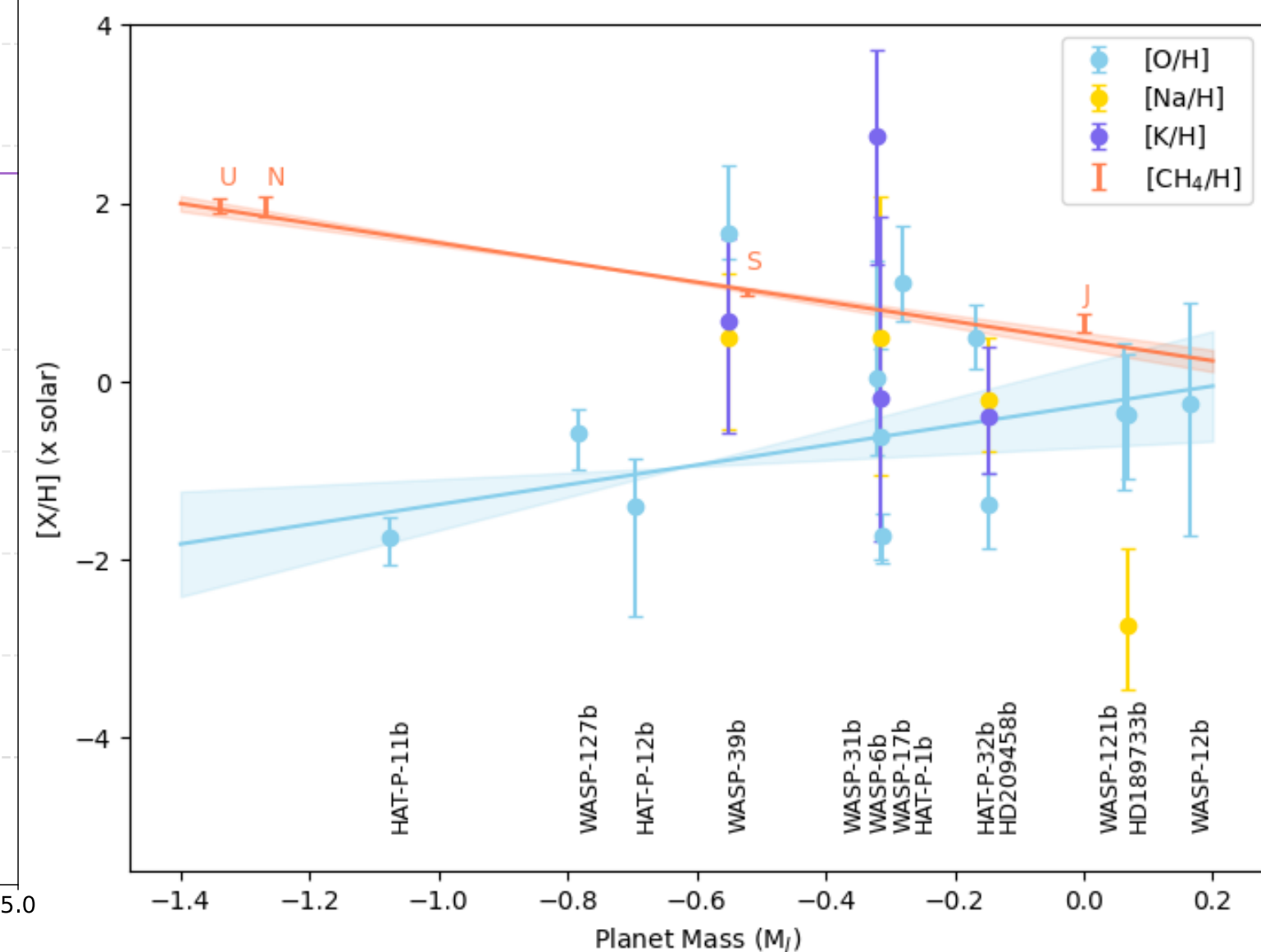
# What have we seen?



## Atoms, Molecules, and Aerosols



Hubble gave us a look at Na, K, & H<sub>2</sub>O and hints at aerosols. JWST will give us carbon-species and cloud composition and location



You can now find all these and more on NASA Exoplanet Archive!

Fairman, Wakeford & MacDonald (in prep)

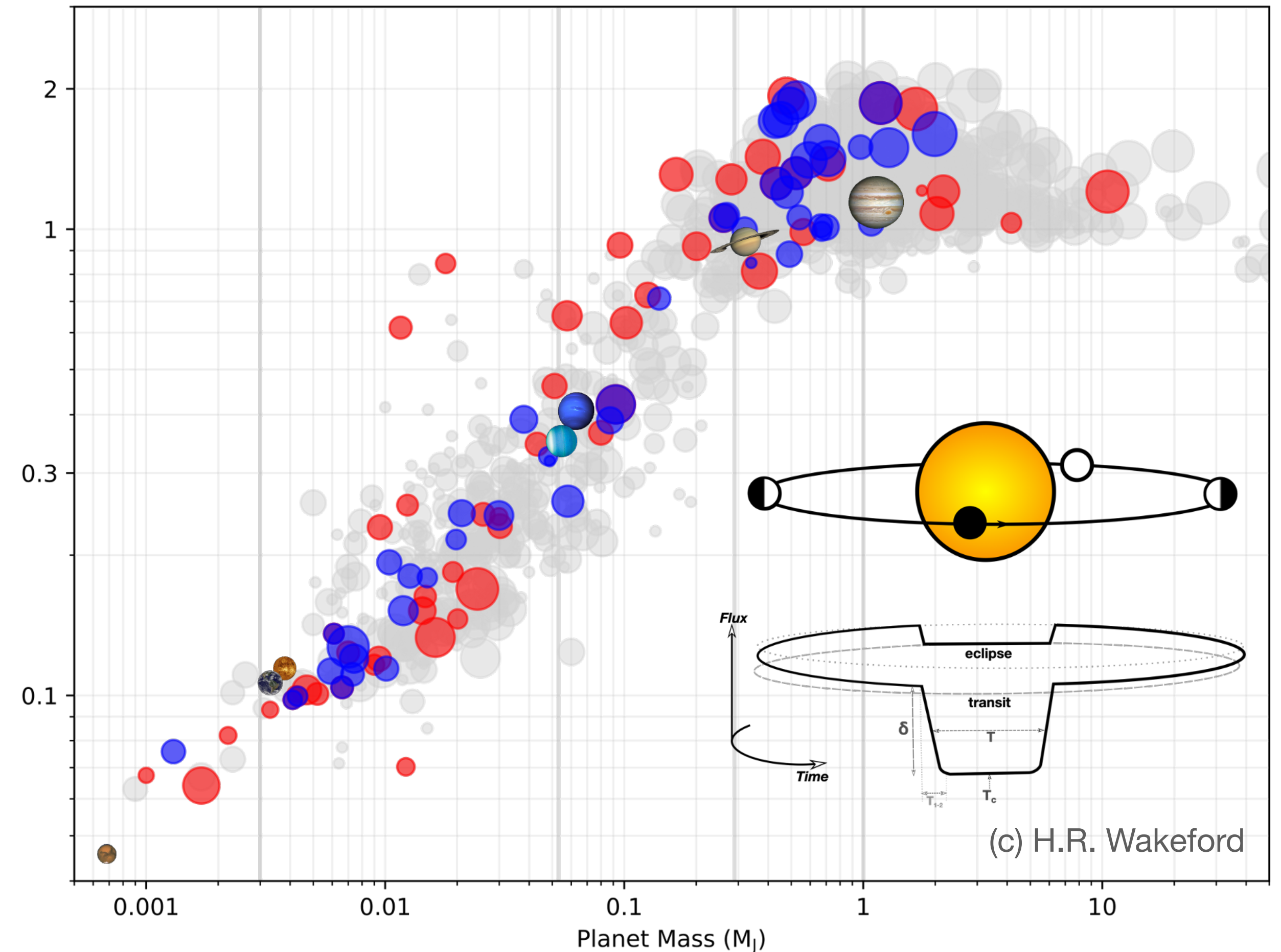


# Transiting Exoplanets with JWST: Cycle 1 & 2

111 individual exoplanets, +200 observation set-ups

## Some high level thoughts:

- Lots of love for NIRSpec/G395H observations
- Multiple large programs looking at small worlds to understand small scale atmospheres
- GTO & ERS performed comprehensive deep dives on a handful of planets (could we get this through a TAC?)
- Exciting complementary brown dwarf science
- **A HORDE of amazing ECRs leading the charge!!**



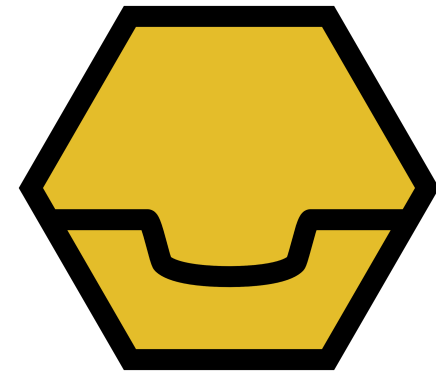
# A look to the future of exoplanets with JWST

Exciting science and opportunities

We will see  $\text{SO}_2$  again in places we don't expect



We will start to resolve cloud features in the IR and get a better handle on C/O importance



There is still a lot to learn about the instruments in different SNR regimes

